

Gravitational-wave progenitors

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Lecture #13

NCU, Summer Semester 2022

The background features a large, faint, light-colored circle centered in the upper half. Overlaid on this are several glowing, ethereal lines in shades of blue, cyan, and magenta. These lines form a complex, web-like pattern that resembles a fractal or a network of connections. The lines are semi-transparent and have a soft, glowing aura around them. The overall aesthetic is futuristic and scientific.

*Previously
on GW-progenitors...*

Population synthesis on *binaries*

- **NOT** the same thing as binary evolutionary simulations

*meaning: 'detailed' evolutionary computations e.g. with MESA
(yes, MESA can run binaries too)*

Remember the Initial Mass Function (IMF)?

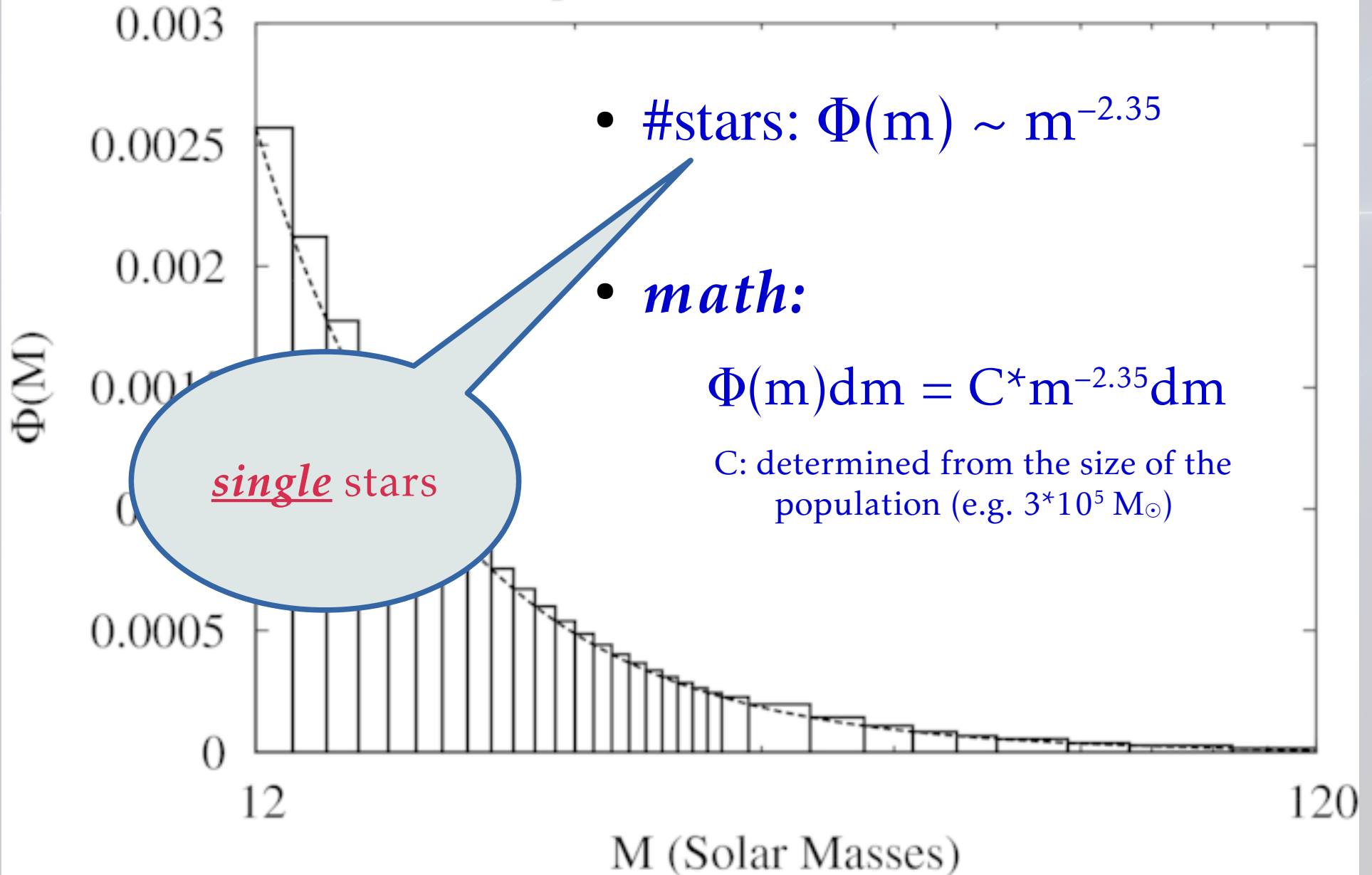
Pop.synth. starts with that.

But binaries make life complicated.

REMINDER:

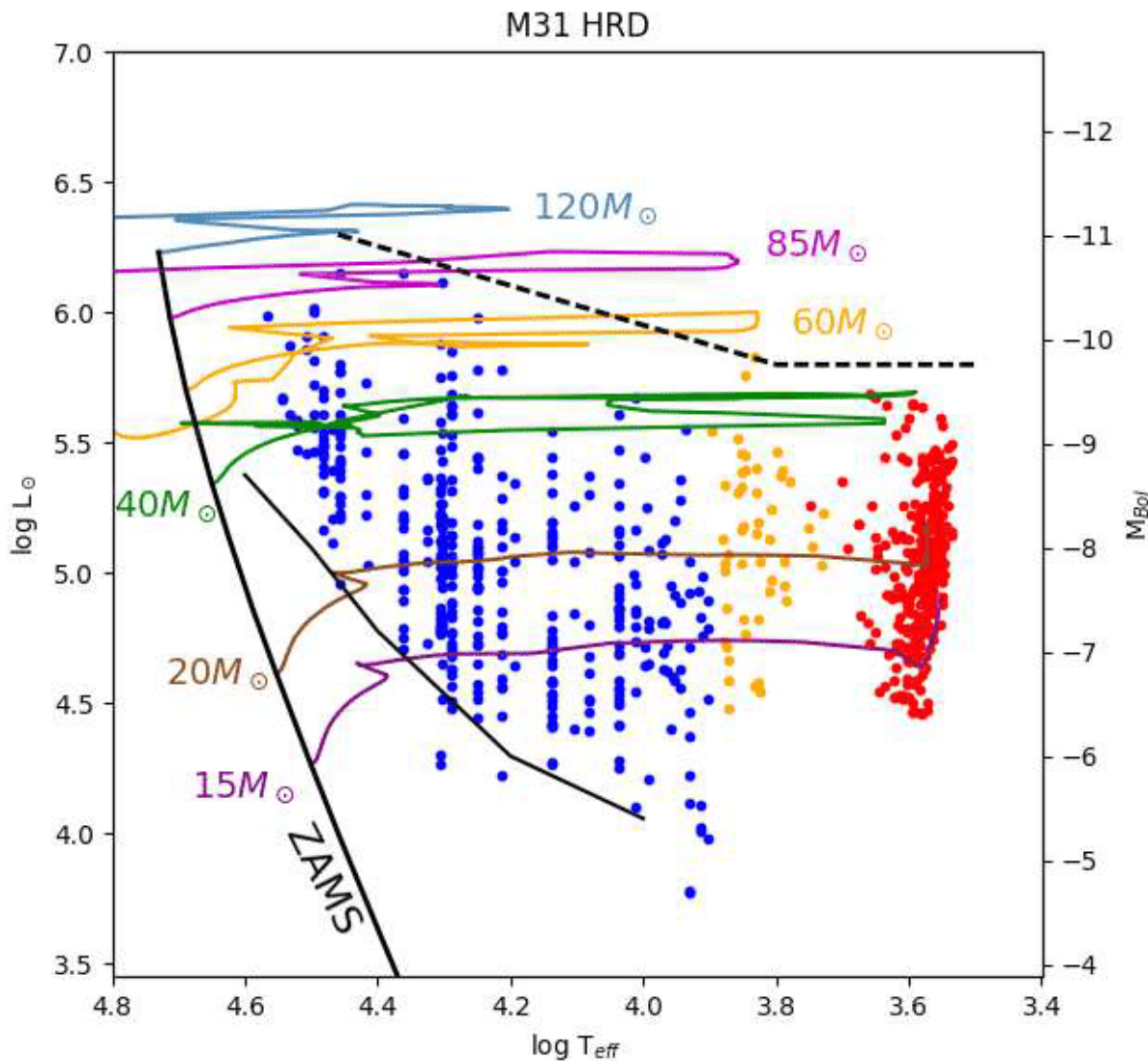
The Initial Mass Function (IMF)

Salpeter Initial Mass Function



(*single* stars)

Let's think!



- How would you “convert” between the lines and the dots?
- *Meaning:*
 - how would you compare theoretical predictions with observations?

HR-diagram

Age, Mass, Radius, T_{eff} [K], $\log(L/L_{\odot})$, Massloss rate...



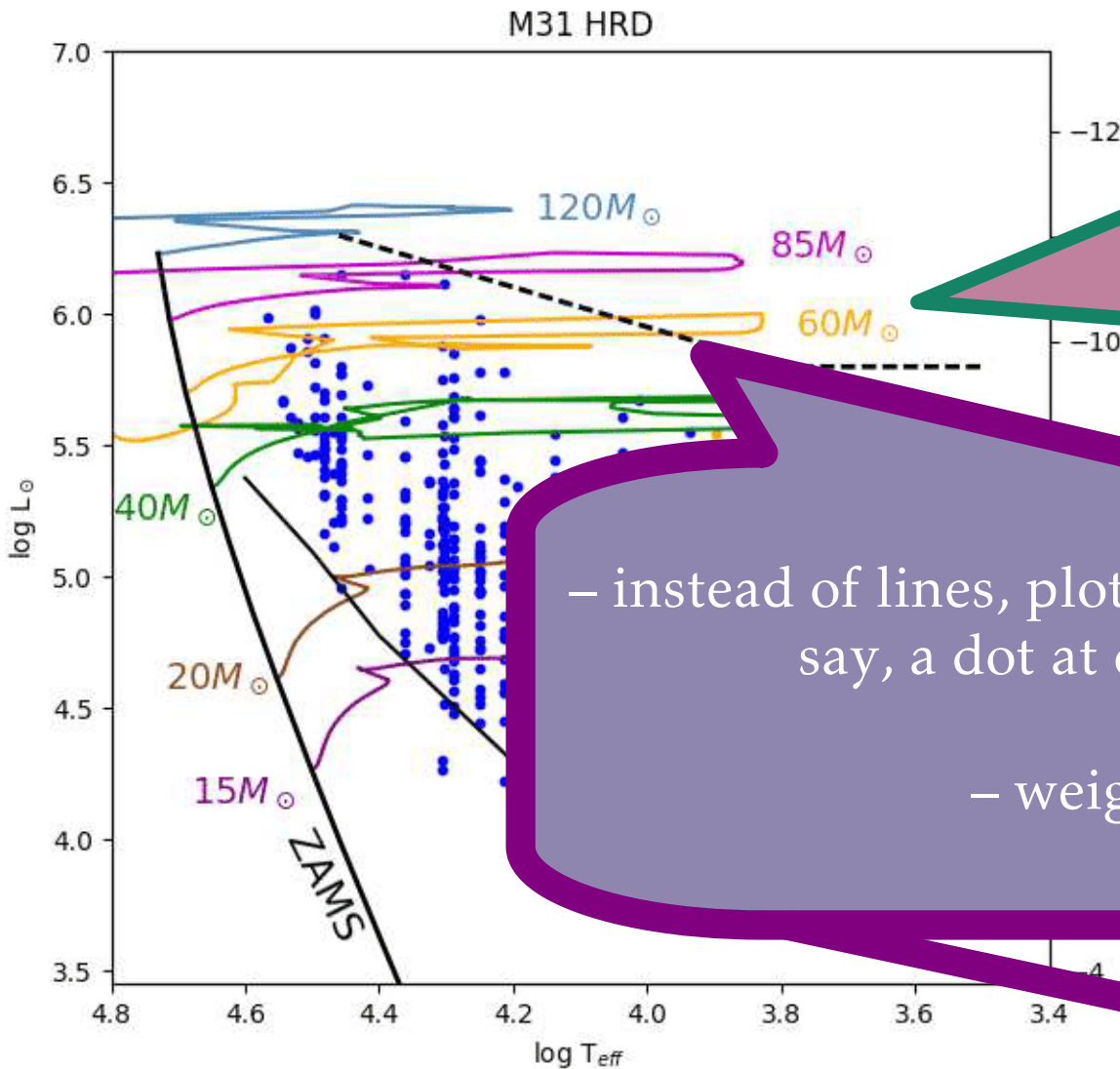
```

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2# MESA revision number = 11701
3# -----
4# Yinit      Zinit  [Fe/H]  [a/Fe]  v/vcrit
5# 0.2511    1.42857E-03  -1.00   0.00    0.00
6# -----
7#      initial mass  N_pts  N_EEP  N_col  phase  type
8# 1.9999727046E+01  808    8      73    YES   high-mass
9# EEPs:      1      202    353    454    605    631    707    808
10# -----
11#
12#          1          2          3          4          5
13#          star_age  star mass  star mdot  log dt      he_core mass
14# 2.7320575584293762E+005  1.9999727045763130E+001  -6.6667141481350412E-009  4.6121780058570057E+000  0.000000000000000E+000
15# 2.7345019073205121E+005  1.9999725407394834E+001  -6.6668930715861210E-009  4.6125719424045064E+000  0.000000000000000E+000
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17# 2.7393906051027833E+005  1.9999722130658245E+001  -6.6672509184882791E-009  4.6133598154995070E+000  0.000000000000000E+000
18# 2.7418349539939192E+005  1.9999720492289949E+001  -6.6674298419393581E-009  4.6137537520470087E+000  0.000000000000000E+000
19# 2.7442793028850551E+005  1.9999718853921653E+001  -6.6676087653904380E-009  4.6141476885945094E+000  0.000000000000000E+000
20# 2.7467236517761904E+005  1.9999717215553360E+001  -6.6677876888415162E-009  4.6145416251420093E+000  0.000000000000000E+000
21# 2.7491680006673269E+005  1.9999715577185061E+001  -6.6679666122925961E-009  4.6149355616895100E+000  0.000000000000000E+000
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```

(*single* stars)

Let's think!

number ratio of
MS vs. RSG stars



- pick lines according to IMF
(cf. initial mass column)
- compute how much time they all spend as blue stars
- and how much as red stars

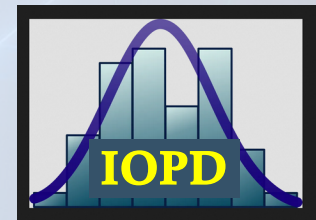
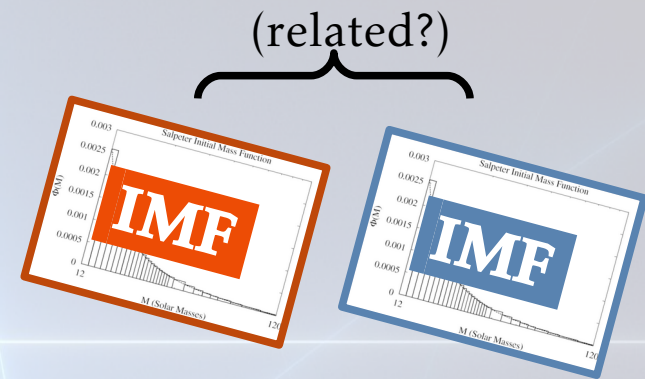
- instead of lines, plot the evolutionary tracks as dots!
say, a dot at every 10 thousand year
- weight with the IMF

an actual (simulated)
stellar population!

*simulated =
“synthetic”*

Population synthesis on *binaries*

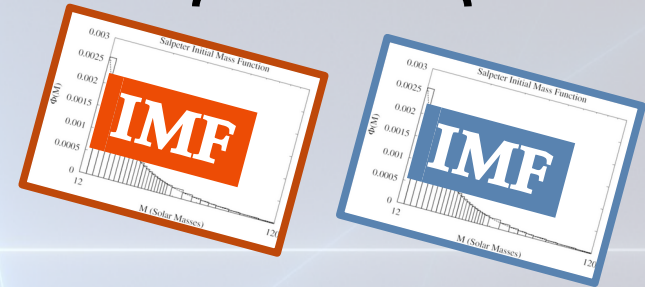
- 2 stars instead of 1
 - both have their individual IMFs
- orbital separation!
 - Initial Orbital Period Distribution
same kind of thing as the IMF but for the period,
i.e. an observation-based statistical distribution
- plus a *lot* of assumptions about the evolution
 - mass transfer (stable/unstable? conservative/non-conservative? ...)
 - Common Envelope phase (outcome: merger or survival?
separation afterwards?)
 - supernova physics... and the kick.



Population synthesis on *binaries*

- 2 stars instead of 1
 - both have their own individual IMFs
- orbital separation
 - Initial Orbital Period (IOPD) is the same kind of thing as the IMF, i.e. an observation-based statistical distribution
- plus a *lot* of assumptions about the evolution
 - mass transfer (stable/unstable? conservative/non-conservative? ...)
 - Common Envelope phase (outcome: merger or separation afterwards?)
 - supernova physics... and the kick.

(related?)

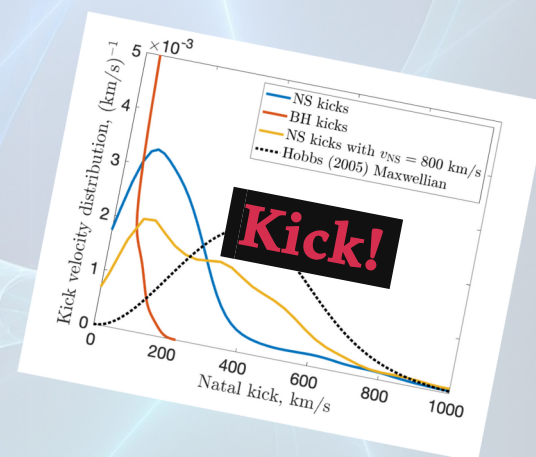
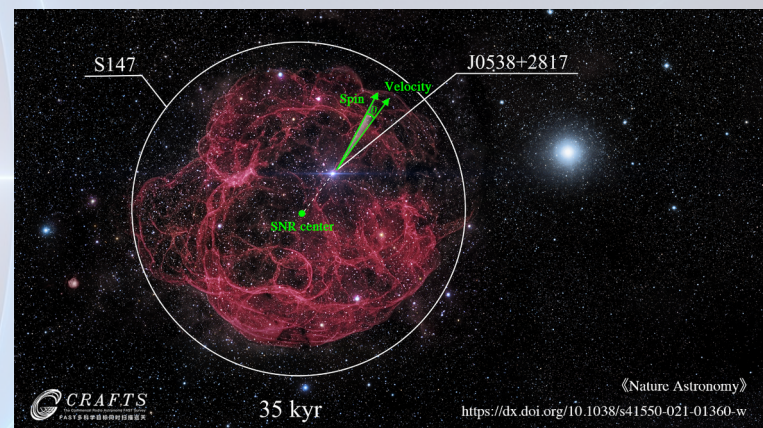


under active research

on top of what we already don't know about *single* stars' evolution

Kicks

- happens for single-star supernovae too
= natal kick
which happen when the NS is born
also see: pulsar kick, NS kick, SN kick
 - needs: asymmetric explosion
- in binaries, one SN may kick out the companion
- survival rate is uncertain
 - but in pop.synth., drawn from a – *you guessed it* – statistical distribution :D

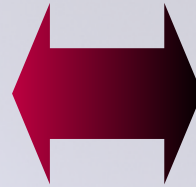


cf. Mandel & Müller (2020)

IMPORTANT . . .

Exam
warning!
:P

- Stellar evolution modelling



- Synthetic population modelling

- based on first principles
(5 stellar equations)
- follows one star's life at the time
- IMF is not yet considered
- result is *a line* ('track') in the HR-diagram

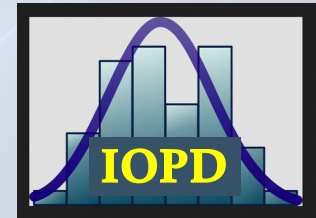
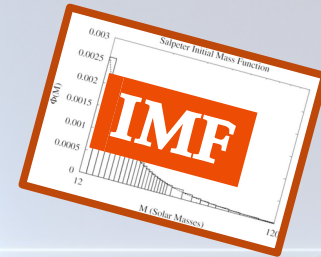
- relies on stellar evolution modelling
- does not simulate the individual star's life (typically)
- IMF is taken into account
- result is a *statistically meaningful* prediction about a *population*

The background features a large, faint circle in the center. Overlaid on this are several glowing, ethereal lines in shades of blue, purple, and pink. These lines form a complex, web-like pattern that resembles a stylized butterfly or a delicate lace design. The overall aesthetic is soft and futuristic.

Today...

...the last steps!

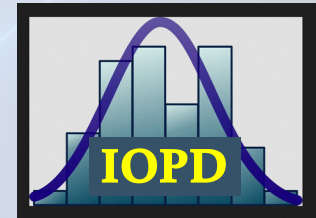
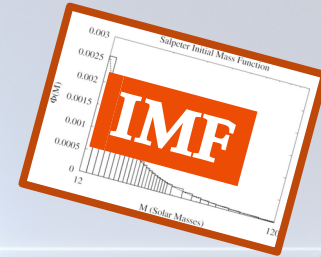
Star-formation history



Not enough!

Star-formation history

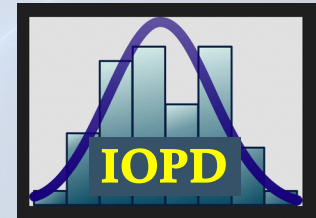
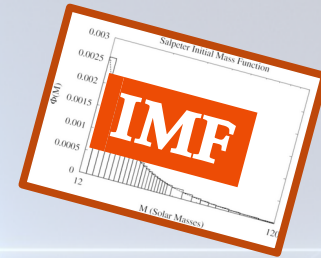
- We need to know the *history* of how the stars are being born...



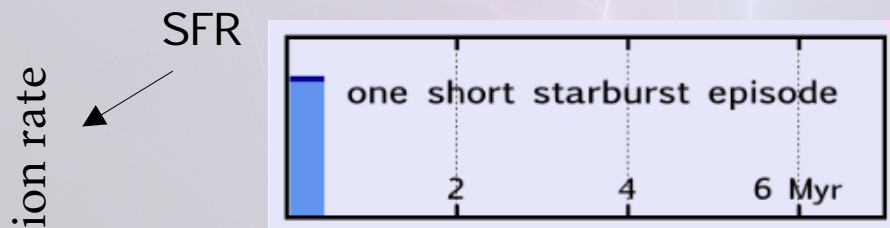
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Star-formation history

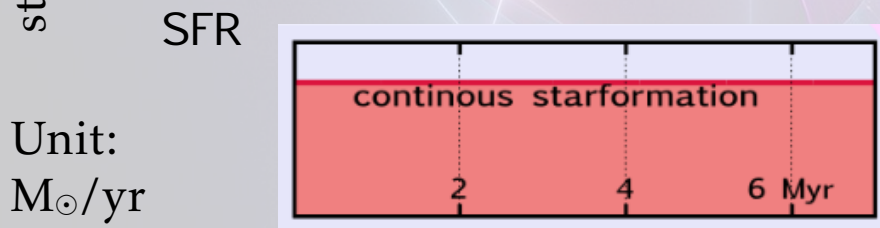
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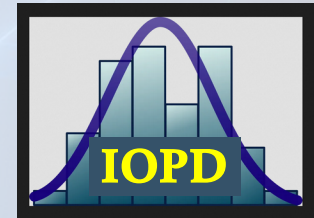
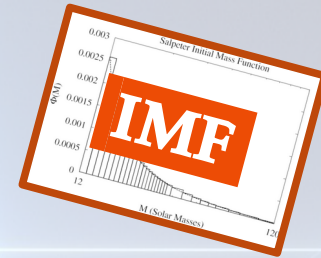


or anything else

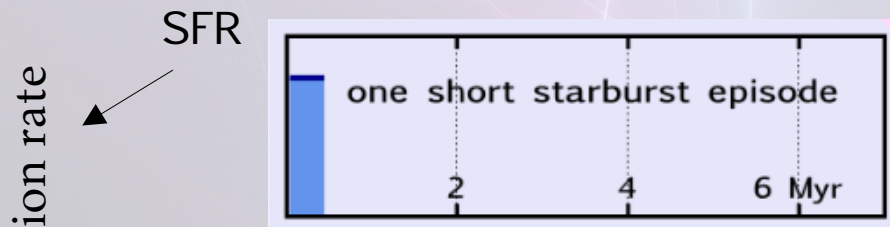


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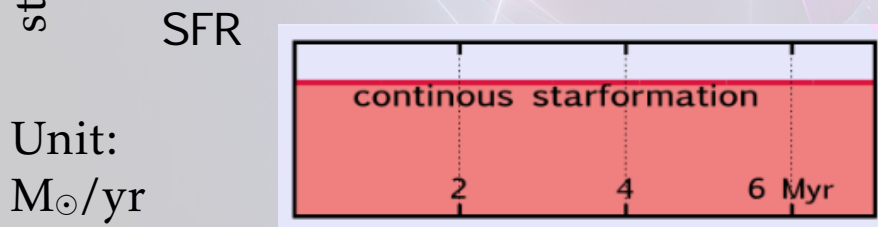
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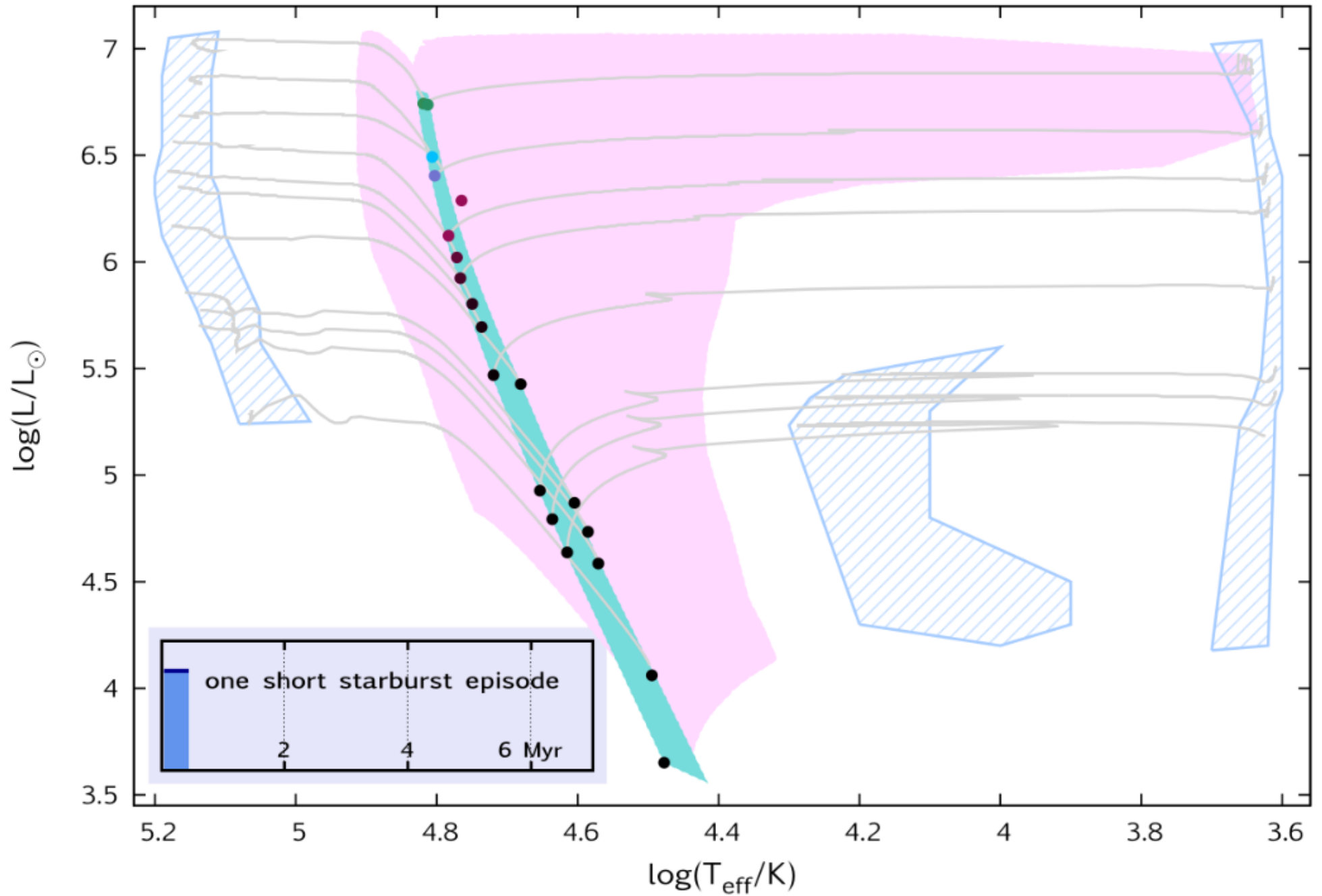


or anything else

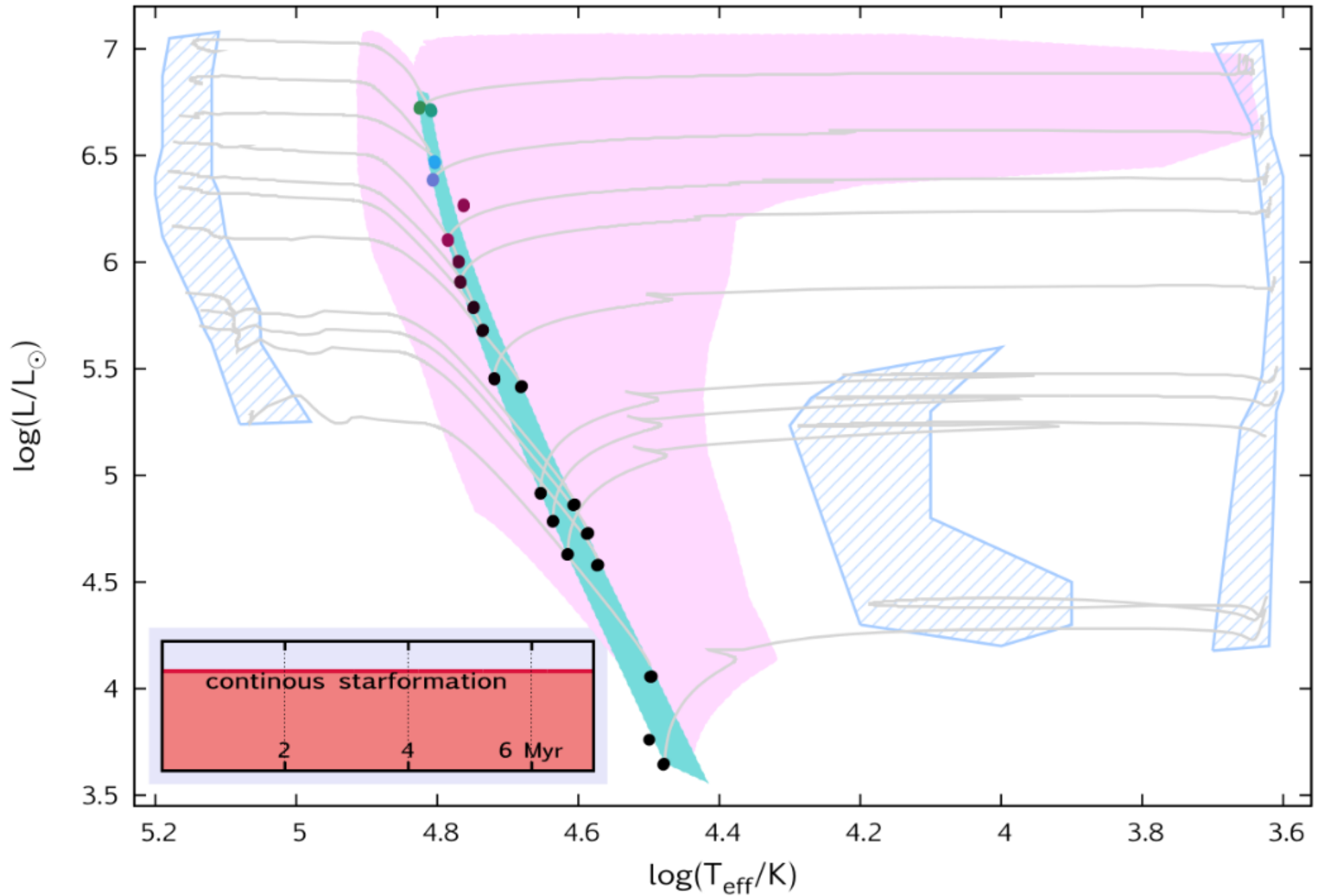


We need all these to do
(binary) population synthesis.

Simulating a galaxy... or starcluster

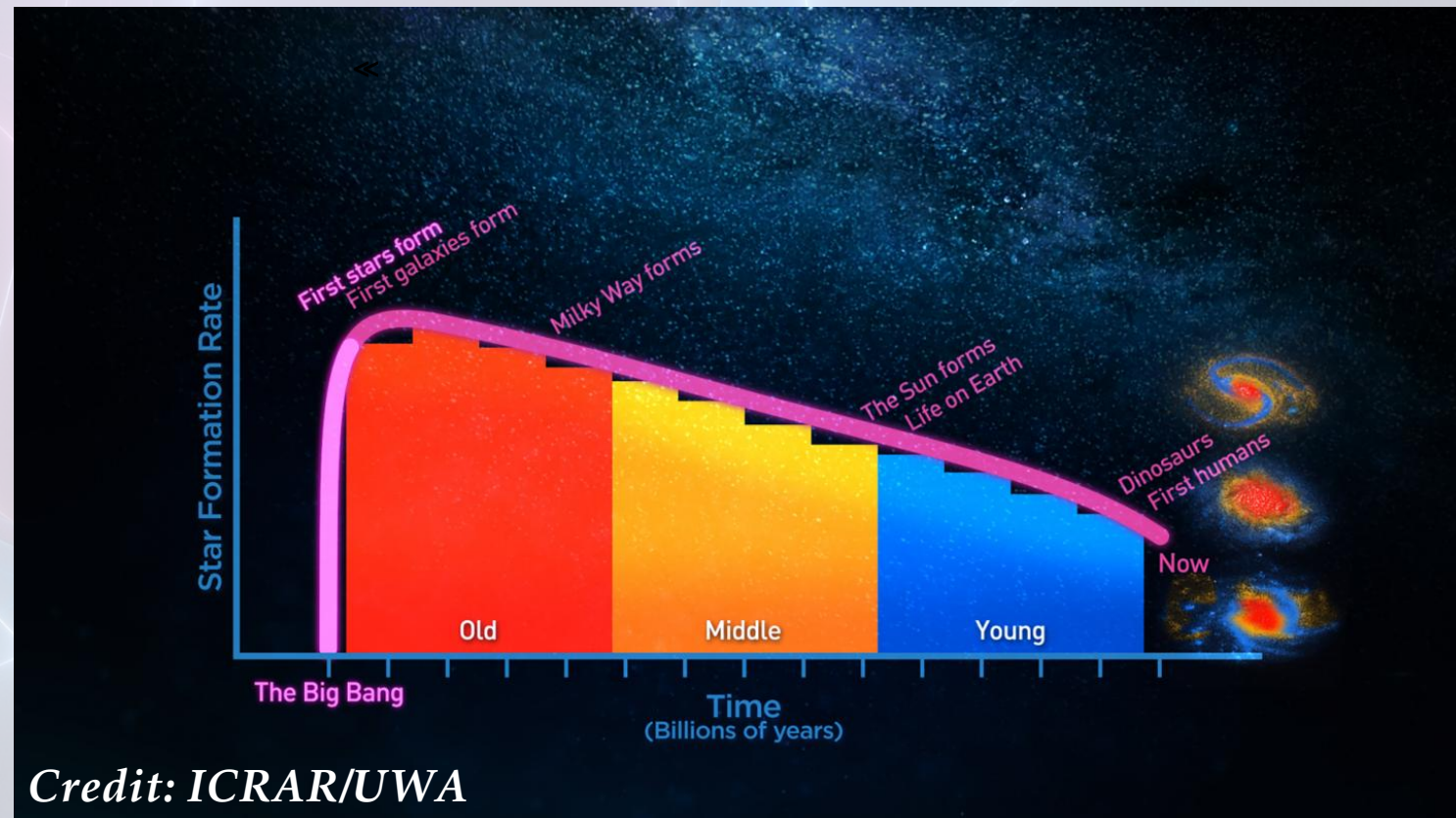


Simulating a galaxy... or starcluster



From star-formation history to *cosmic* star-formation history

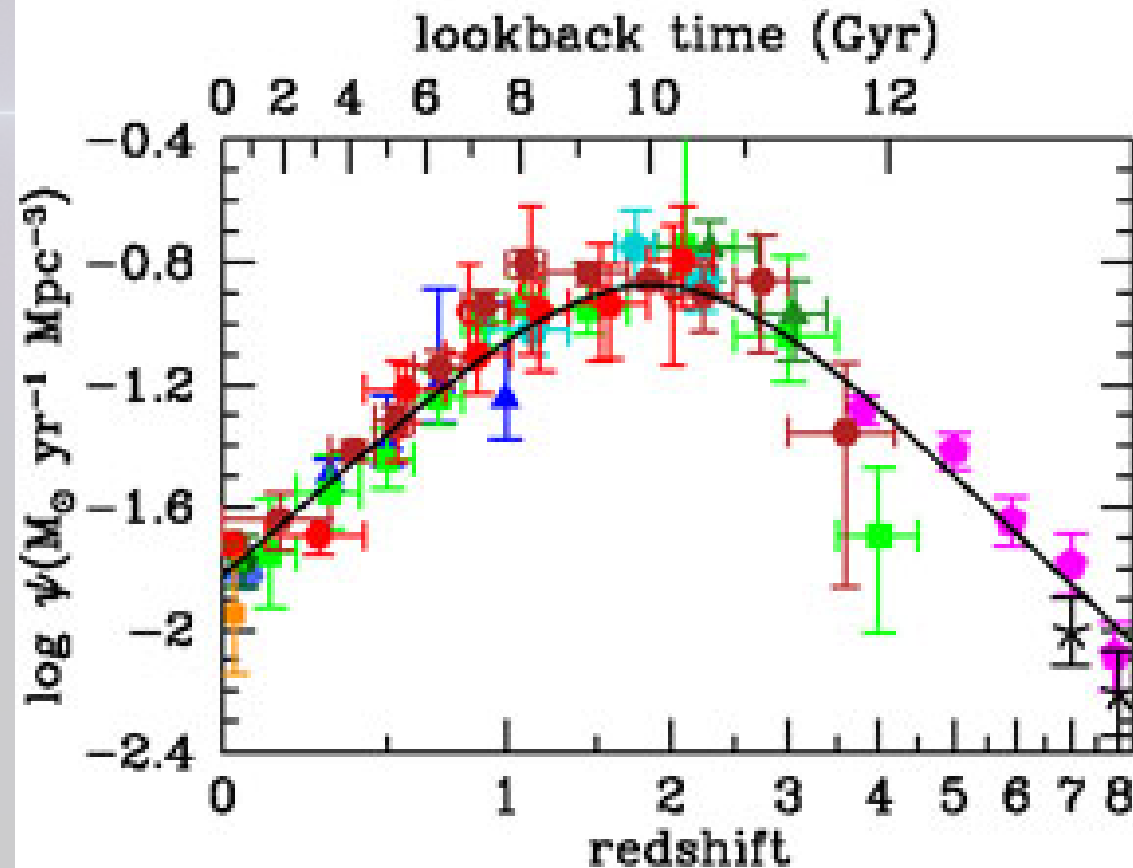
- This is what we need to predict GW-event rates from synthetic populations



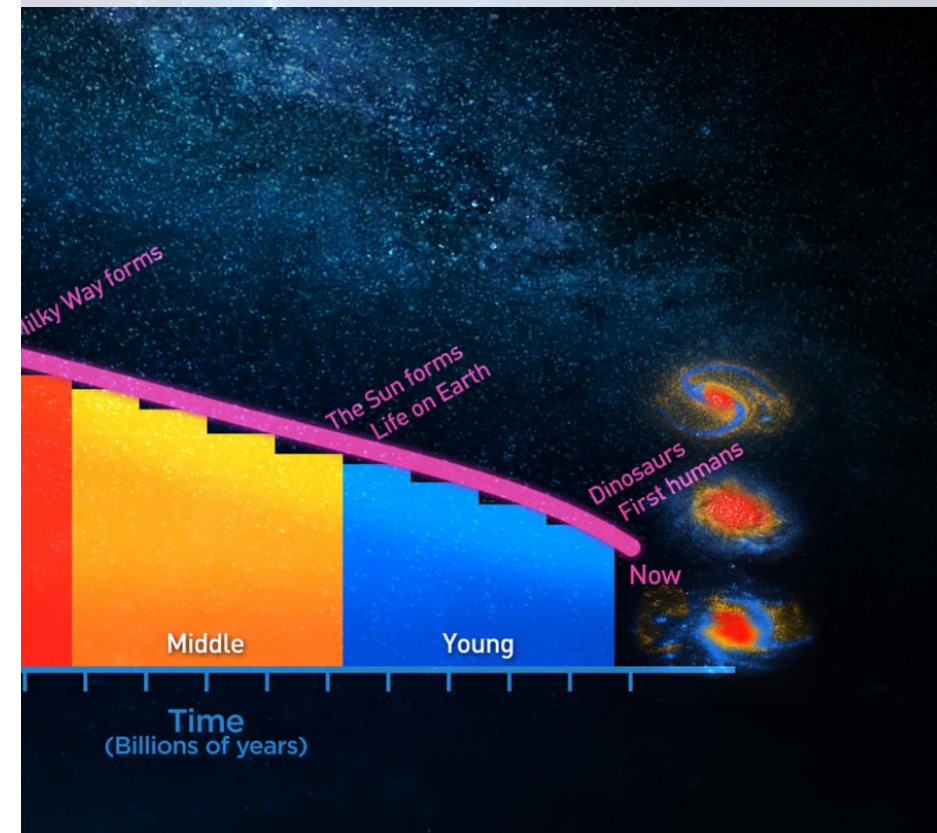
From star-formation history to *cosmic* star-formation history

predict GW-event rates

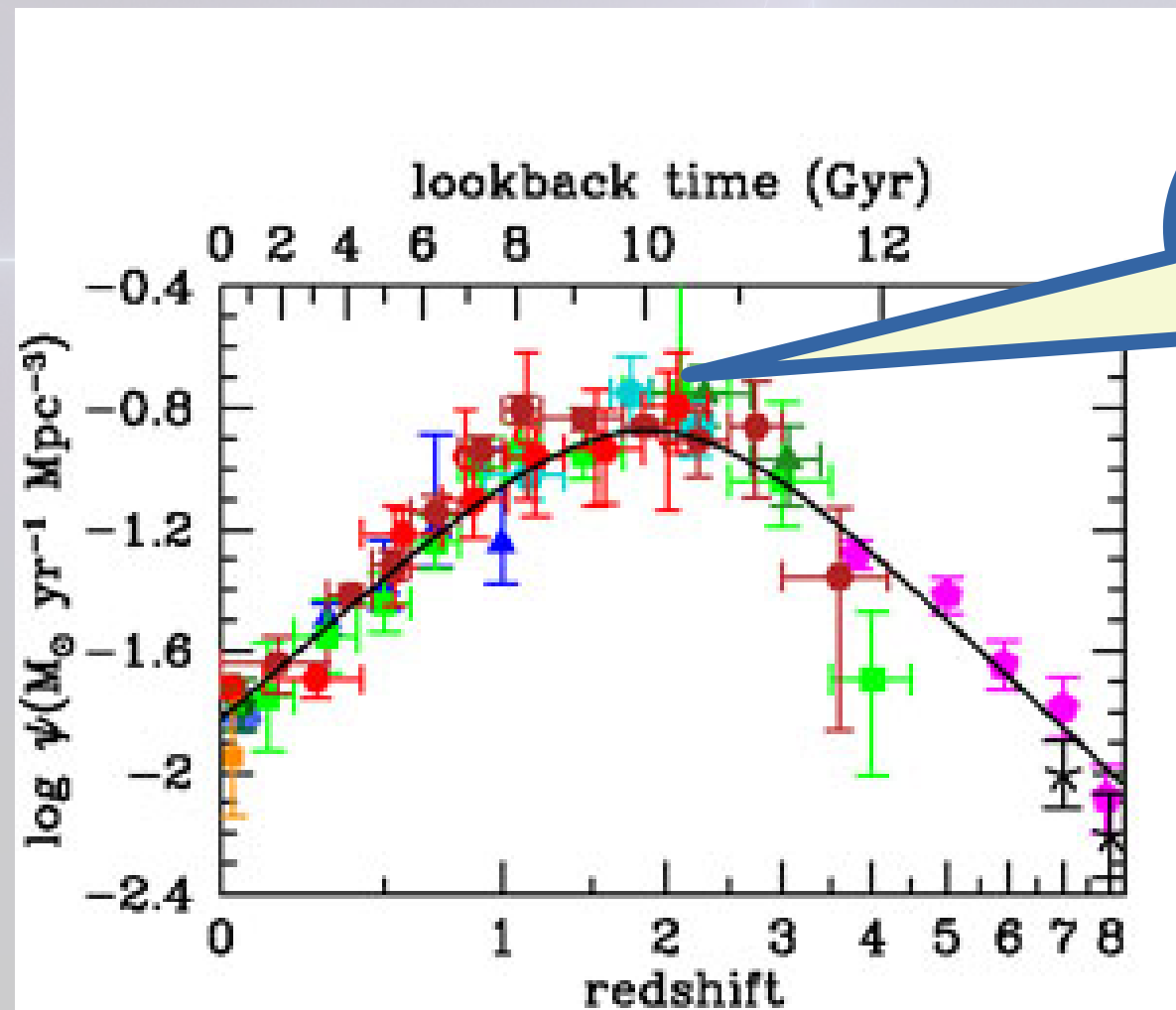
S



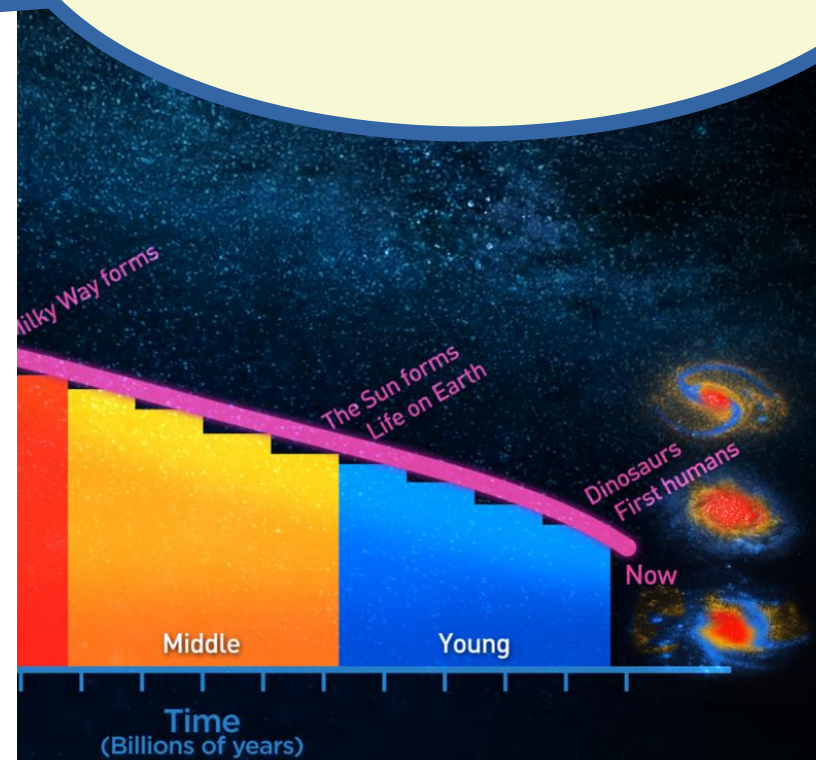
Credit: Madau & Dickinson (2014)



From star-formation history to *cosmic* star-formation history

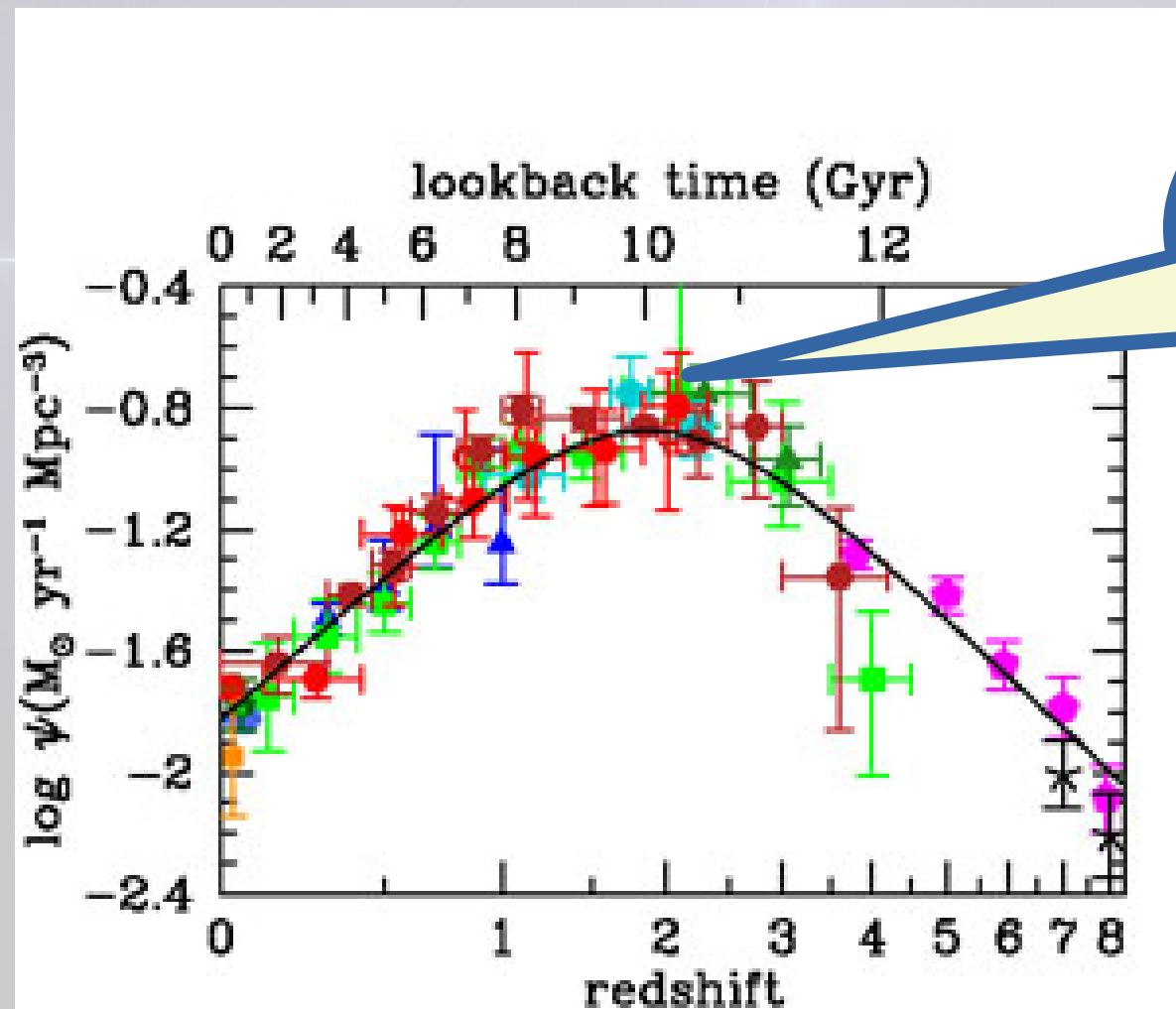


Peaking: somewhere around $z = 2$, when the Universe was ~ 3.5 Gyr old



Credit: Madau & Dickinson (2014)

From star-formation history to *cosmic* star-formation history



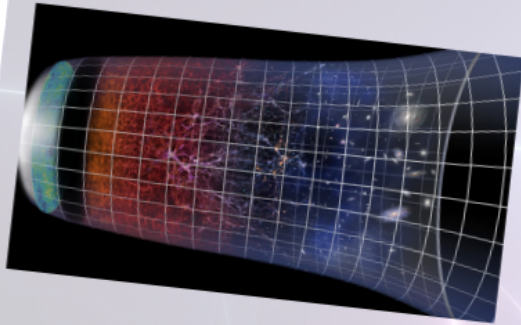
Peaking: somewhere around $z = 2$, when the Universe was ~ 3.5 Gyr old

Note:
massive stars live short lives!
 $2\text{-}20 \text{ Myr} \ll 13 \text{ Gyr}$

Credit: Madau & Dickinson (2014)

Now we can answer the original *(kind of)*
question of this whole lecture series

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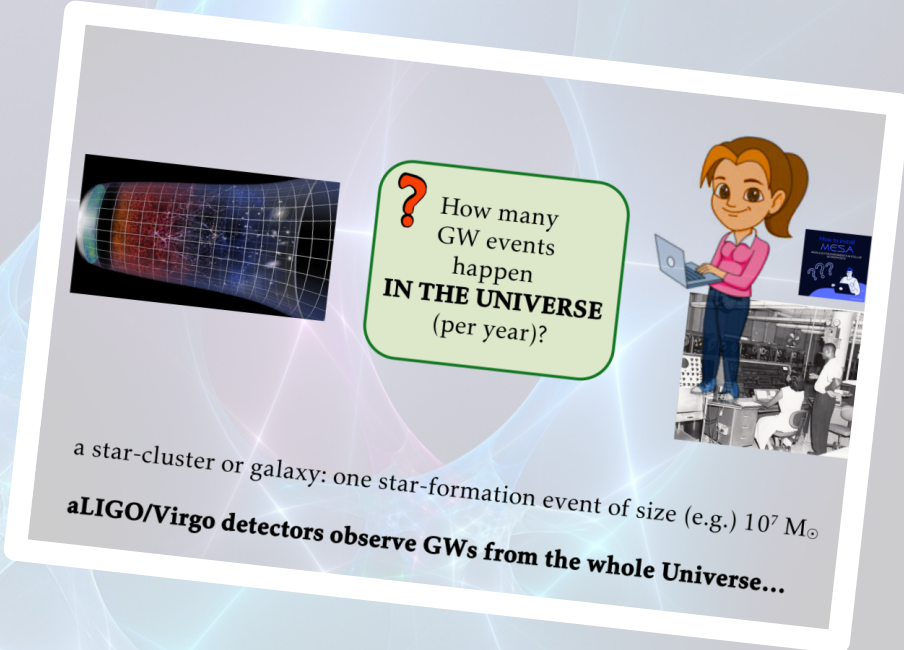


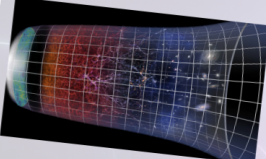
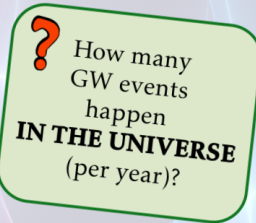


? How many
GW events
happen
IN THE UNIVERSE
(per year)?



a star-cluster or galaxy: one star-formation event of size (e.g.) $10^7 M_{\odot}$
aLIGO/Virgo detectors observe GWs from the whole Universe...

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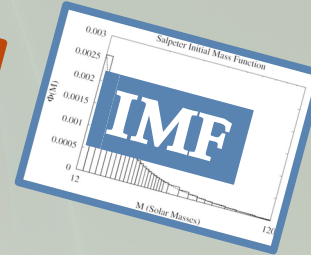
stellar models

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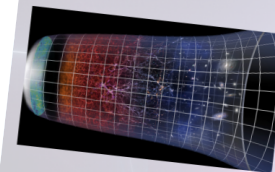
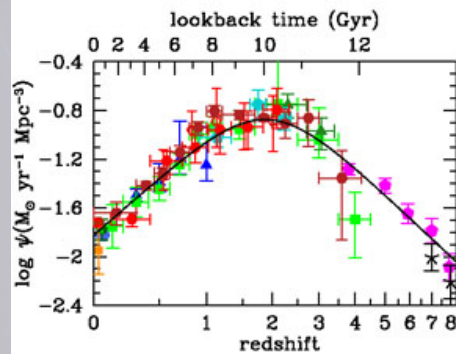


initial distributions



+ a lot of assumptions about binary physics

cosmic SFH



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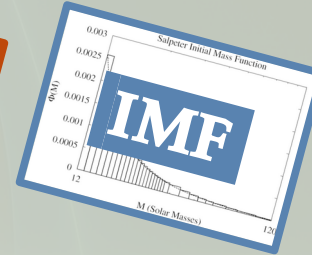
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15# 2.7369462562116400E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
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21# 2.7516123495584622E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
22# 2.7540566984495980E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
23# 2.7565010473407339E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
24# 2.7589453962318092E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
25# 2.7613897451230051E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
26# 2.7638340940141404E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
27# 2.7662784429052763E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
28# 2.7687227917964122E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
29# 2.7711671406075481E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
30# 2.7736114095766848E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
31# 2.7760558384698193E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
32# 2.7785001873669552E+005  1.9999725407394034E+001  -6.6668930715061210E-009  4.6125719424045504E+000  0.000000000000000E+000
    
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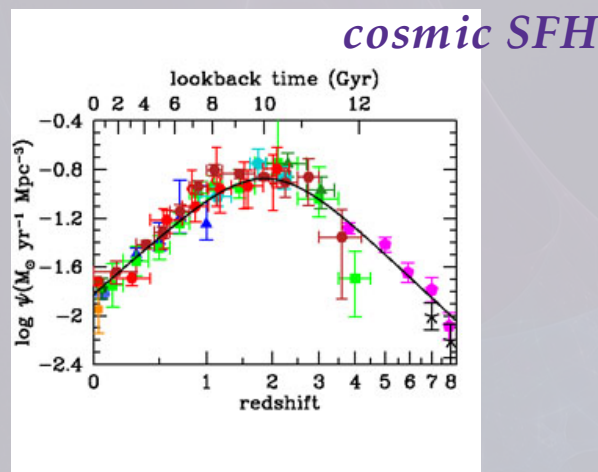


initial distributions



+ a lot of assumptions about binary physics

cosmic SFH



Important piece of math:
Convolution
of two functions

$$(f * g)(t) := \int_{-\infty}^{\infty} f(\tau)g(t - \tau) d\tau.$$

Some more terms

- Lookback time:
 - difference between the age of the Universe *now* (at observation) and the age of the Universe when the photons* were emitted (from the given object).
**grav.waves*
- Delay time:
 - the time it takes for a binary system to (1) evolve both stars, then (2) spiral in due to the emission of (undetectably weak) gravitational waves, and then (3) merge (emitting ((potentially)) detectable grav.waves). Typically: ~10 Myr – 13.77 Gyr

Even some more terms

- Chirp mass:
$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$

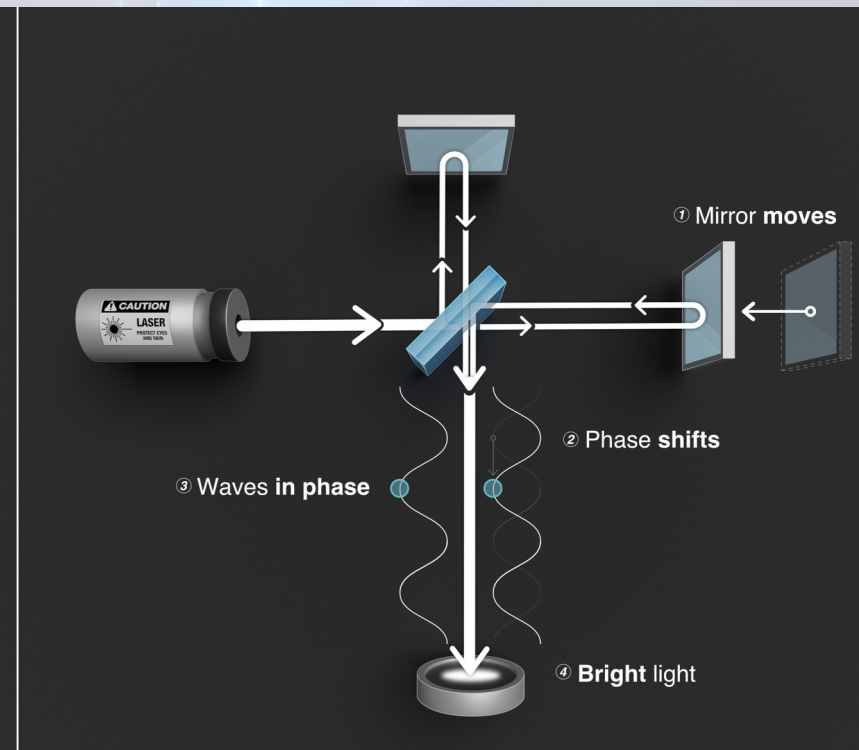
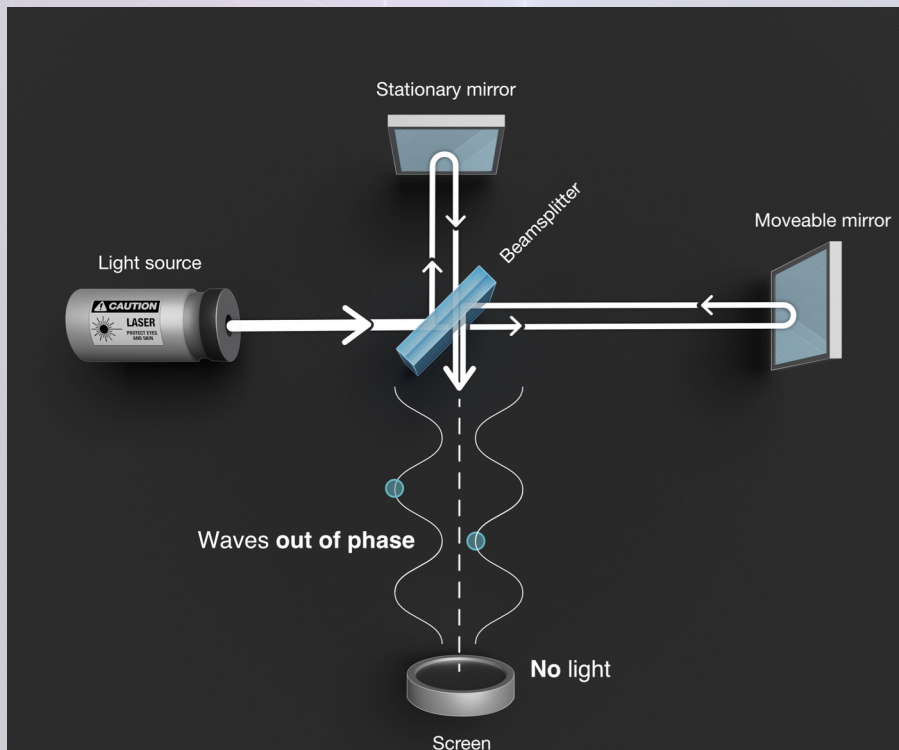
this is what can be directly derived from a measured GW-signal to derive m_1 and m_2 , a strong signal with good resolution is needed

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- Interferometer:



Credit: S. Kelley/NIST

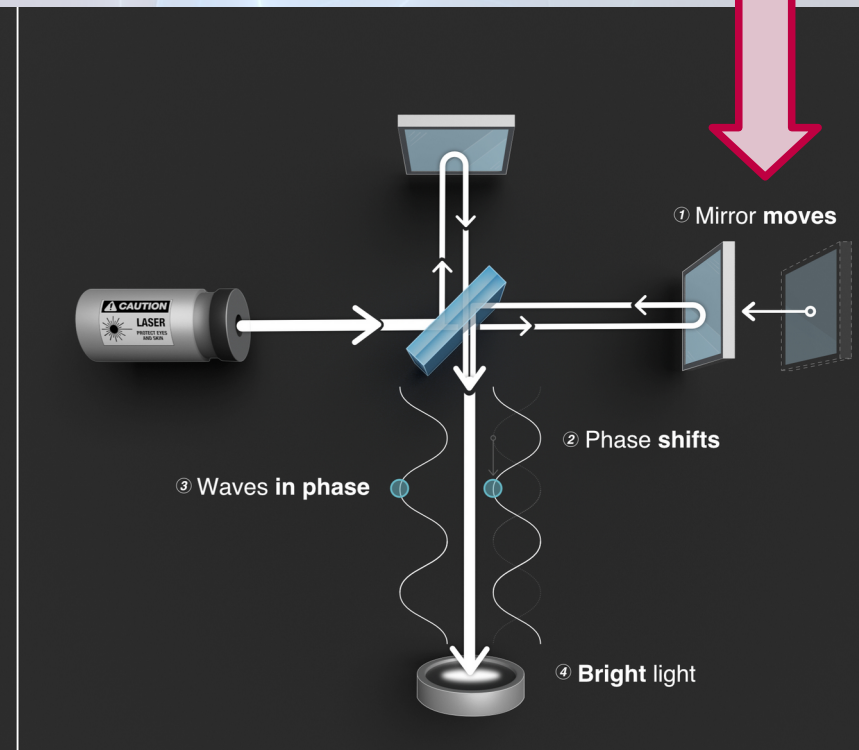
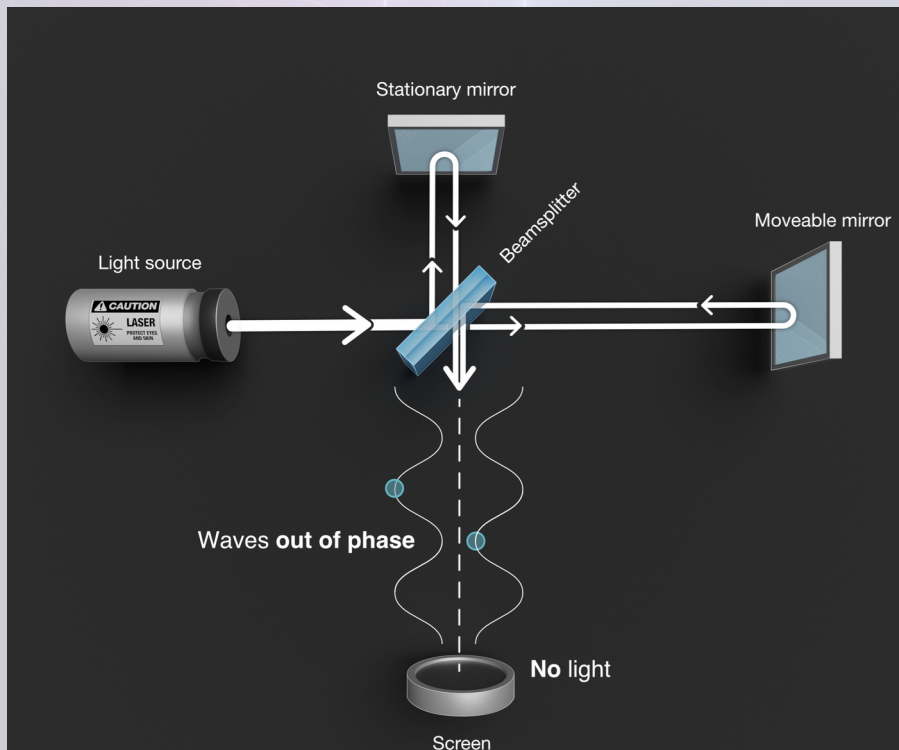
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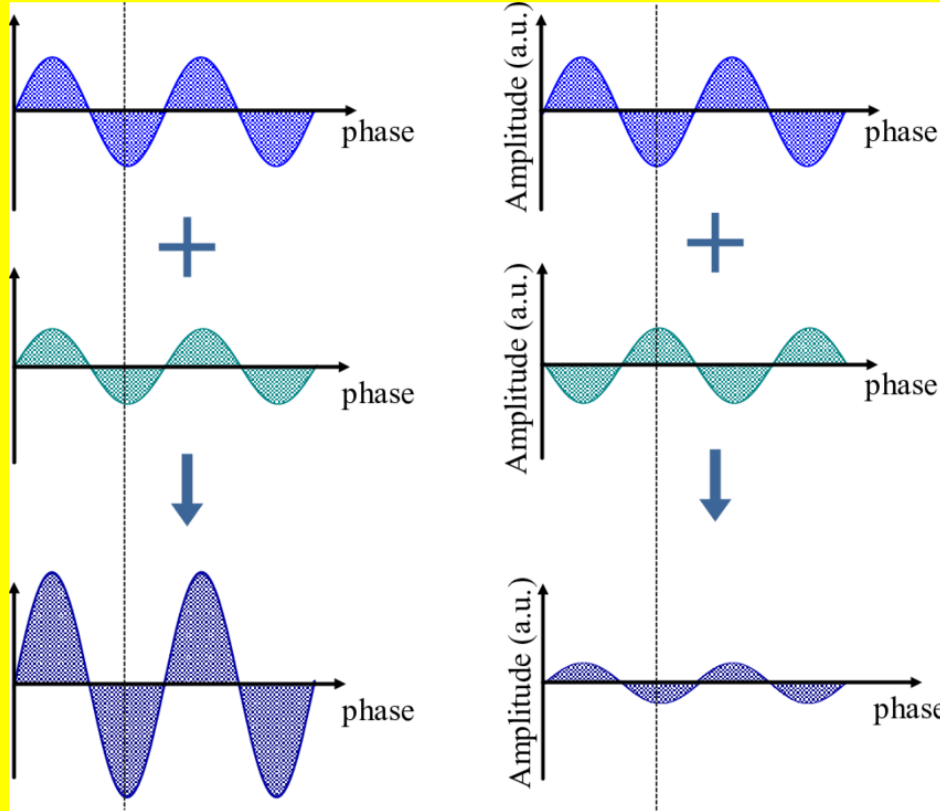
GW!



Credit: S. Kelley/NIST

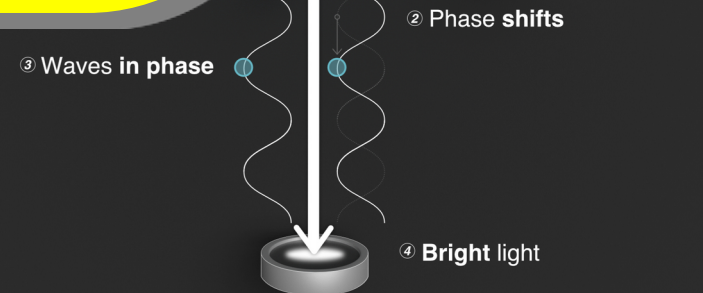
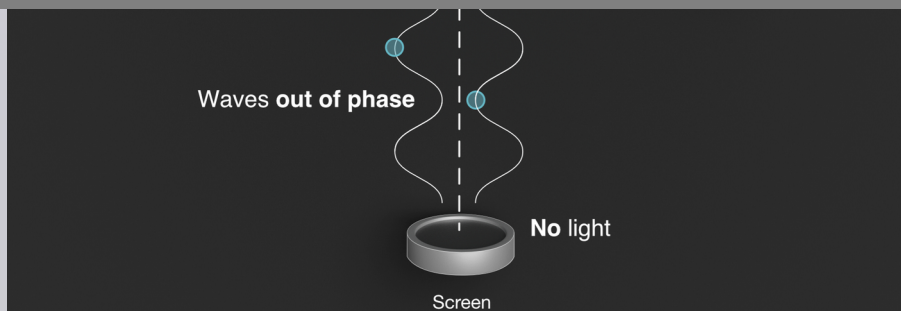
Interference

(of the *light* from the laser, not the GW signal!!)



can be directly
measured GW-signal
and m_2 , a strong signal
resolution is needed

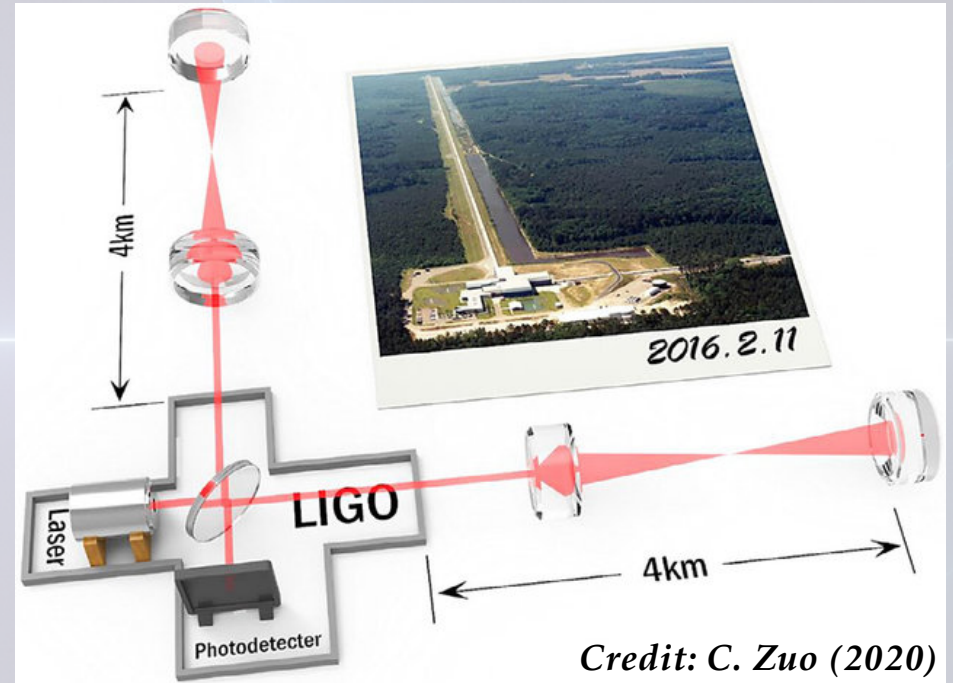
GW!



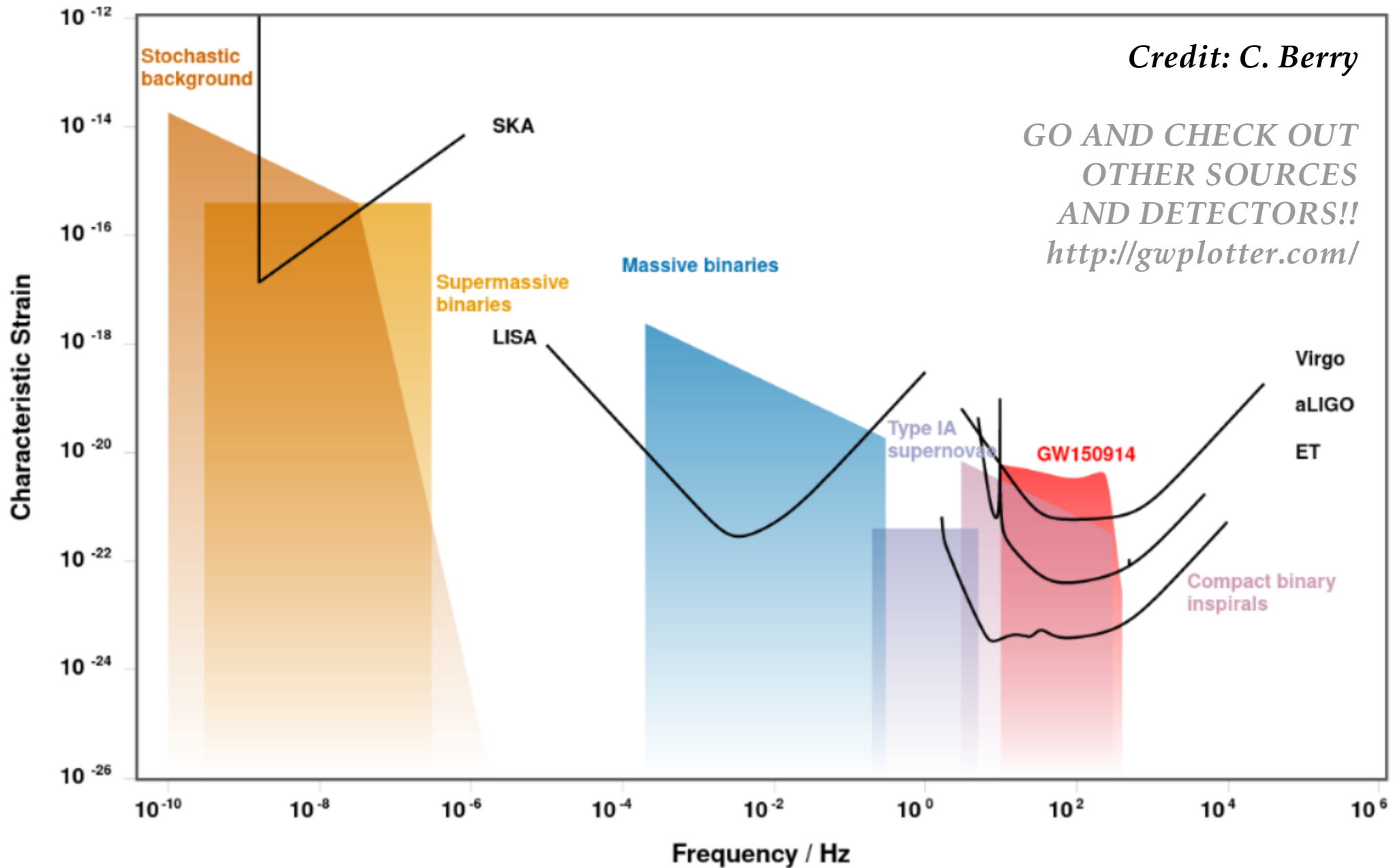
Credit: S. Kelley/NIST

And some names you MUST know

- LIGO:
 - Laser Interferometer Gravitational-wave Observatory (USA)
- **aLIGO**
 - advanced LIGO
 - the current version
- **Virgo**
 - LIGO's important little sister in Europe

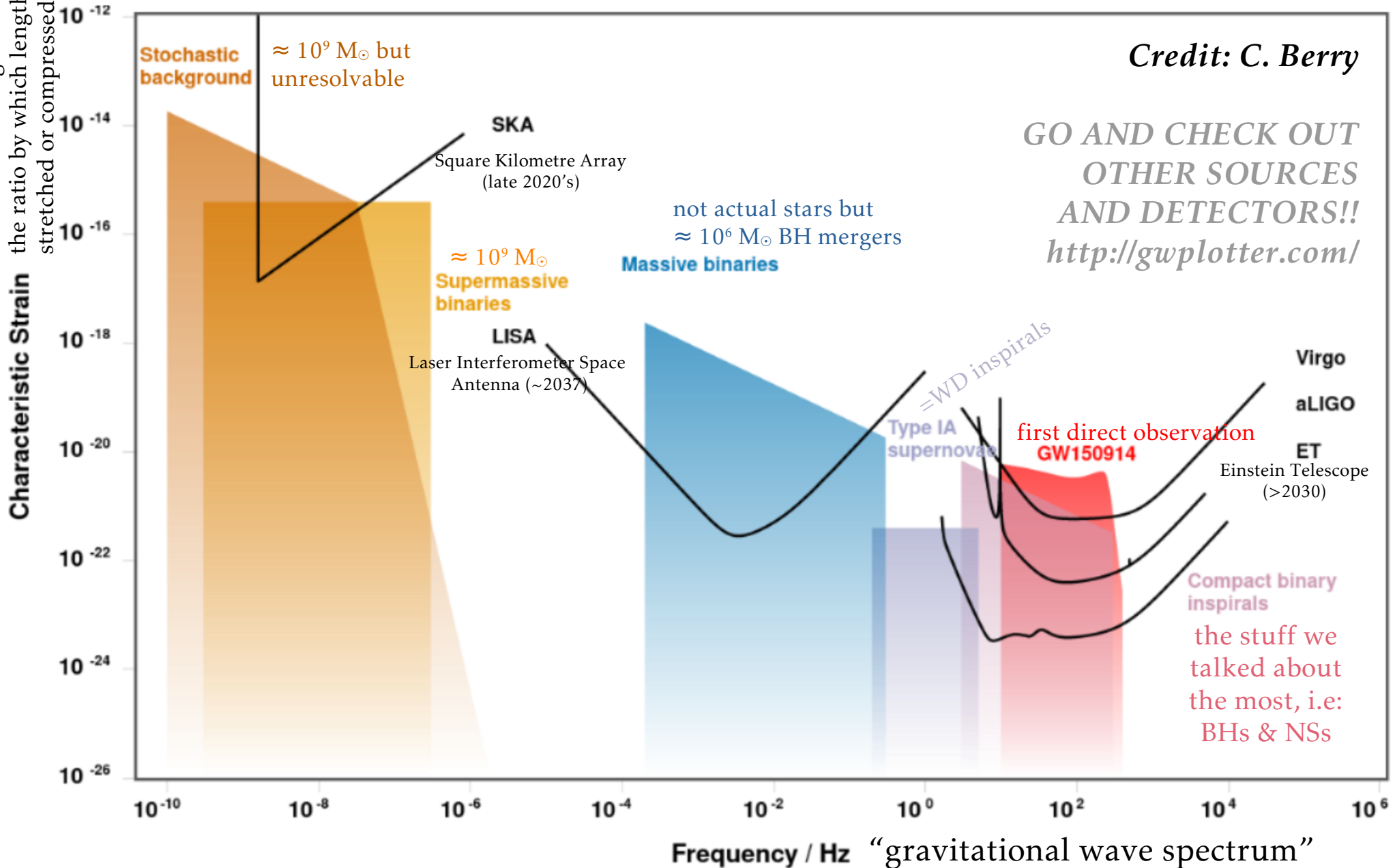


Detector sensibility



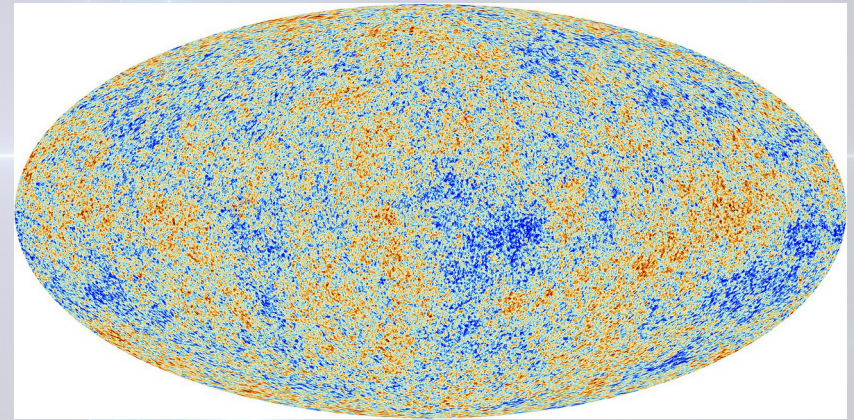
Detector sensibility

a measure of the grav. wave's effect:
the ratio by which lengths are
stretched or compressed (dimensionless)



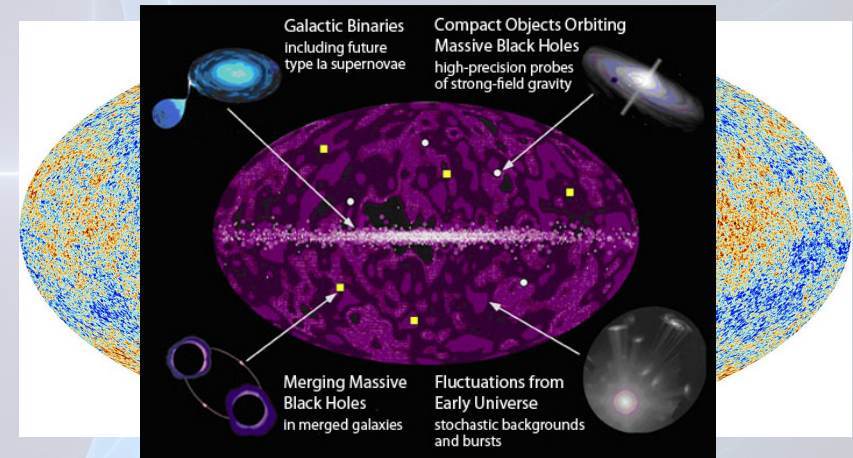
Cosmic grav.wave background

- Heard about the cosmic microwave background?



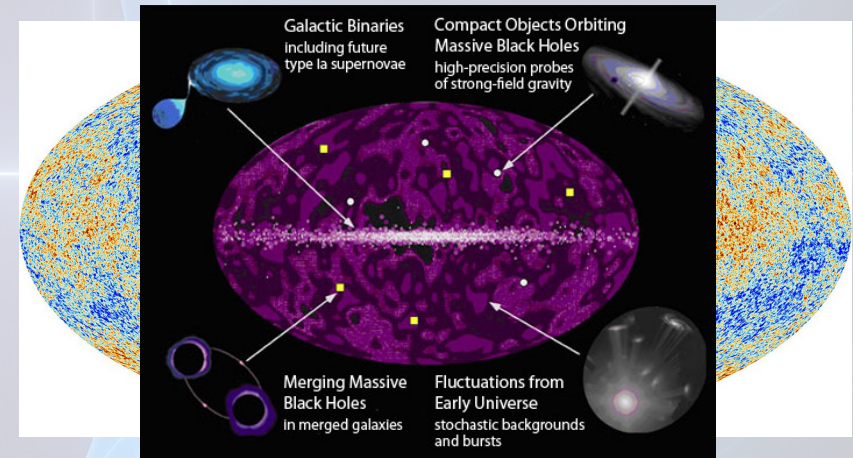
Cosmic grav.wave background

- Heard about the cosmic microwave background?
- GW-background:
 - undetected (yet)



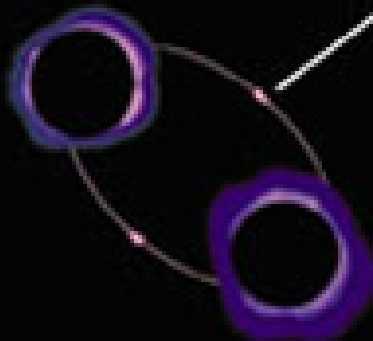
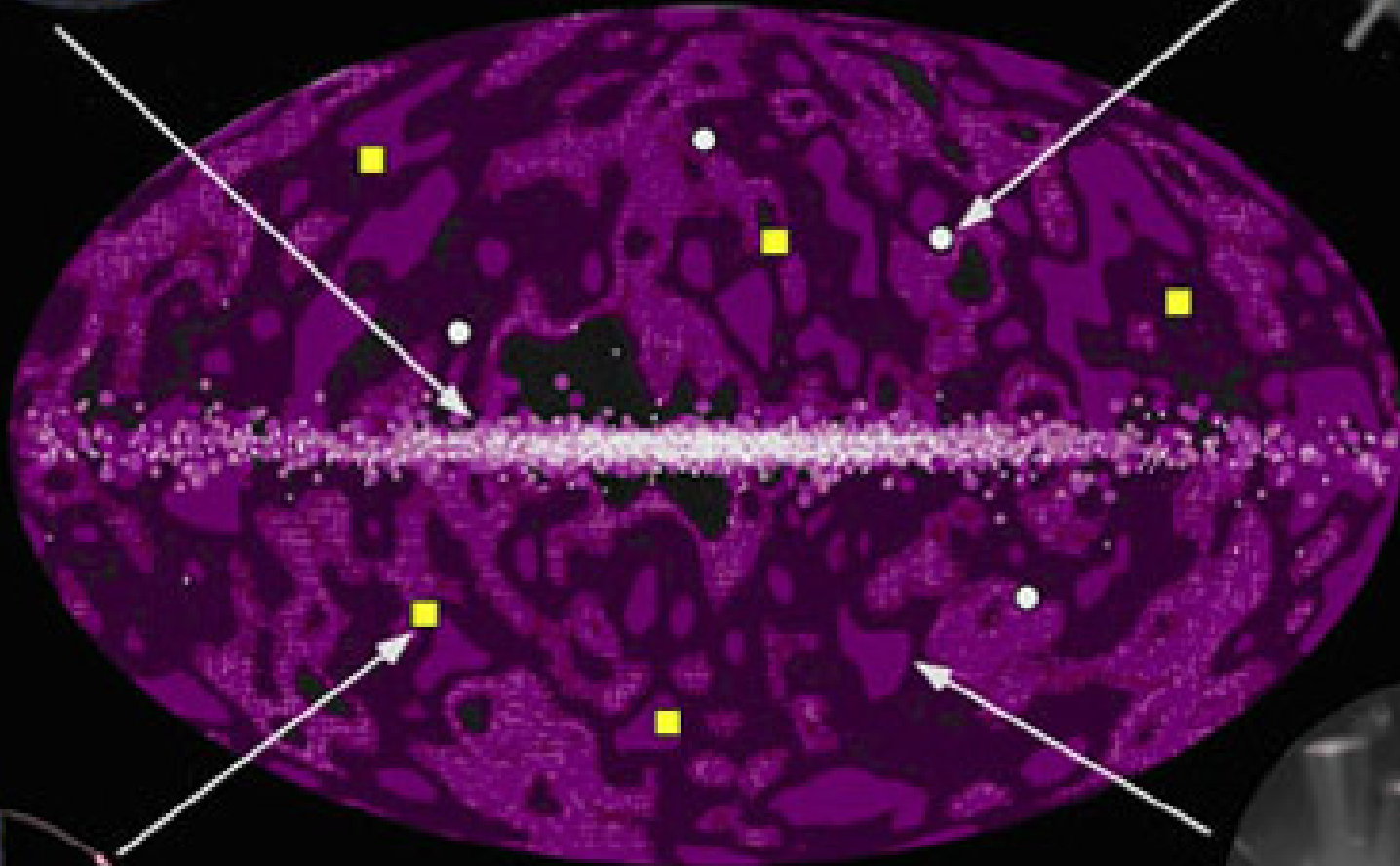
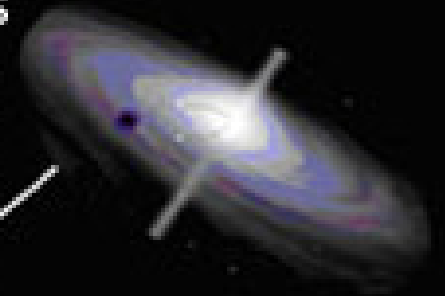
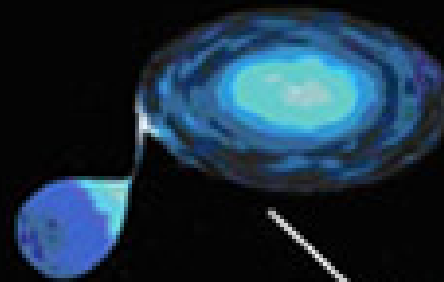
Cosmic grav.wave background

- Heard about the cosmic microwave background?
- GW-background:
 - undetected (yet)
 - cosmological sources
 - processes during e.g. the cosmic inflation (10^{-36} – 10^{-33} sec after the Big Bang)
 - astrophysical sources
 - large number of *unresolvable* BH-BH (or BH-NS, or NS-NS) mergers; additional WD-WD mergers, supernova explosions...



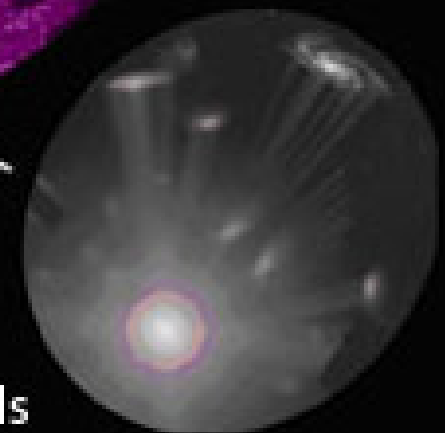
Galactic Binaries
including future
type Ia supernovae

Compact Objects Orbiting
Massive Black Holes
high-precision probes
of strong-field gravity



Merging Massive
Black Holes
in merged galaxies

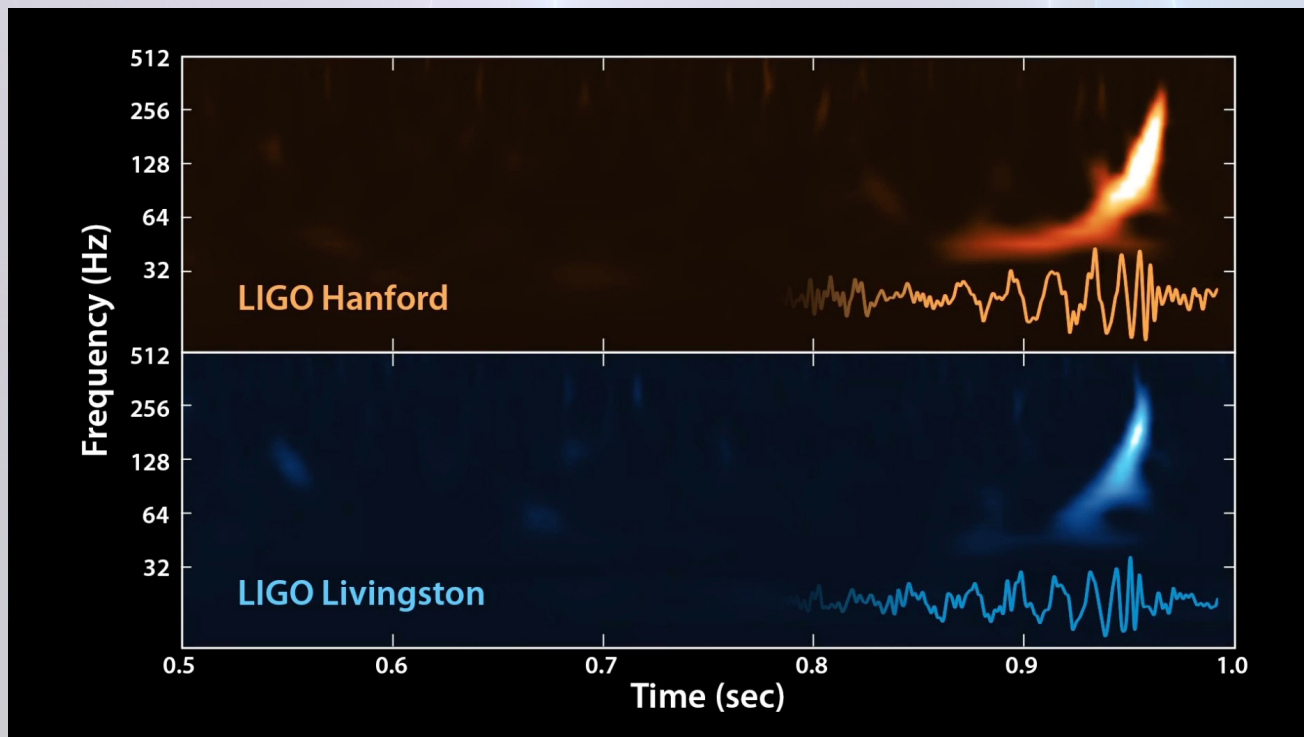
Fluctuations from
Early Universe
stochastic backgrounds
and bursts



Credit: NASA/ESA

The whispering of the Universe

<https://www.youtube.com/watch?v=2PzbYK1x3Vo>



'GW150914'

$35 M_{\odot}$ & $30 M_{\odot}$

(BH+BH)

=

$64 M_{\odot}$

*$3 M_{\odot}$ converted
into GWs!*