

Gravitational-wave progenitors

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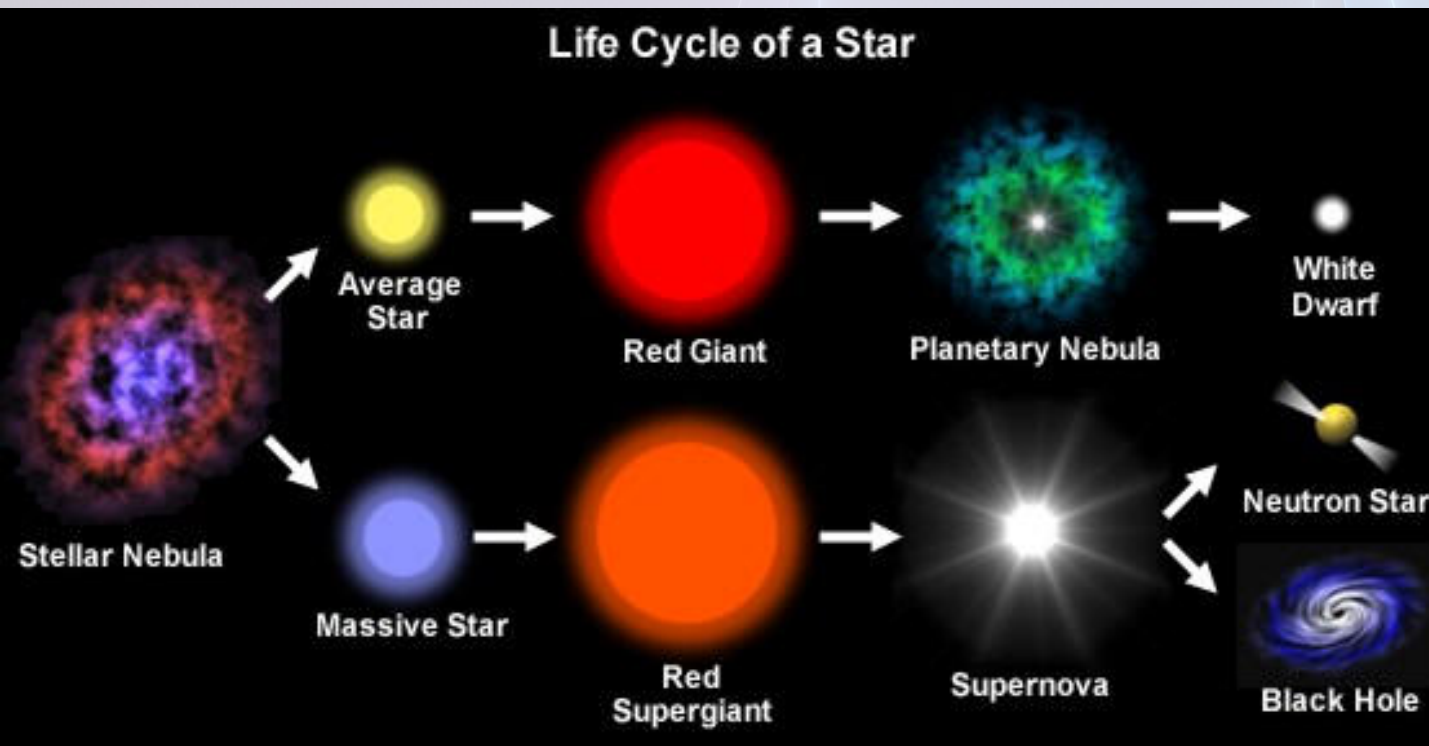
Lecture #14

NCU, Summer Semester 2022

The background features a large, faint, light-colored circle centered in the upper half. Overlaid on this are several glowing, ethereal lines in shades of blue, cyan, and magenta. These lines form a complex, web-like pattern that resembles a fractal or a network of connections. The lines are semi-transparent and have a soft, glowing effect, creating a sense of depth and movement. The overall aesthetic is clean, modern, and futuristic.

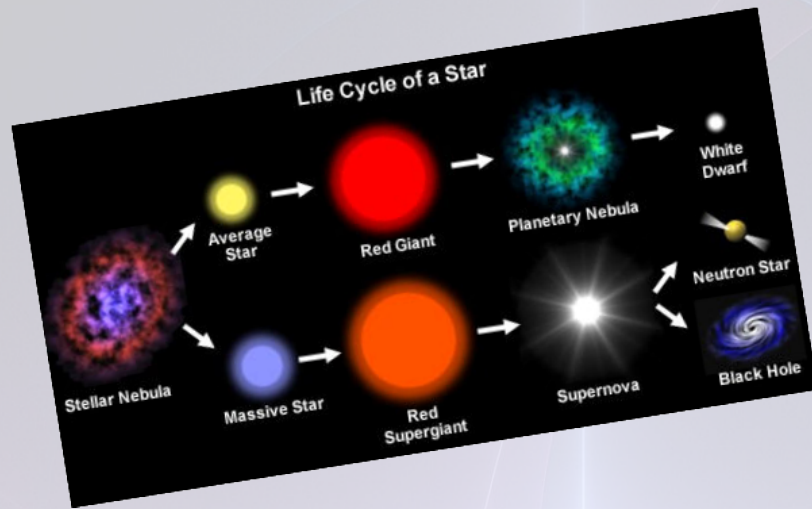
*Previously
on GW-progenitors...*

Stars evolve → stellar evolution



low-mass: $< 8 M_{\odot}$

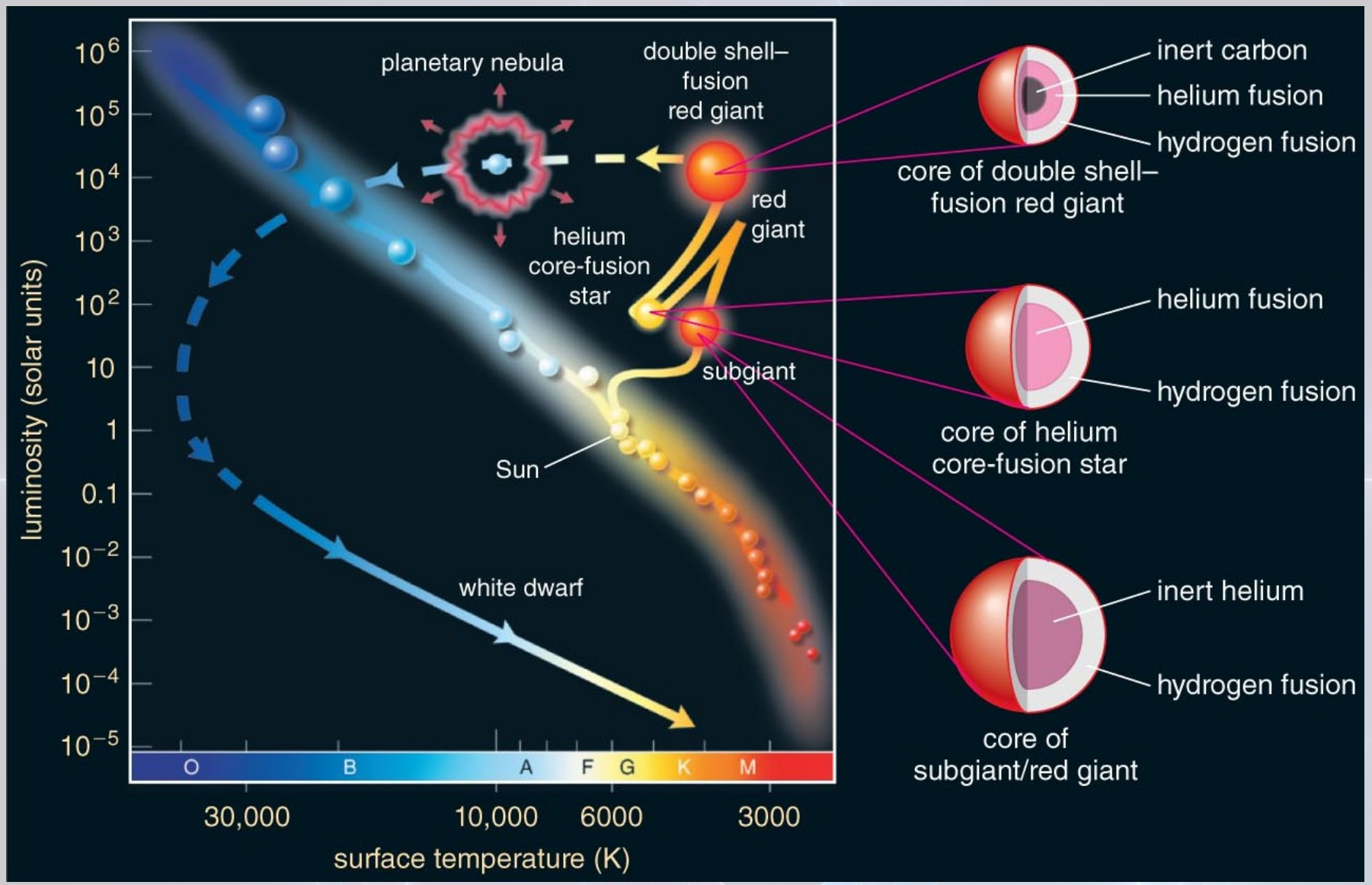
massive: $> 8 M_{\odot}$



How to do it more scientifically?

The HRD

Hertzsprung–Russell diagram



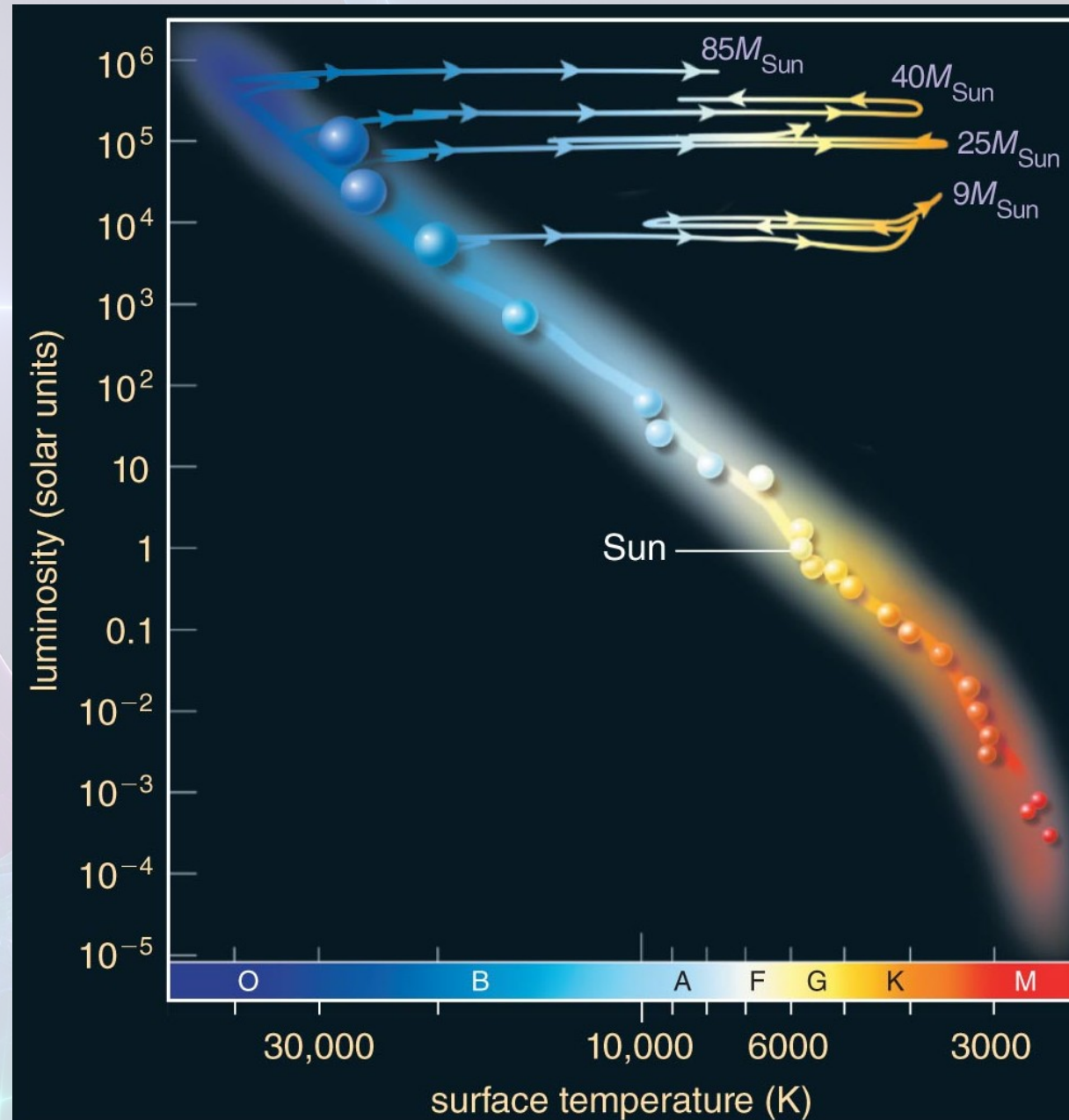
Credit: https://jila.colorado.edu/~ajsh/courses/astr1200_18/starevol.html

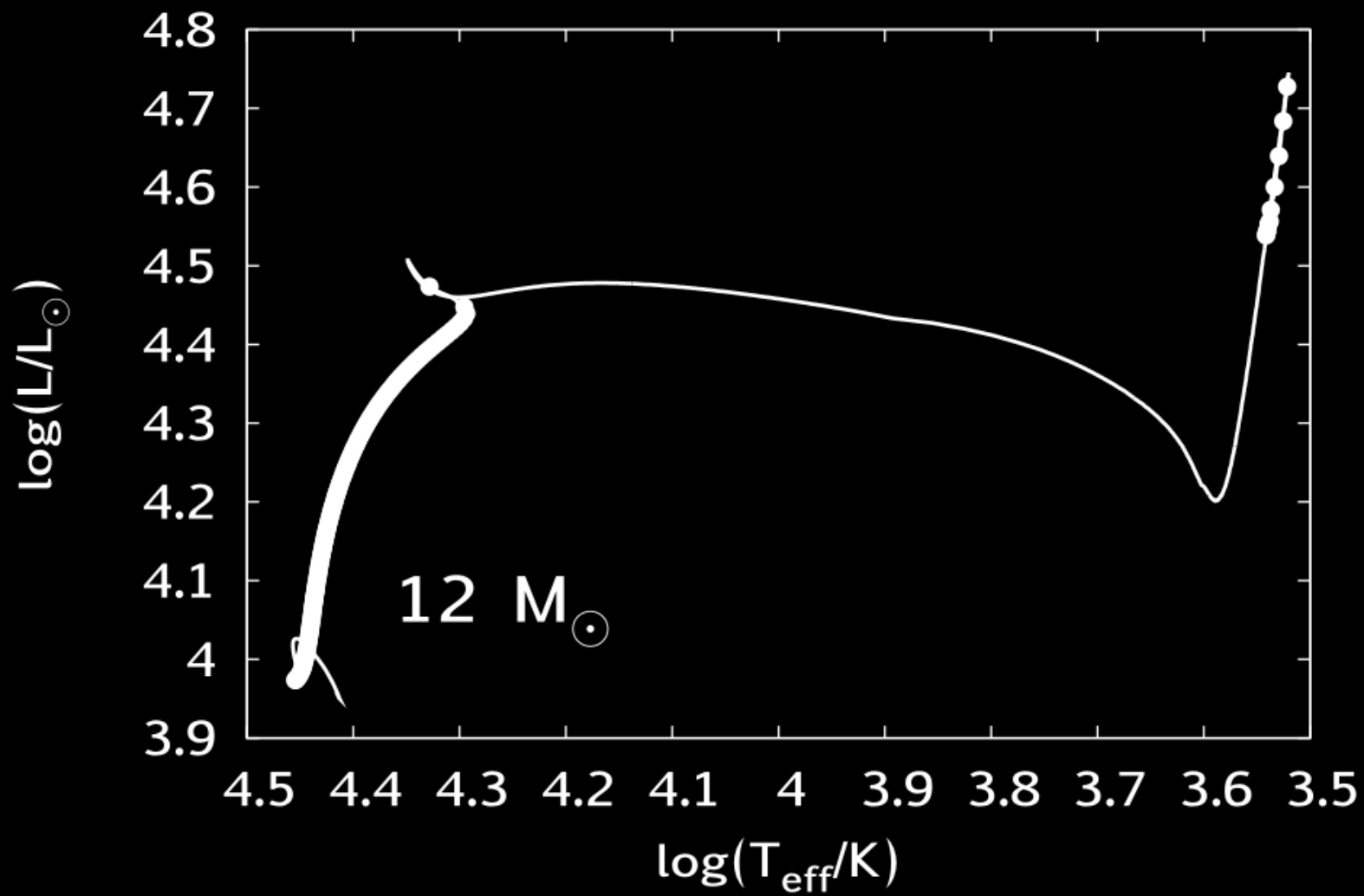
The HRD

Hertzsprung-Russell diagram

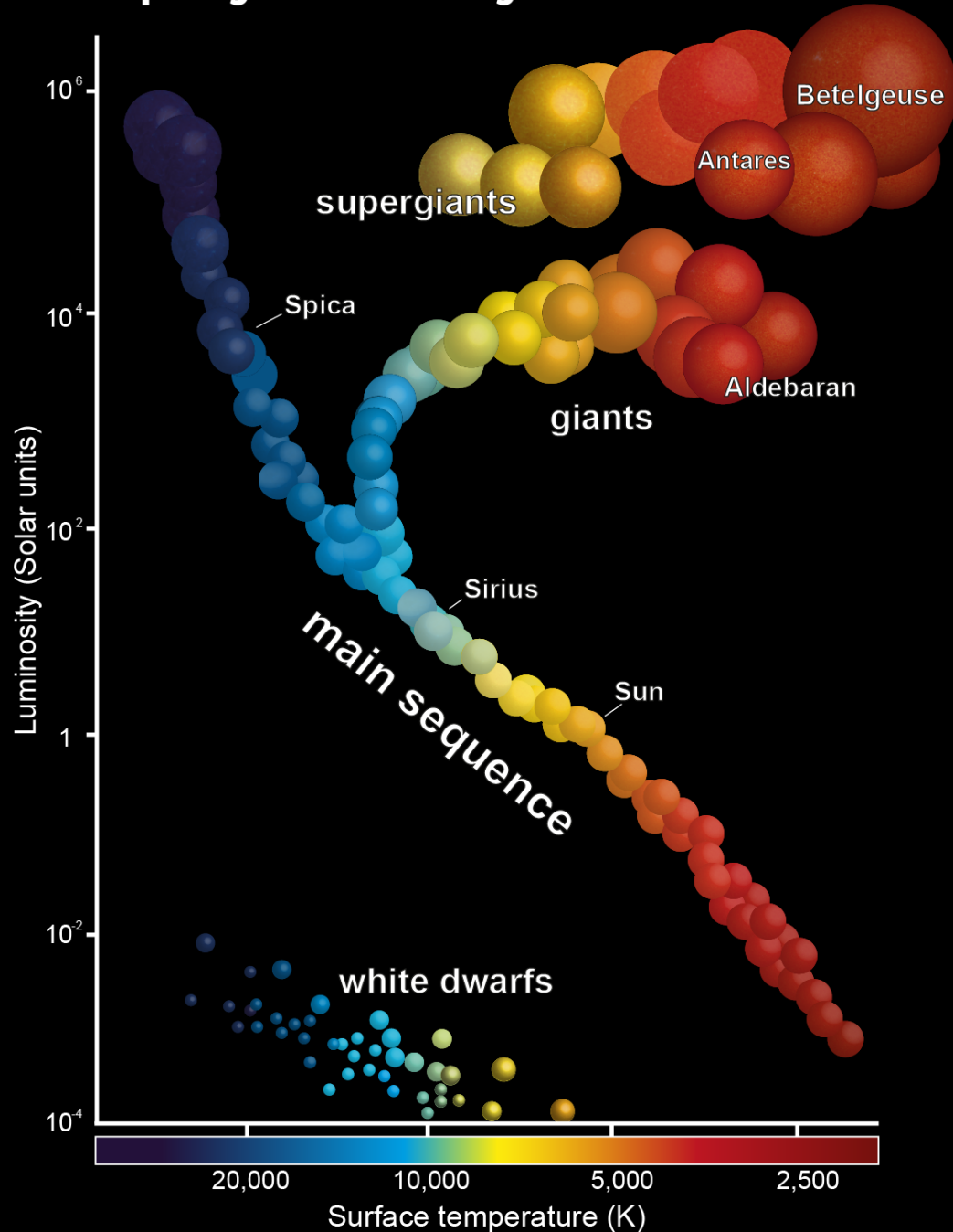
Further advantages of the HRD

- allows comparison of an observed *star* and its corresponding *stellar evolutionary model*
- allows comparison of low-mass stars vs. massive stars





Hertzsprung–Russell Diagram



of the HRD

radius can be easily read out

– equiradial lines due to Stephan-Boltzmann law

color of the star can be easily read out

(~surface temp.)

brightness: ~luminosity

What is a star?

→ surface?
→ photons escape
"photosphere"

hot, dense plasma

What is inside?



theoretical
modelling
of the stellar
structure

equilibrium:

pressure gradient

gravity



Theoretical modelling of the stellar structure

$$\frac{\partial r}{\partial m_r} = \frac{1}{4\pi r^2 \rho} \quad \text{equation of mass conservation} \quad (1)$$

$$\frac{\partial P}{\partial m_r} = -\frac{Gm_r}{4\pi r^4} \quad \text{equation of momentum conservation} \quad (2)$$

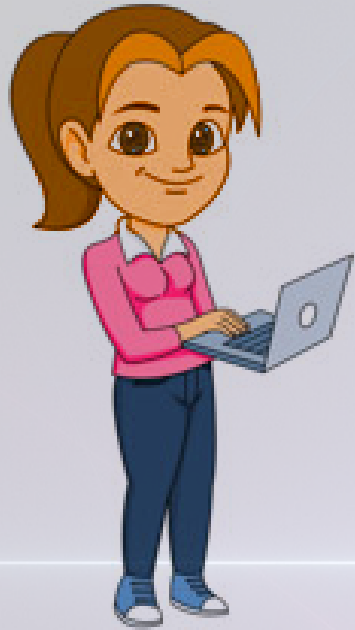
$$\frac{\partial L_r}{\partial m_r} = \epsilon_{\text{pl}} - T \frac{\partial S}{\partial t} \quad \text{equation of energy conservation} \quad (3)$$

$$\frac{\partial T}{\partial m_r} = -\frac{Gm_r T}{4\pi r^4 P} \nabla \quad \text{equation of transport of energy} \quad (4)$$

Guilera+ 11

composition change due to nuclear burning:

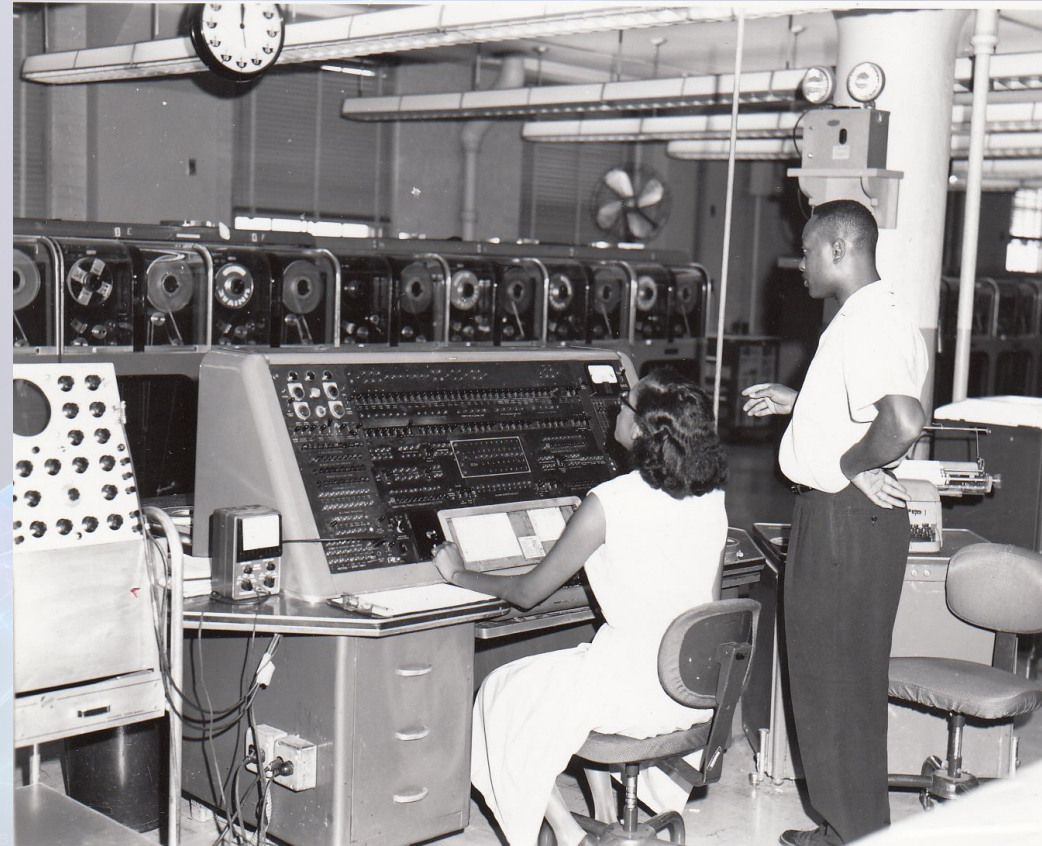
$$\frac{\partial X_i}{\partial t} = \frac{A_i m_u}{\rho} (-\Sigma_{j,k} r_{i,j,k} + \Sigma_{k,l} r_{k,l,i}) \quad (5)$$



Where to start:

<https://docs.mesastar.org/en/latest/index.html>

https://cococubed.com/mesa_market/education.html

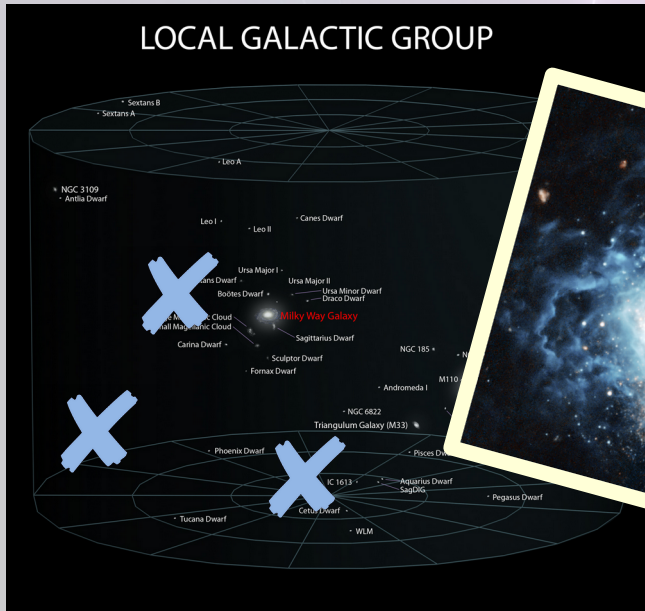


Where can we find stars*

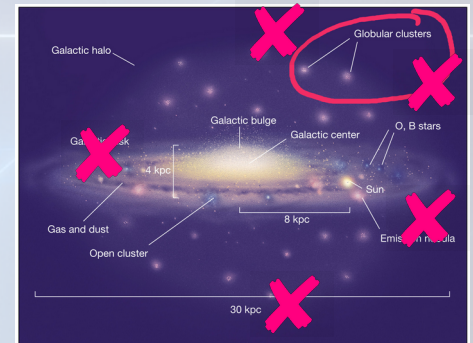
*gas/galaxies/anything: "environments"

with sub-Solar Z?

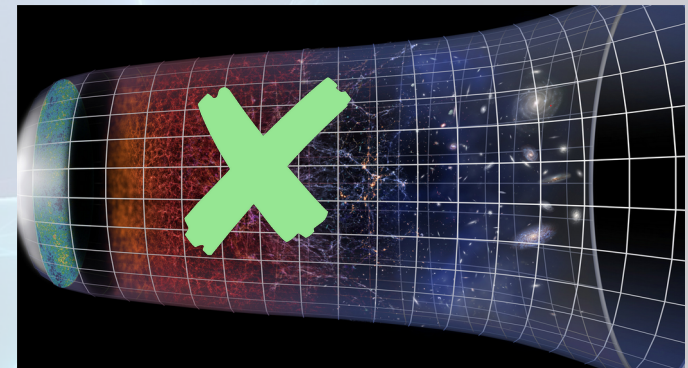
Dwarf galaxies



Globular clusters



Early Universe



The winds of *massive* stars are...
strong.



$$10^{-7} - 10^{-3} M_{\odot}/\text{yr}$$



loss of 10-70% of
material over
lifetime...

(Sun: $\sim 10^{-14} M_{\odot}/\text{yr}$)

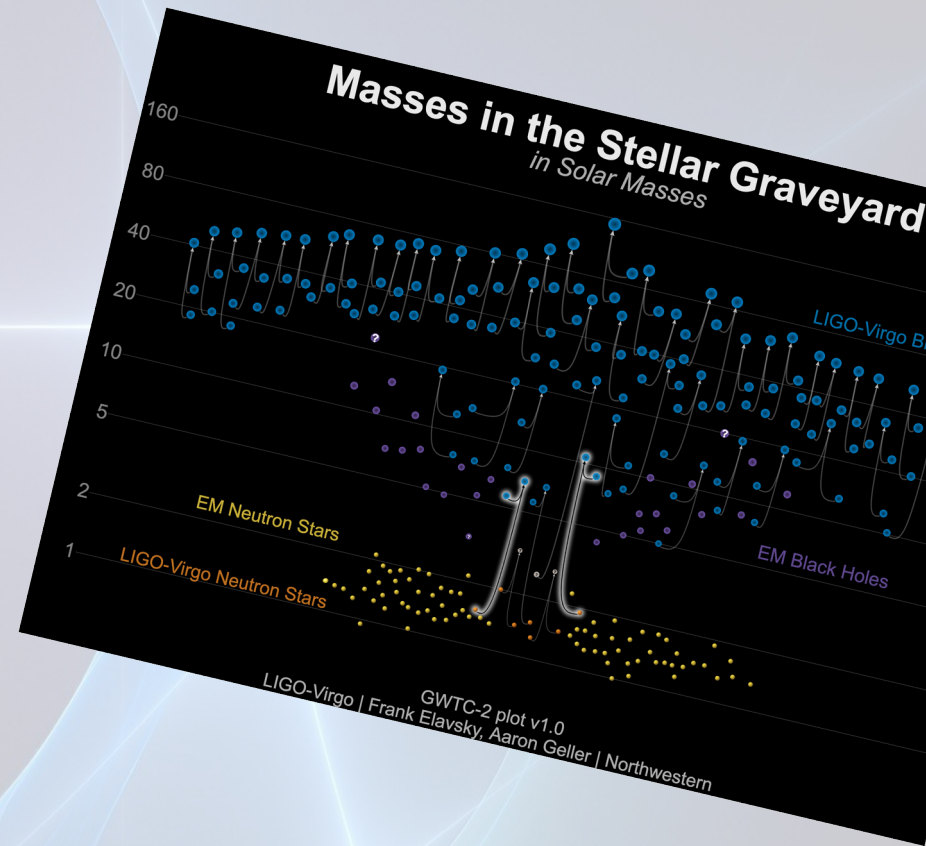
Wolf-Rayet star WR 124 with its surrounding nebula known as M1-67.
The nebula came *from the star!*

To form a $60 M_{\odot}$ black hole...

- start with a very-very massive star*
*later
(IMF, mass limits...)

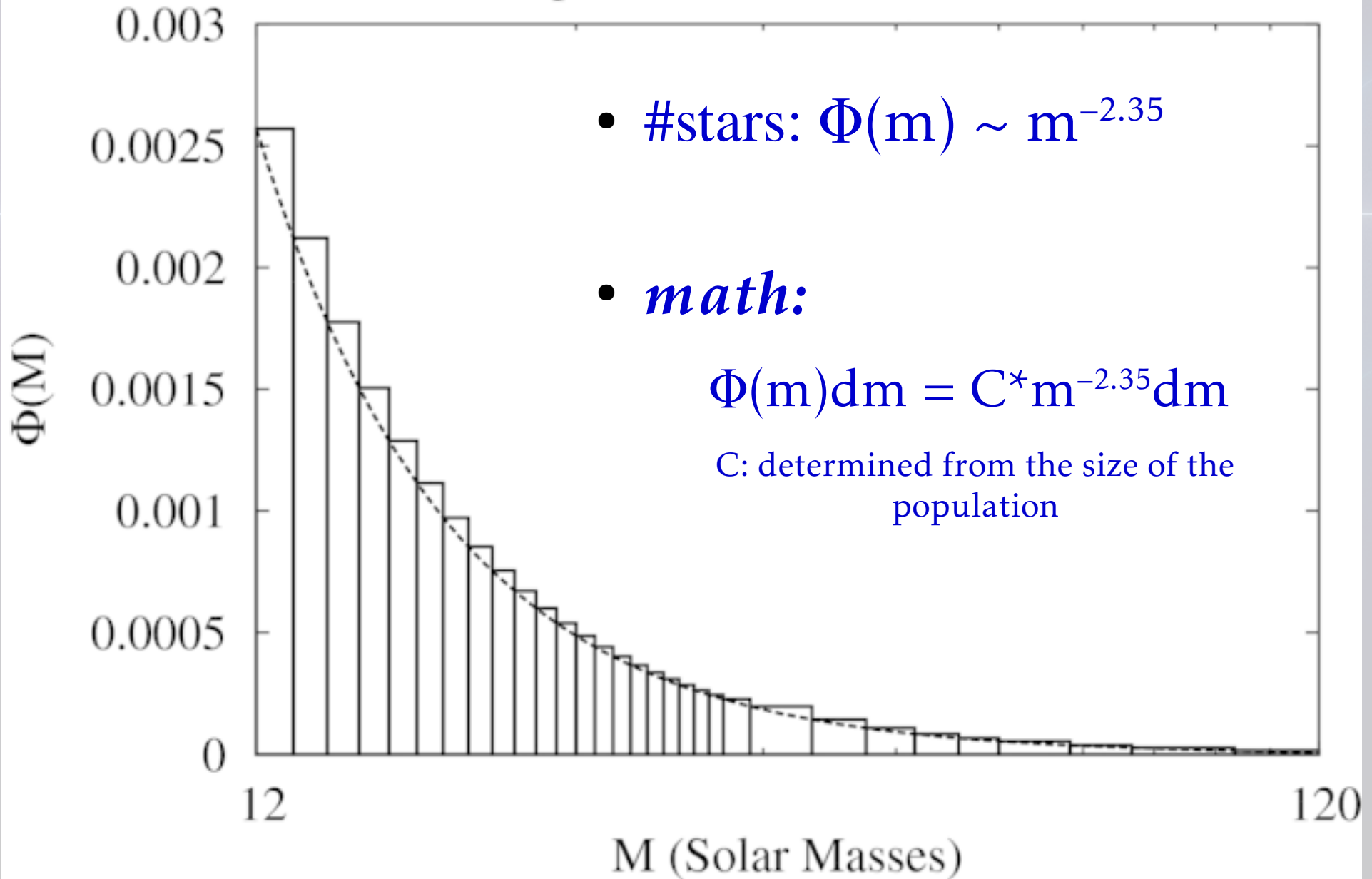
or

- decrease the strength of the wind somehow?



The Initial Mass Function (IMF)

Salpeter Initial Mass Function

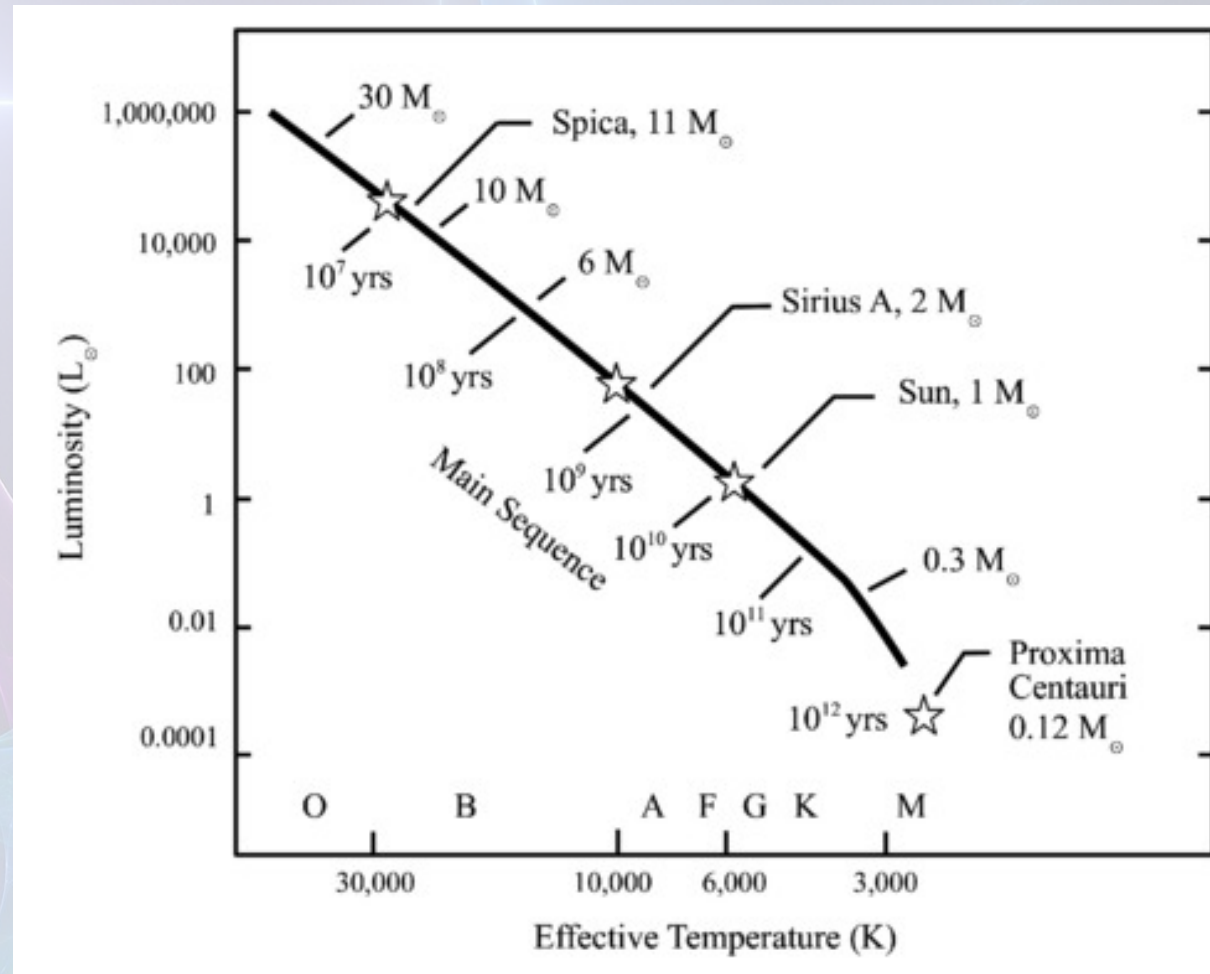


Lifetime of stars

- $\tau(m) \sim m^{-2.5}$
 - Sun's lifetime: $\sim 10^{10}$ yrs
 - an $8 M_{\odot}$ star's lifetime: $\sim 5 \times 10^7$ yrs
 - a $100 M_{\odot}$ star's lifetime: $\sim 2 \times 10^6$ yrs

Stars of higher mass are more luminous. They burn their fuel at a faster rate.

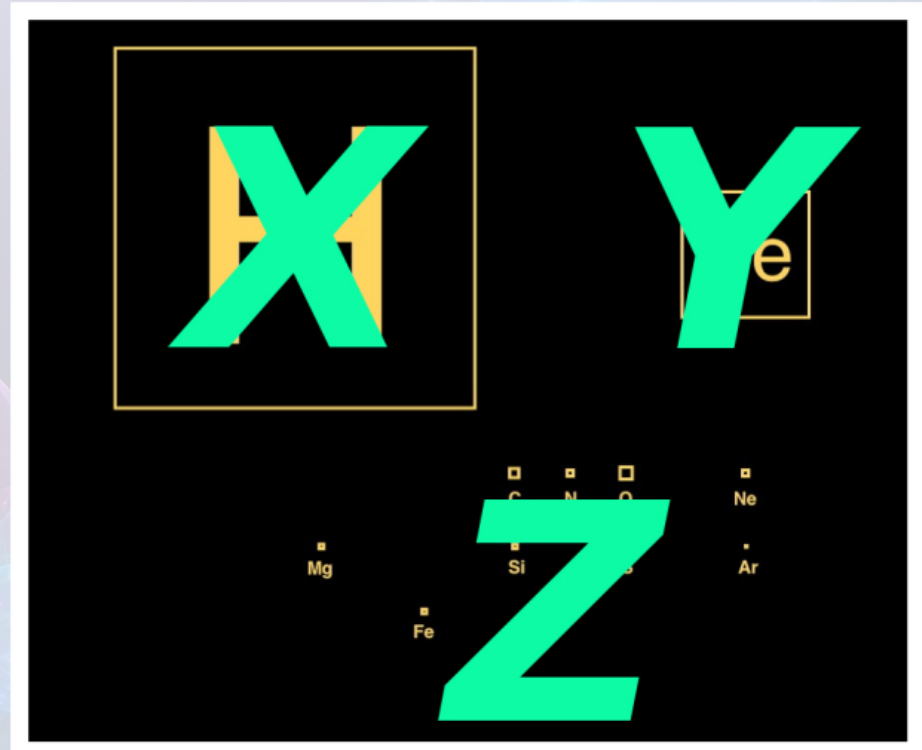
→ shorter lifetimes



Astronomers and metal

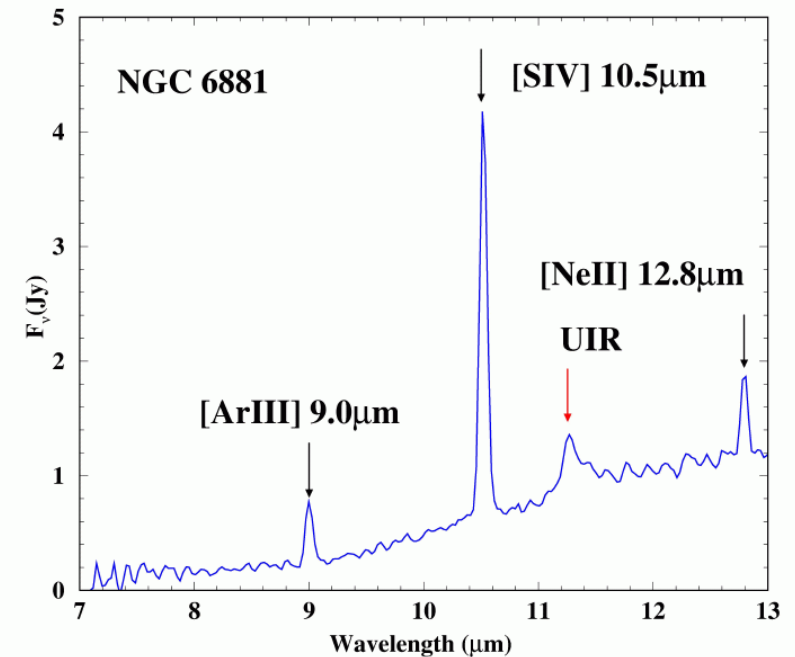
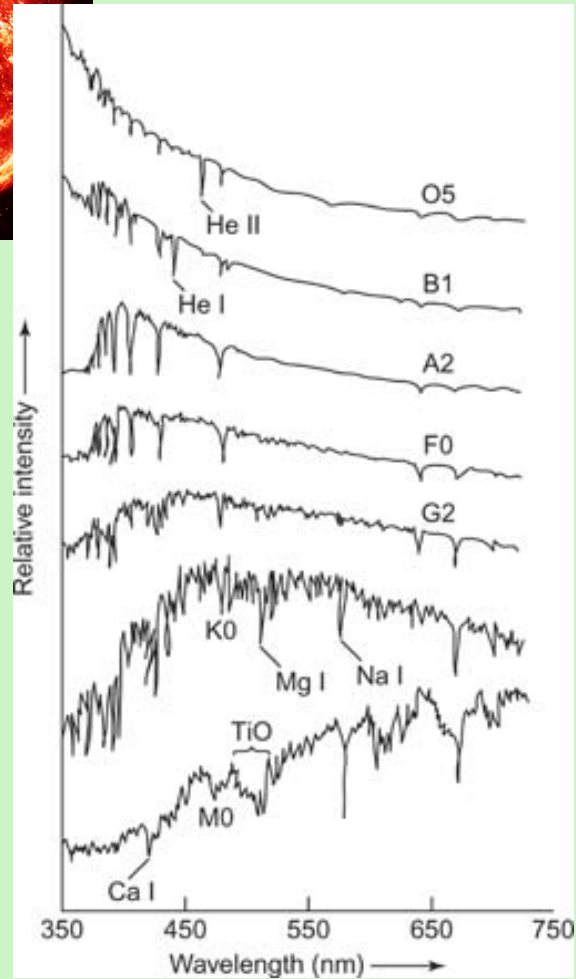
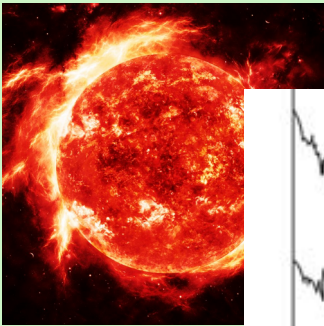
LEGEND																	
[Grey Box]		: Non-Metal															
[Yellow Box]		: Metal															
H															He		
Li	Be											B	C	N	O	F	Ne
Na	Mg											Al	Si	P	S	Cl	Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
Fr	Ra	Ac	Unq	Unp	Unh												

"Z: metallicity"

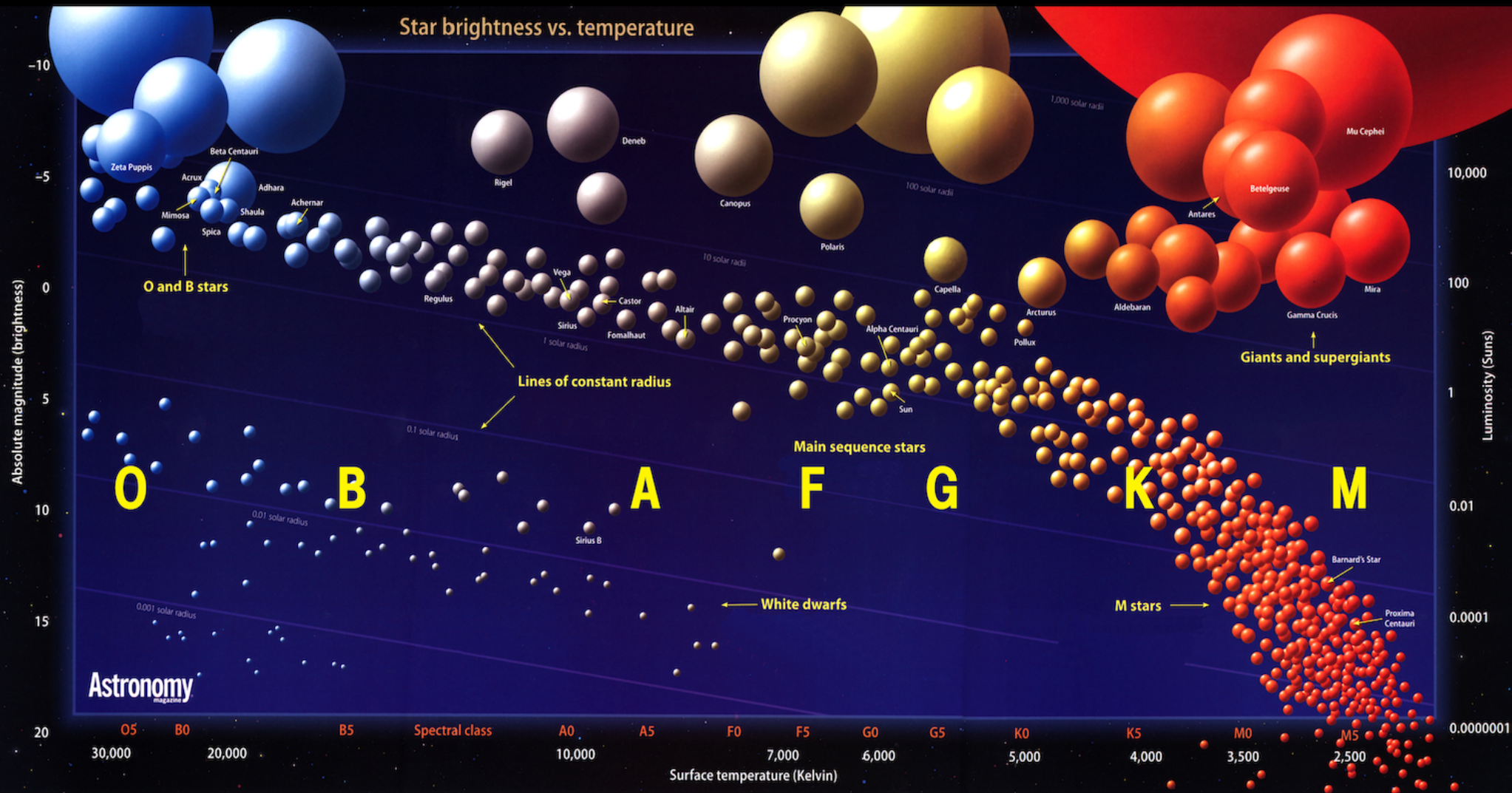


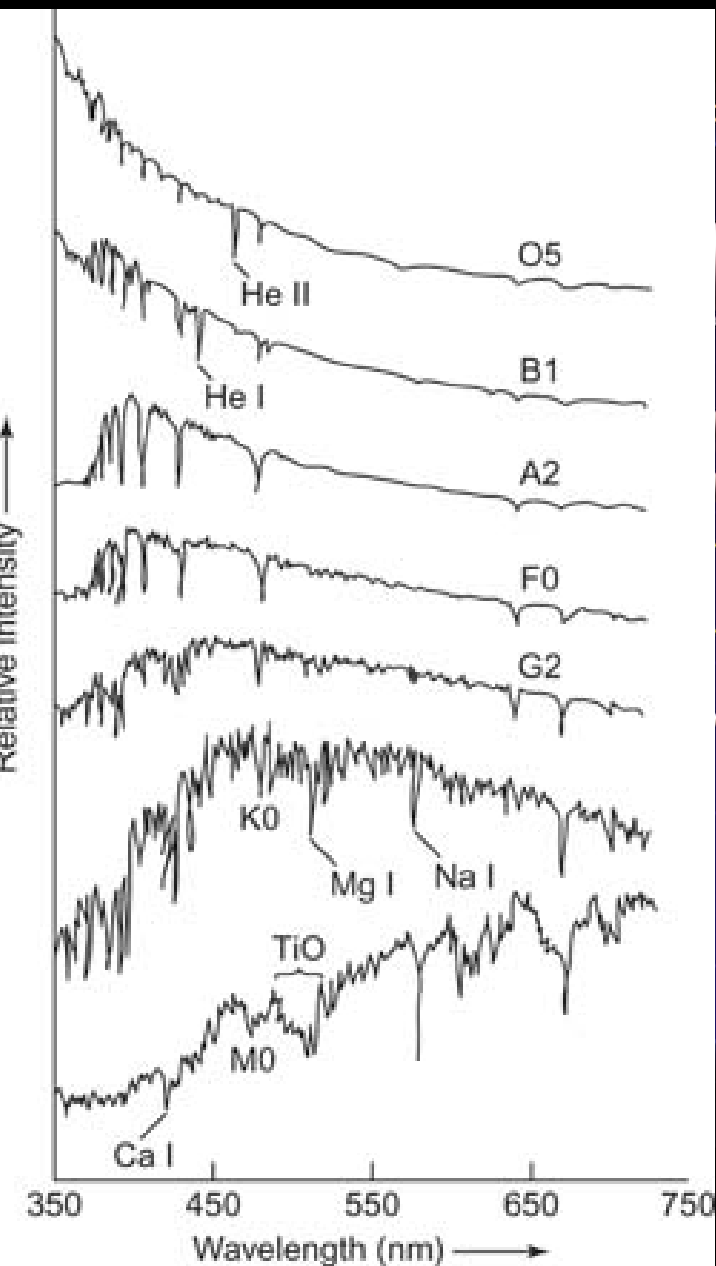
- Stellar spectra
 - absorption lines (mostly)

- Nebular spectra
 - emission lines (a light source needed for the excitation)

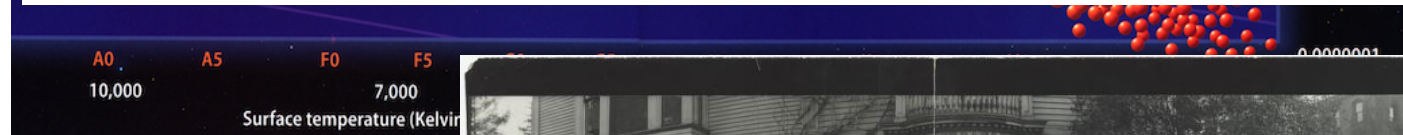
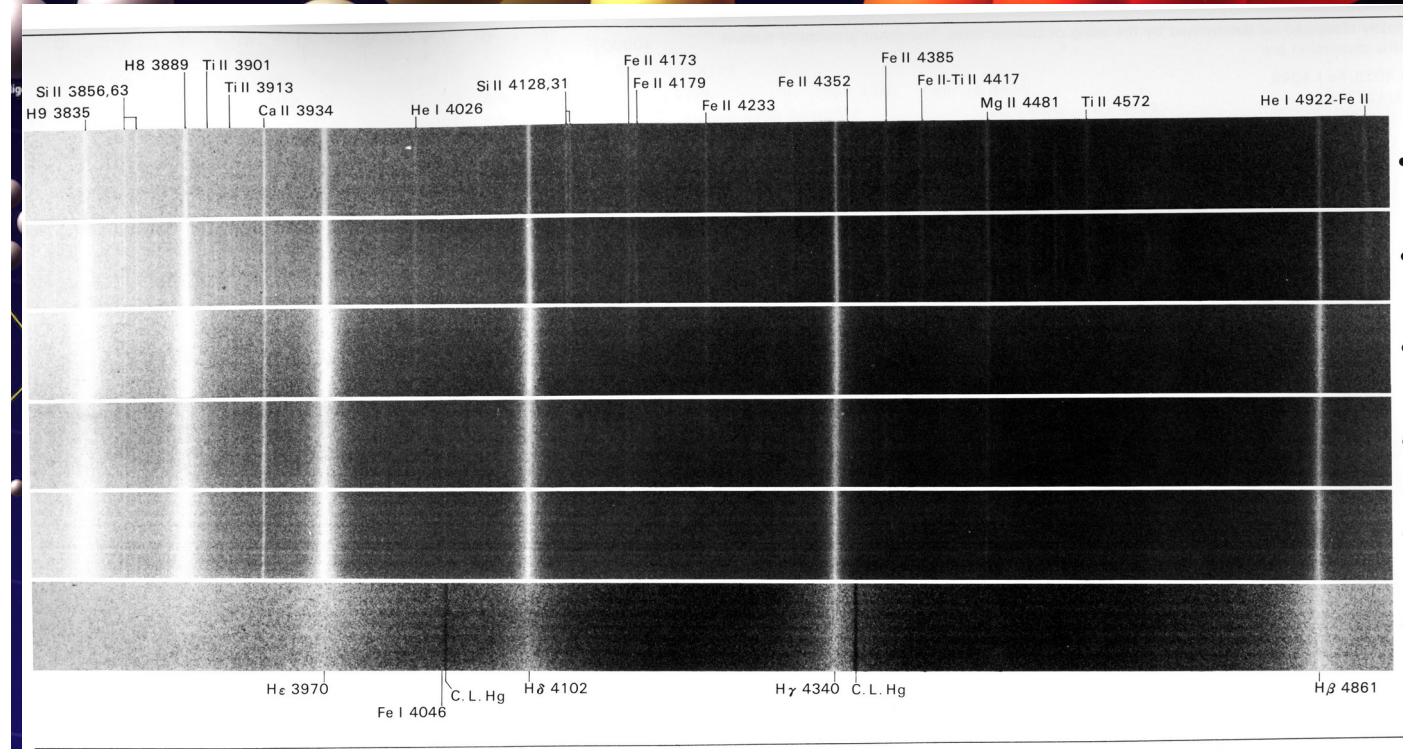


Star brightness vs. temperature





Mass vs. temperature



Planck law

$$B(\nu, T_{eff}) = \frac{2h}{c^2} \frac{\nu^3}{e^{\frac{h\nu}{k_B T_{eff}}} - 1} \quad (3)$$

*here: as a function of frequency
(works with wavelength as well)*

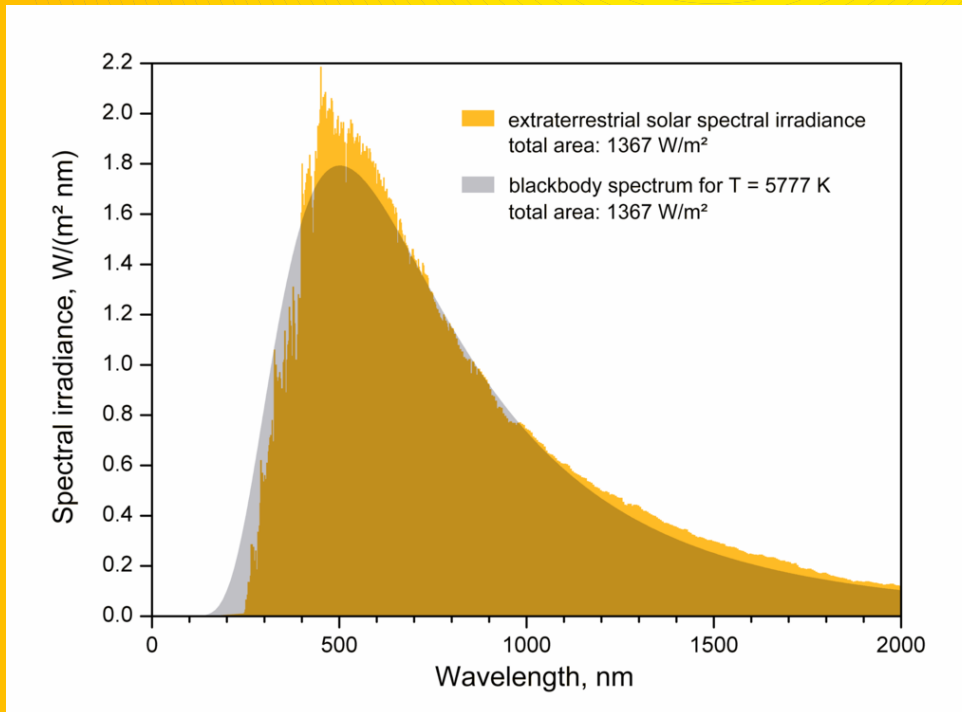
Note: there is a T value in it!

Moral of the story:

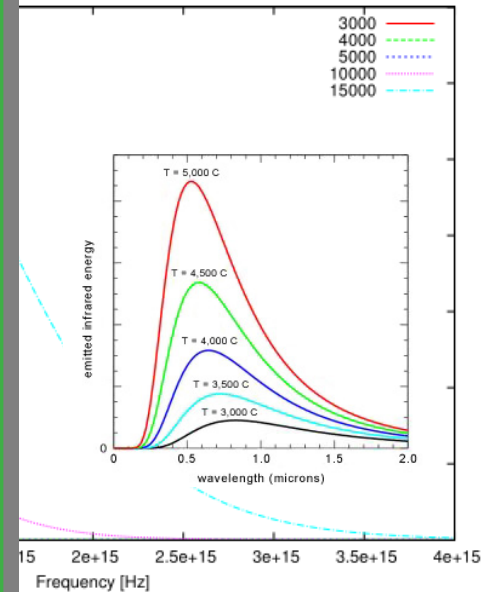
Stars are perfect Black Bodies.

(Most of the time, more or less; but basically they are.)

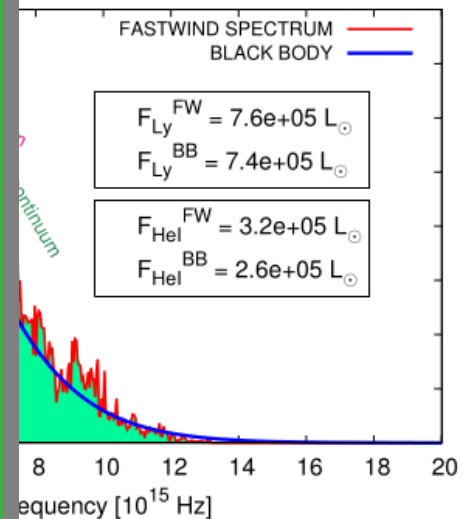
Their T_{eff} in the HRD is the T_{eff} from the Planck law.



T_{eff}

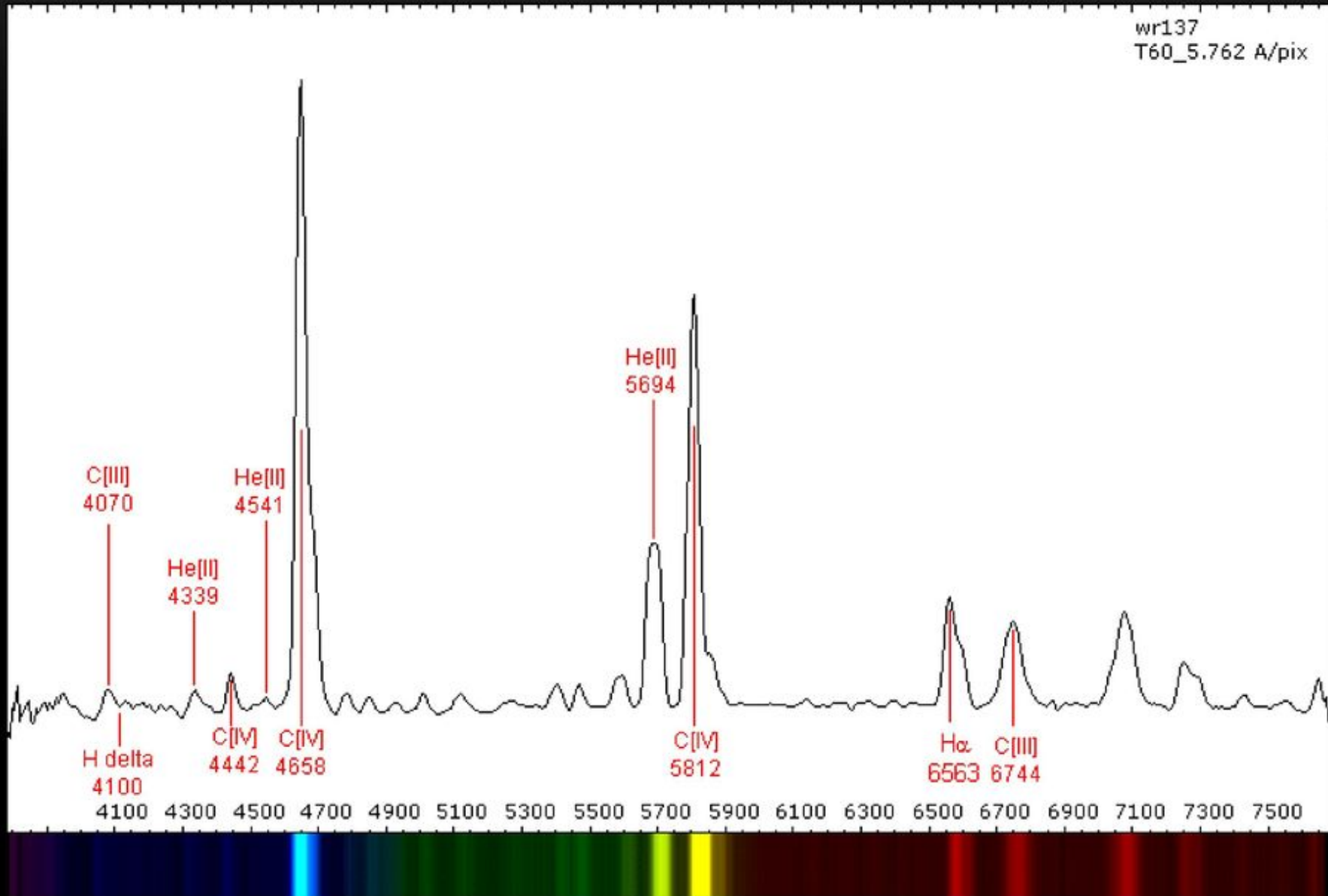


$\log L/L_{\odot} = 6.1$ $M = 80.3 M_{\odot}$

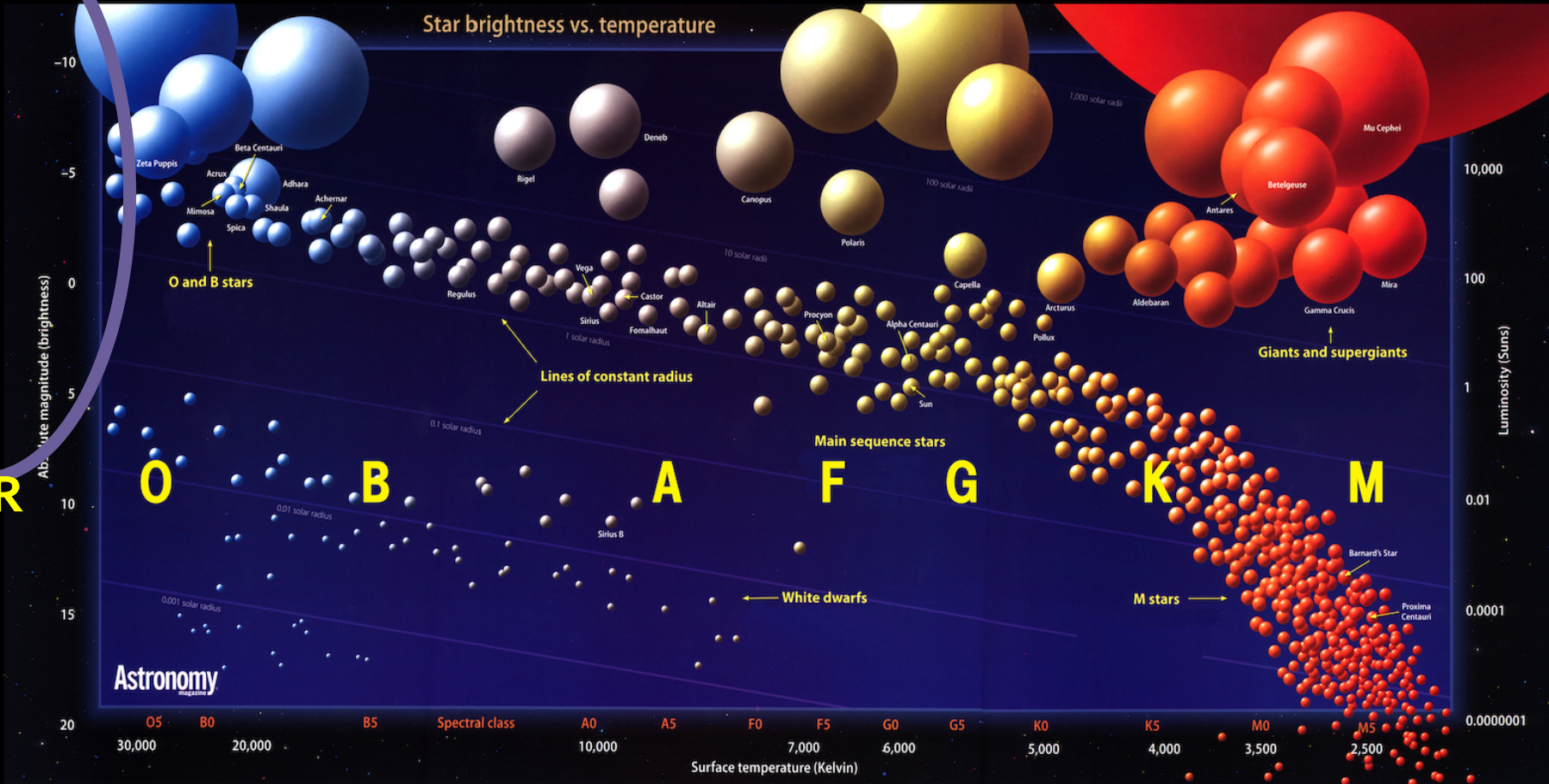


FIRST OBSERVATION

1867: Wolf & Rayet



Star brightness vs. temperature



WR

O

B

A

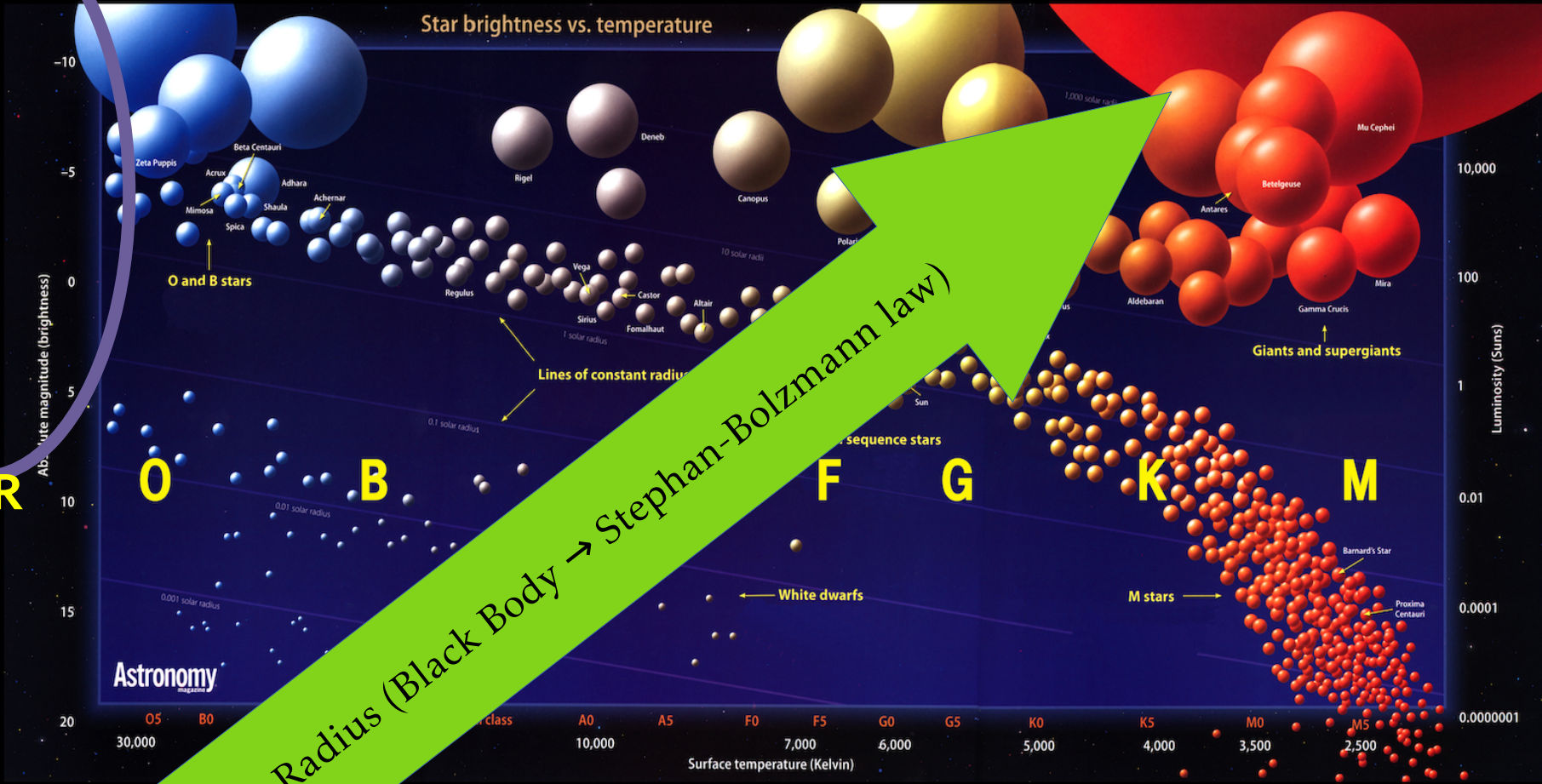
F

G

K

M

Star brightness vs. temperature



WR

Radius (Black Body → Stephan-Boltzmann law)

O

B

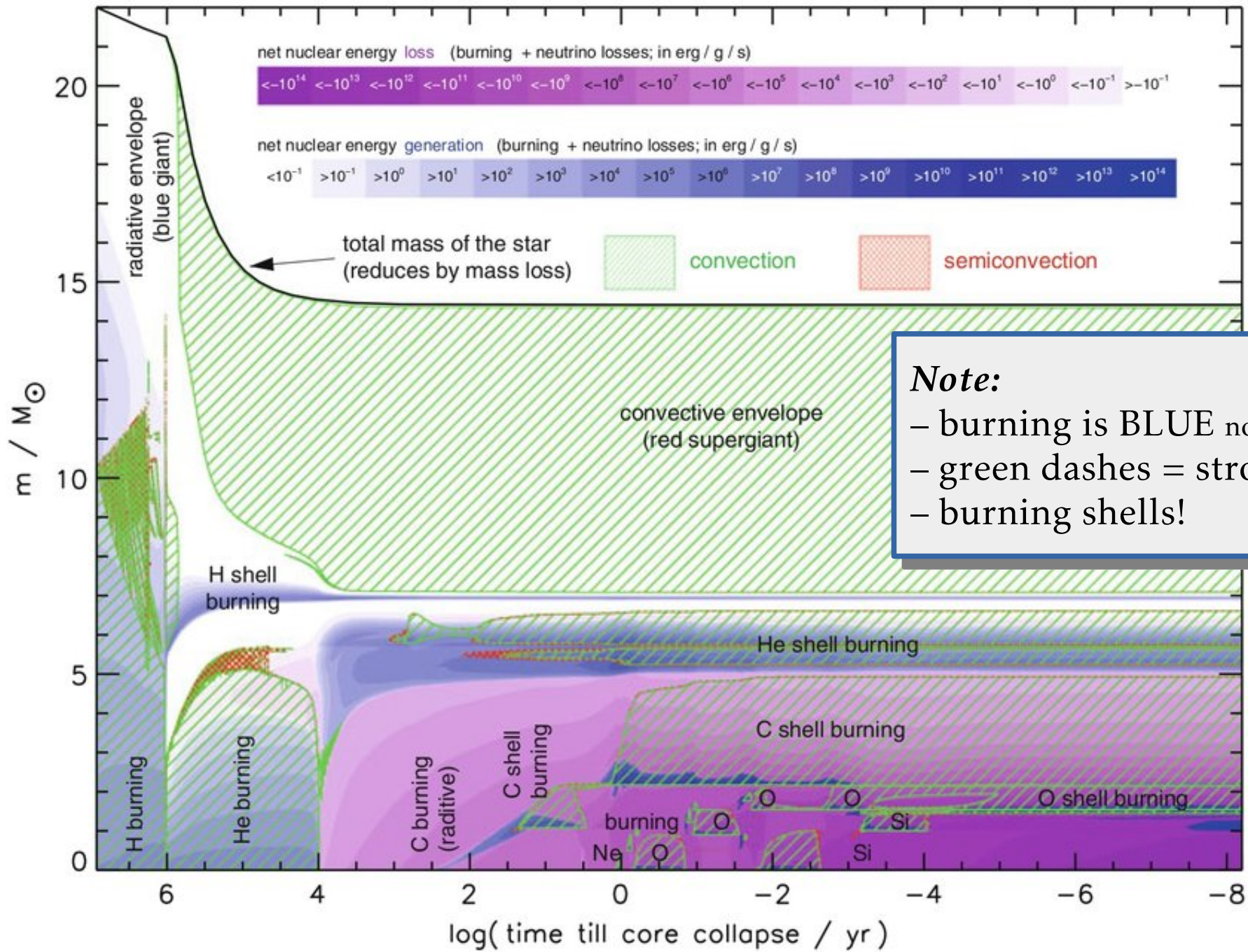
F

G

K

M

Kippenhahn diagram



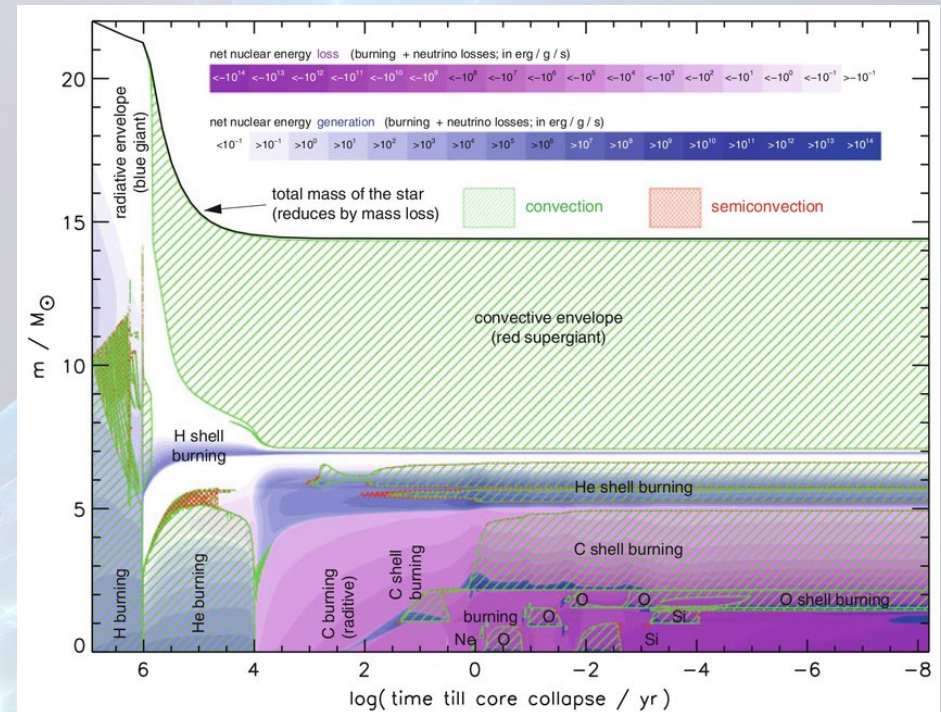
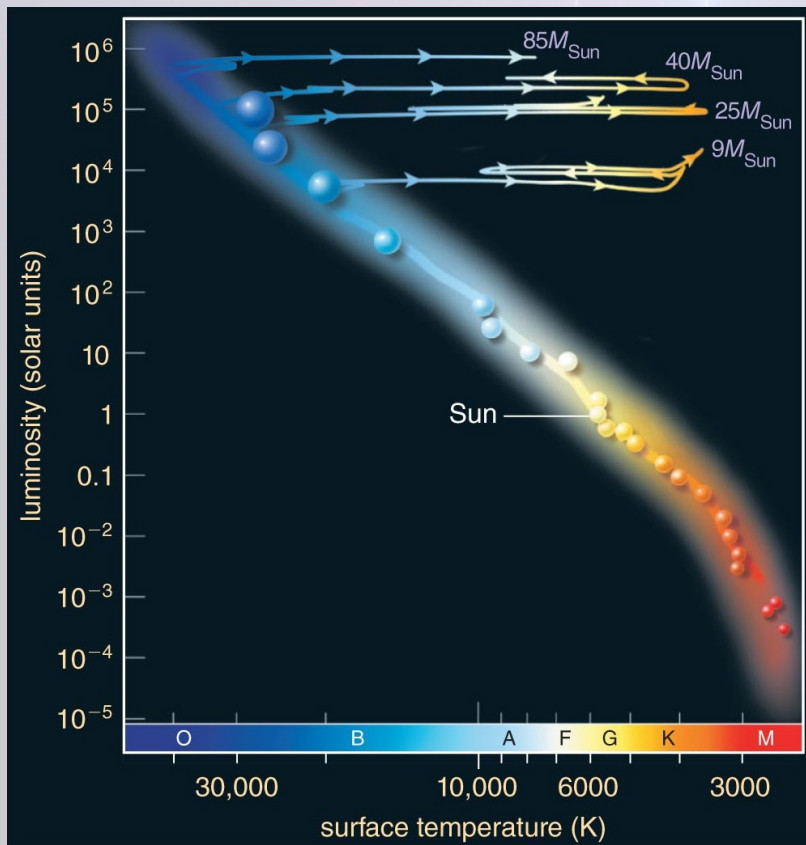
Note:

- burning is BLUE not green/purple
- green dashes = strong mixing
- burning shells!

HRD vs. Kippenhahn

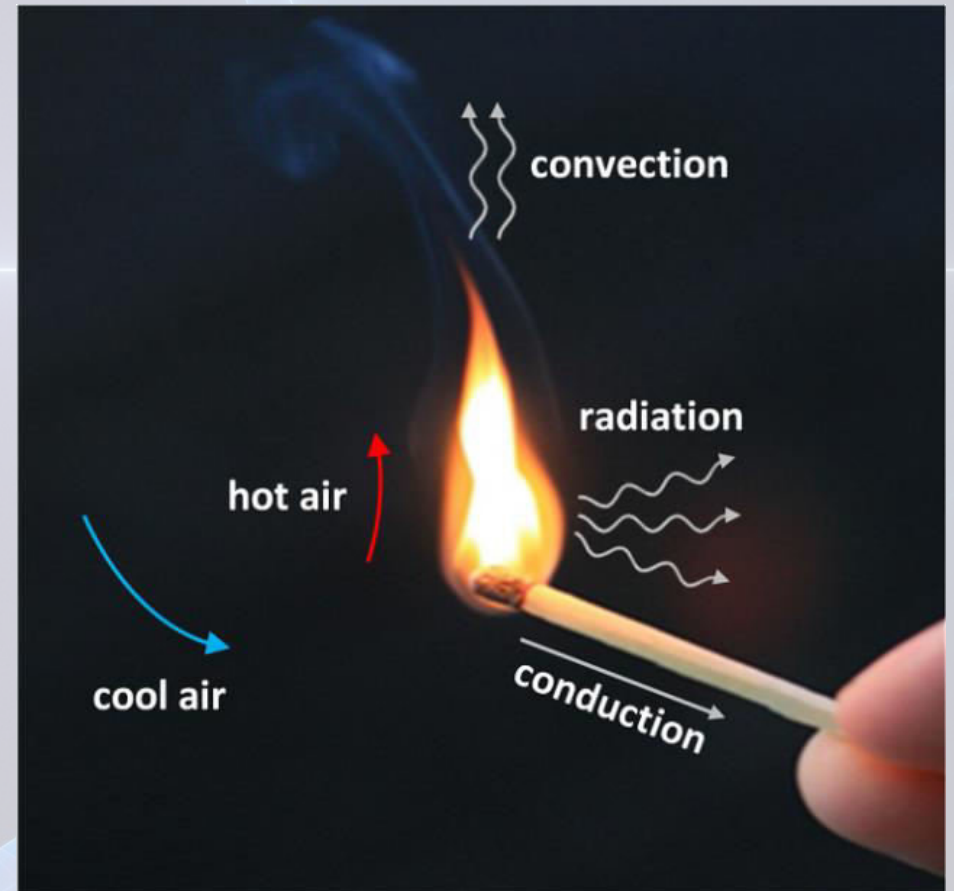
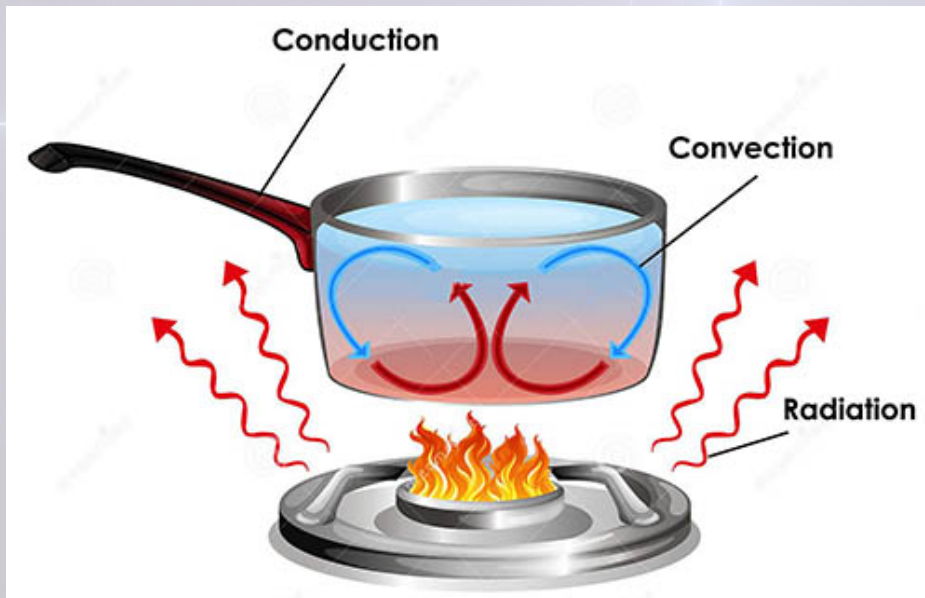
- surface T, L
 - helps observational comparison

- interior structure
 - e.g. pre-supernova structure, mixing...



Some words about convection

and about *heat transfer* in general



- convection arises wherever heat needs to be transported extra efficiently
e.g. burning core of massive stars, envelope of (super)giants and low-mass stars...
- leads to strong mixing (cf. boiling soup)

Some

ection

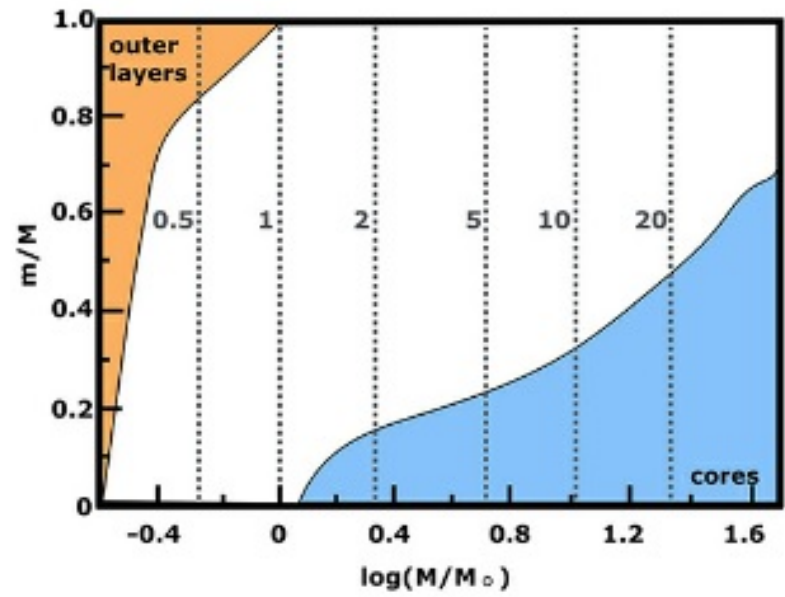


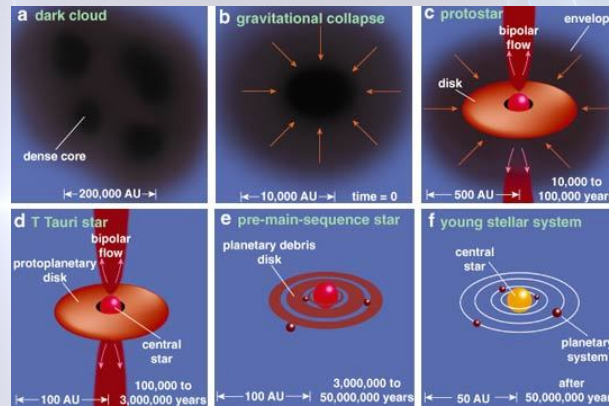
Figure 7.6. Occurrence of convection in stars at the beginning of the core H-fusion phase (ZAMS). The mass of convective envelopes (orange) and convective cores (blue) is expressed as a fraction of the stellar mass, from $m/M = 0$ in the core to $m/M = 1$ at the surface. The vertical lines indicate the stel-



- convection arises wherever heat needs to be transported extra efficiently
 e.g. burning core of massive stars, envelope of (super)giants and low-mass stars...
- leads to strong mixing (cf. boiling soup)

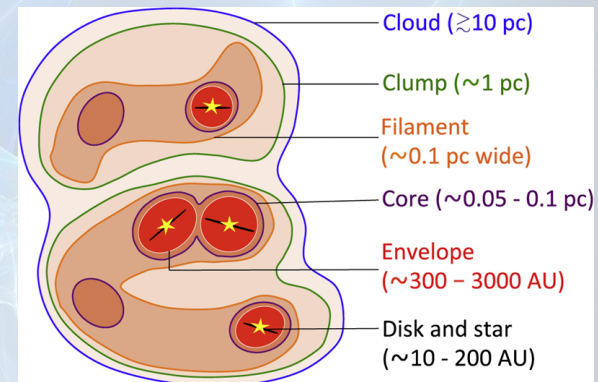
Star-formation (of massive stars)

- under active research
- low-mass stars:



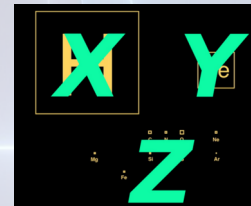
- massive stars?
 - strong radiation may blow away the material
 - hierarchical star formation?

Stellar evolution *technically* starts where star-formation ends
(IRL: ?? ...under active research)



Onset of stellar evolution: ZAMS

- Zero-Age Main Sequence
 - (core) composition:
same as the molecular cloud



$$Z_{\odot} \sim 0.014 (<2\%)$$

$$Z_{\text{LMC}} \sim 0.004$$

$$Z_{\text{SMC}} \sim 0.002$$

$$Z_{\text{GCs}} \sim <0.005$$

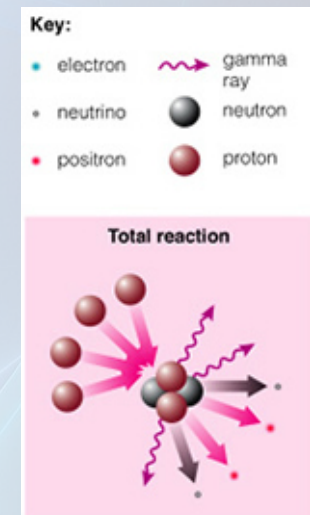
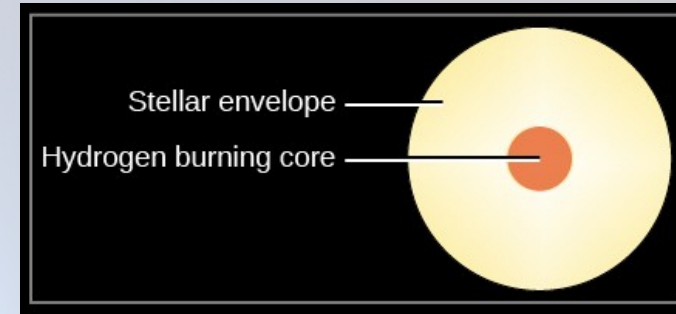
$$Z_{\text{PopIII}} = 0$$

- hydrogen burning starts (in the core)
- hydrostatic & thermodynamic equilibrium
 - no bipolar outflows etc.
 - stellar structure equations hold*

*"pre-MS": last phases of star-formation modelled using the structure equations

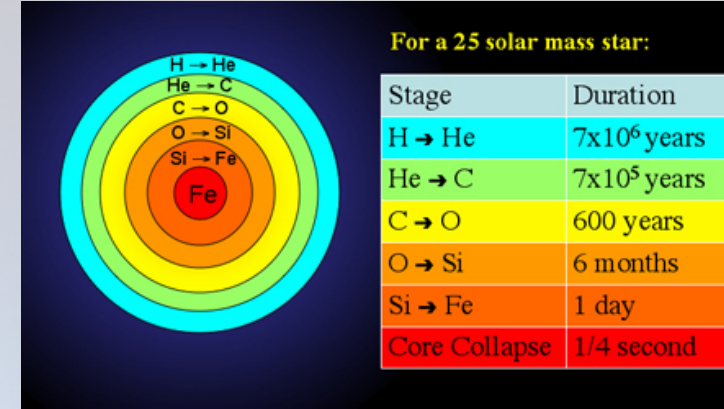
Longest phase of stellar evolution: MS

- Main Sequence
 - **core**-hydrogen-burning phase
- lasts for ~90% of the lifetime (longest of them all)
- core temperatures: ~40M K
- in massive stars: CNO cycle
 - low-mass stars like the Sun: pp-chain
- $4\ ^1\text{H} \rightarrow\ ^4\text{He} + \gamma$
- end of MS: Terminal-Age Main Sequence (TAMS)

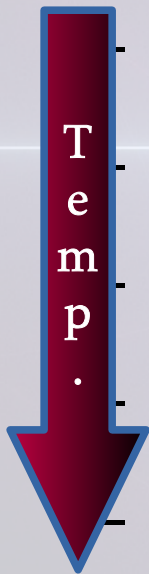


Post-MS

Pre-supernova structure



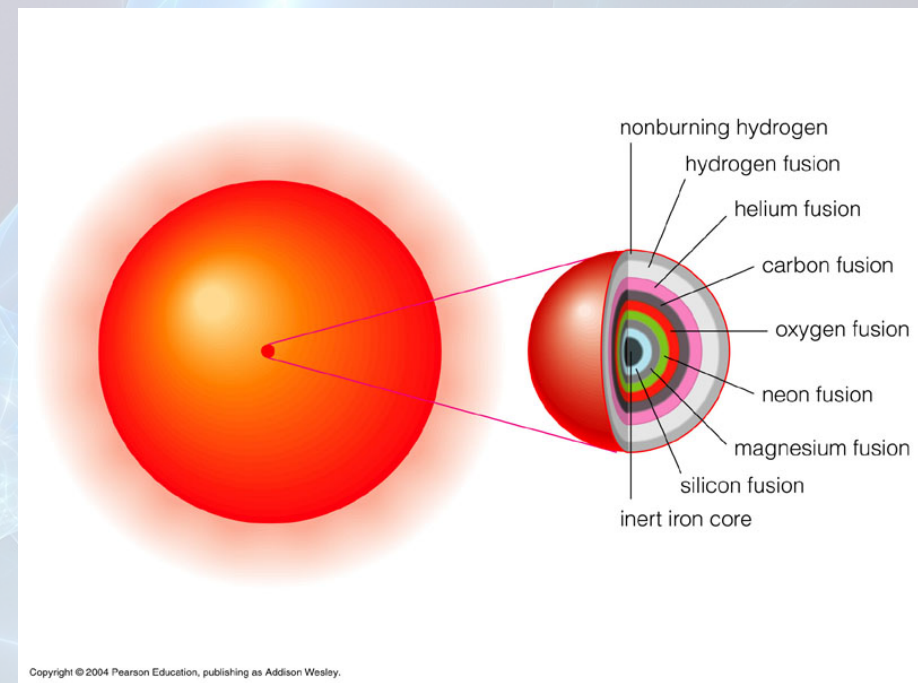
- Includes:



- core-He-burning (& shell-H-burning)
- core-C-burning (& shell-He & shell-H-burning)
- core-O-burning (& shell-C, shell-He, shell-H...
- core-Ne-burning (& shell...
- core-Si-burning (& shell...

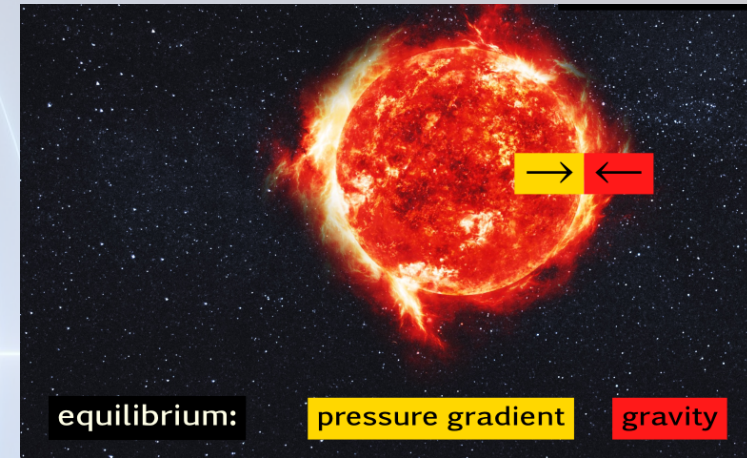
- **onion-structure** of massive stars

Note: the onion layers become more and more complex nearing the end of the lifetime

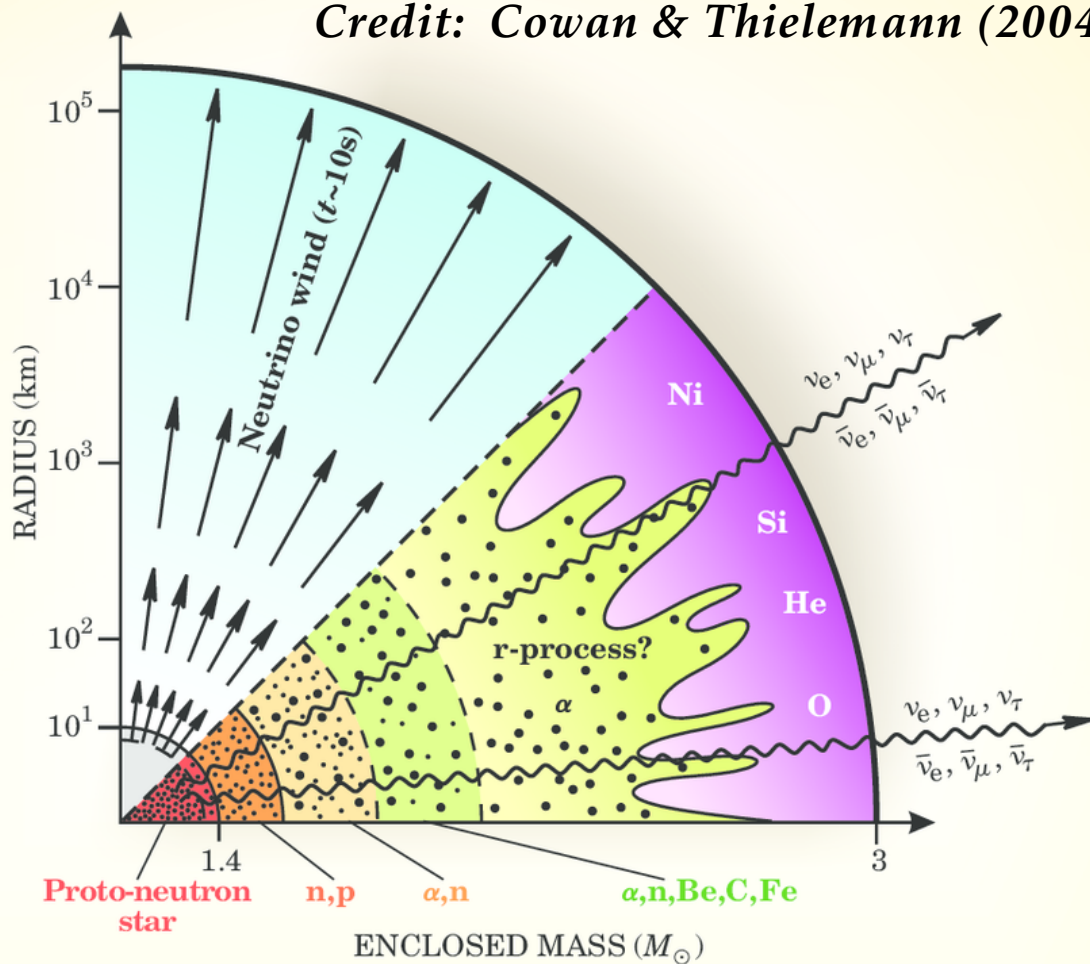


Core collapse

- Gravity takes over
 - end of the long-term equilibrium
 - fall-in: on the free-fall timescale
- ...is there something to stop it?
 - Well... it depends.
 - Most of the time (“classical” case): a neutron star forms in the center (“proto-neutron-star”)
 - a neutron star is: one giant nucleus. dense. stable.
 - bounce-back, shock waves, emission of neutrinos and light = **SUPERNOVA EXPLOSION**
 - technically: a core-collapse supernova (CCSN)

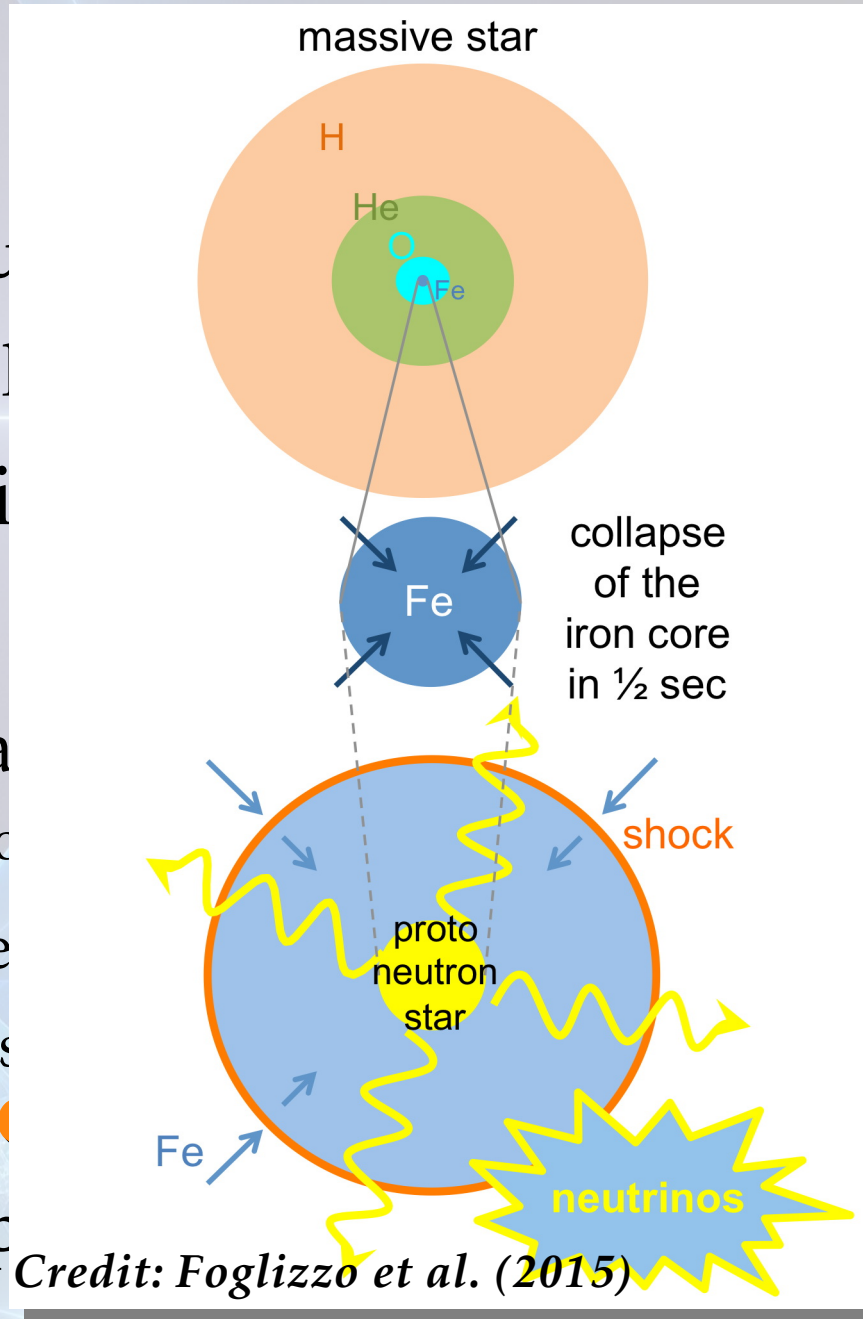


Credit: Cowan & Thielemann (2004)



apse

- forms in the center (“proto-neutron star”)
- a neutron star is: one giant nucle
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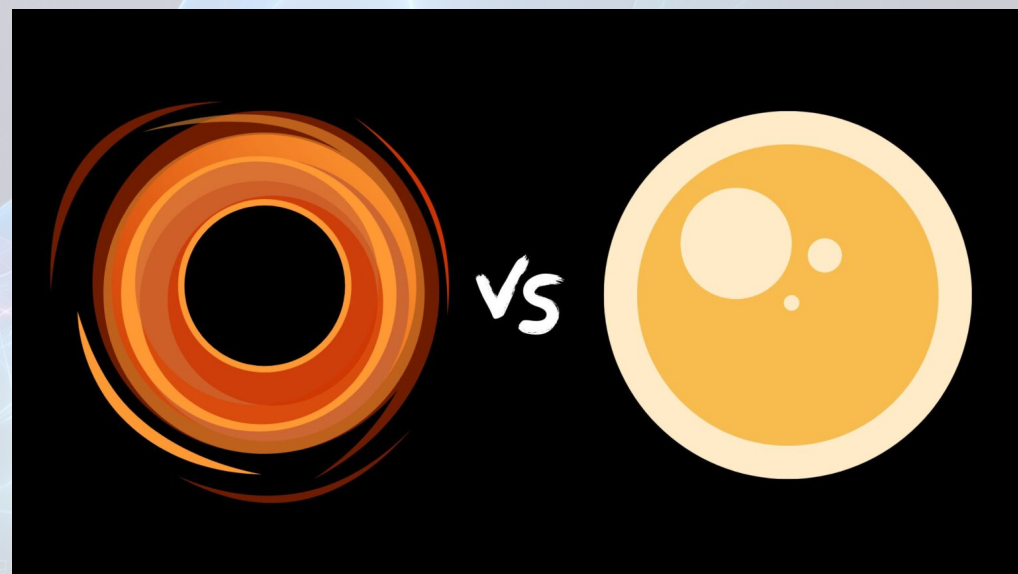
Credit: Foglizzo et al. (2015)

Fate of the proto-NS

- depends on the mass of the object
 - $M_{\text{ini}} < \sim 20 M_{\odot}$: NS
 - $> \sim 20 M_{\odot}$: BH
 - but... explosion physics is complicated (as is stellar evolution...)
- Tolman–Oppenheimer–Volkoff limit: **$2.16 M_{\odot}$**
 - maximum observed mass of a neutron star is $2.14 M_{\odot}$
for PSR J0740+6620 discovered in 2019

under active research

*Not the Chandrasekhar limit! $\sim 1.4 M_{\odot}$
(= limit between NSs and white dwarfs)*



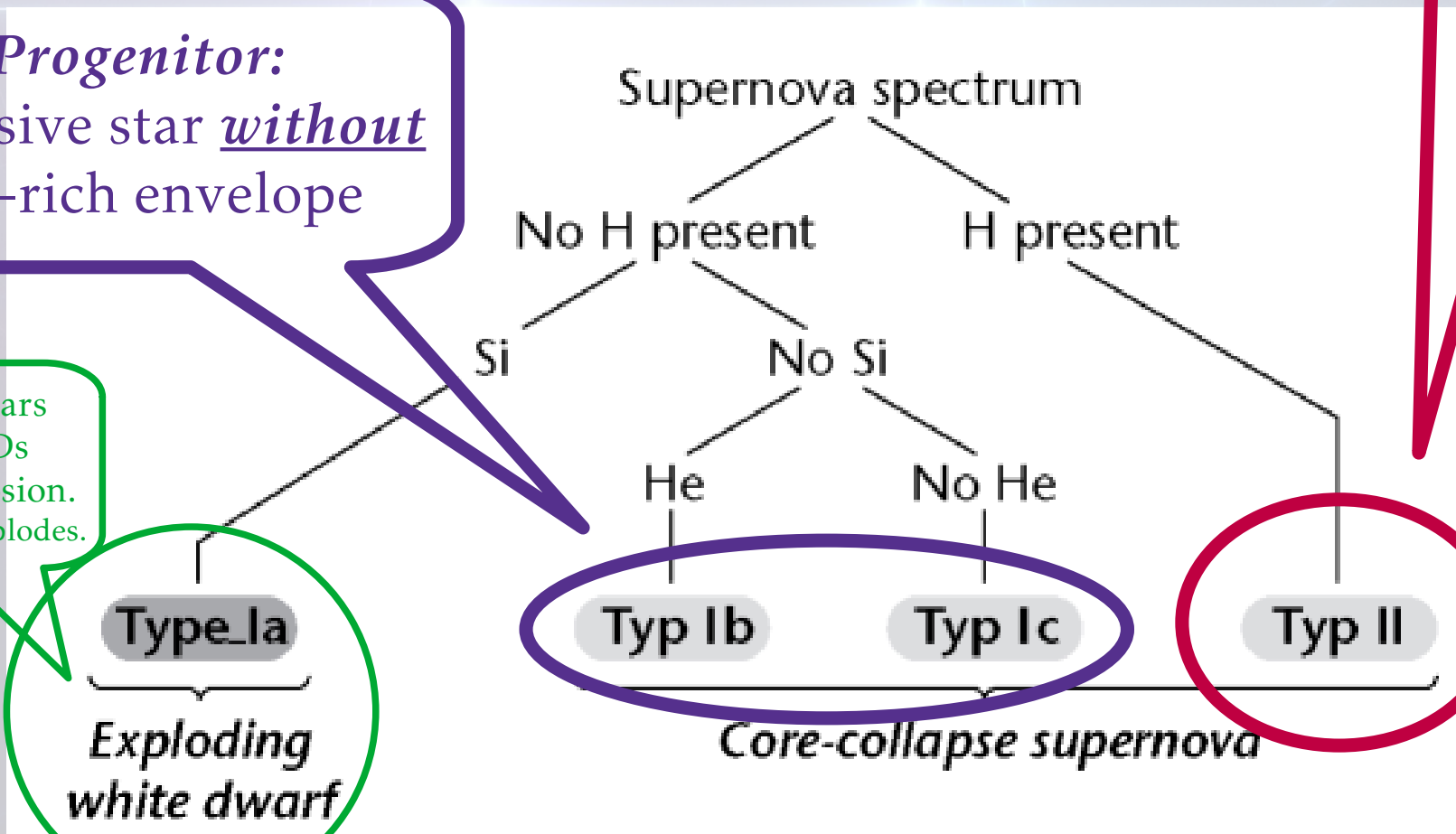
Supernova types

- There are many types...
- Classified by observers (simple picture):

Progenitor:
a massive star with
a H-rich envelope

Progenitor:
a massive star without
a H-rich envelope

Low-mass stars
become WDs
without explosion.
Later on: WD explodes.



Type Ia
Exploding
white dwarf

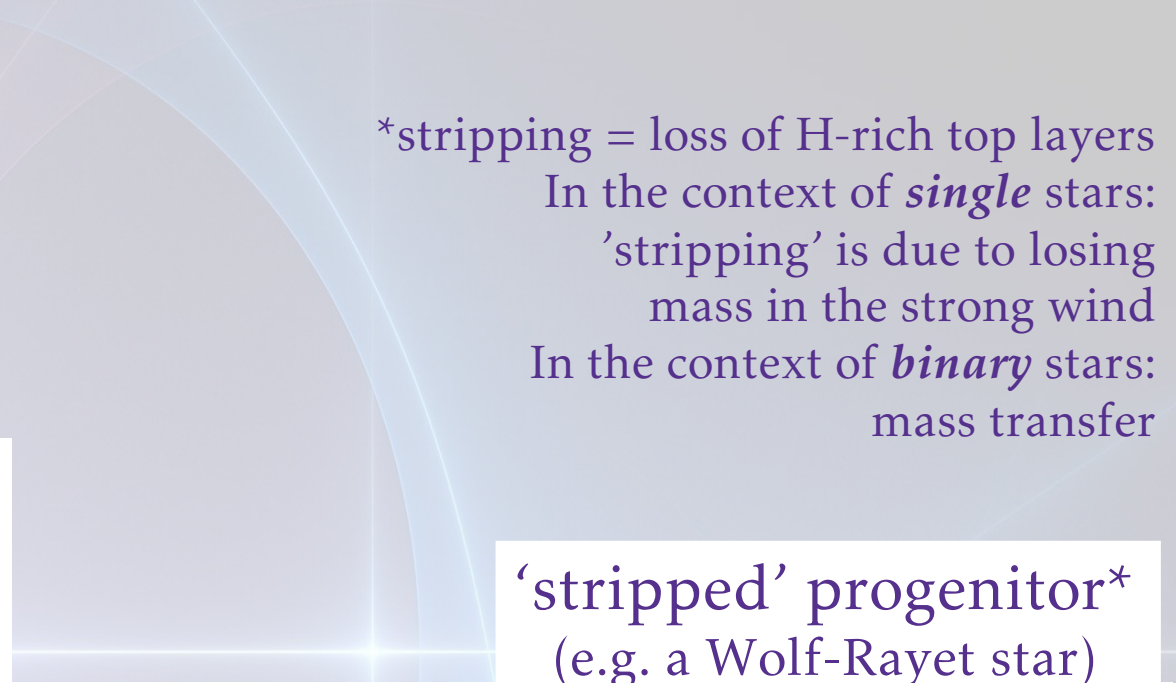
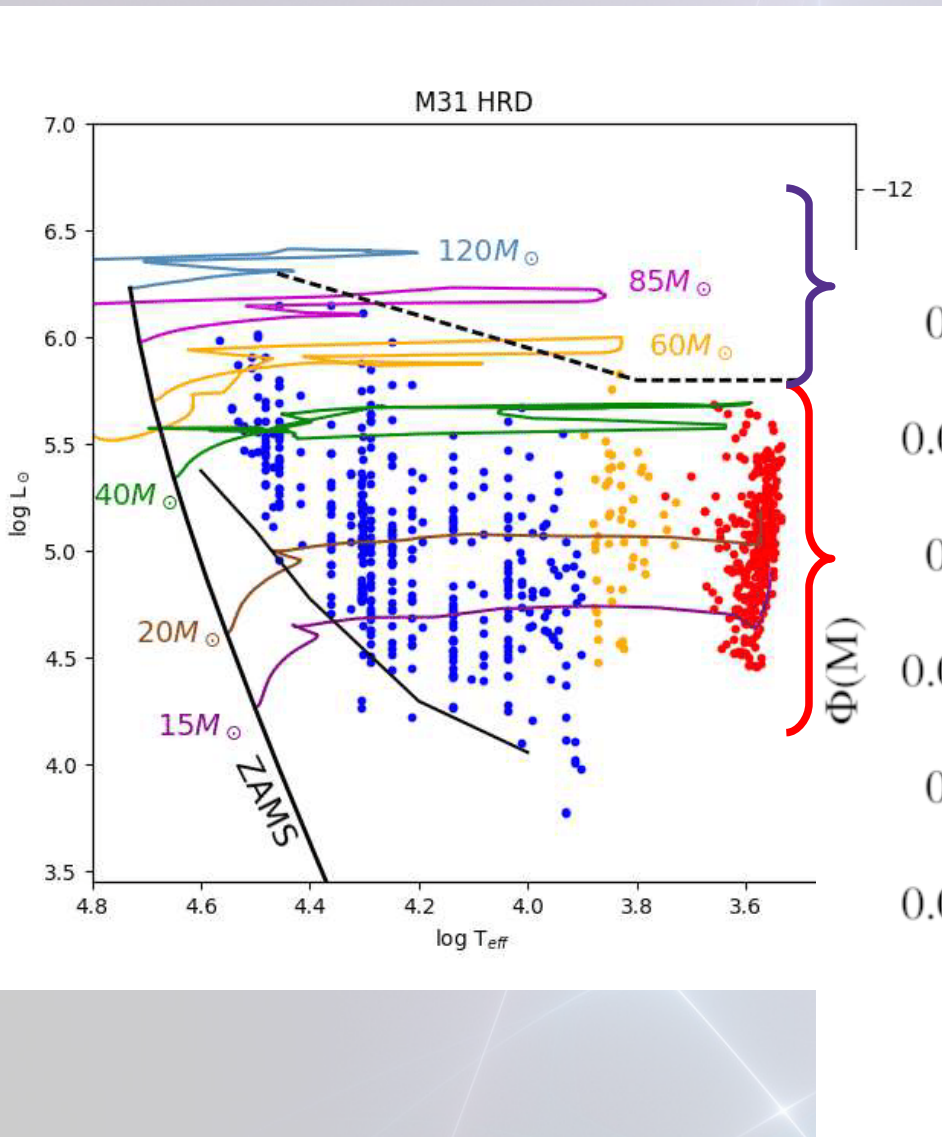
Typ Ib
Typ Ic

Typ II

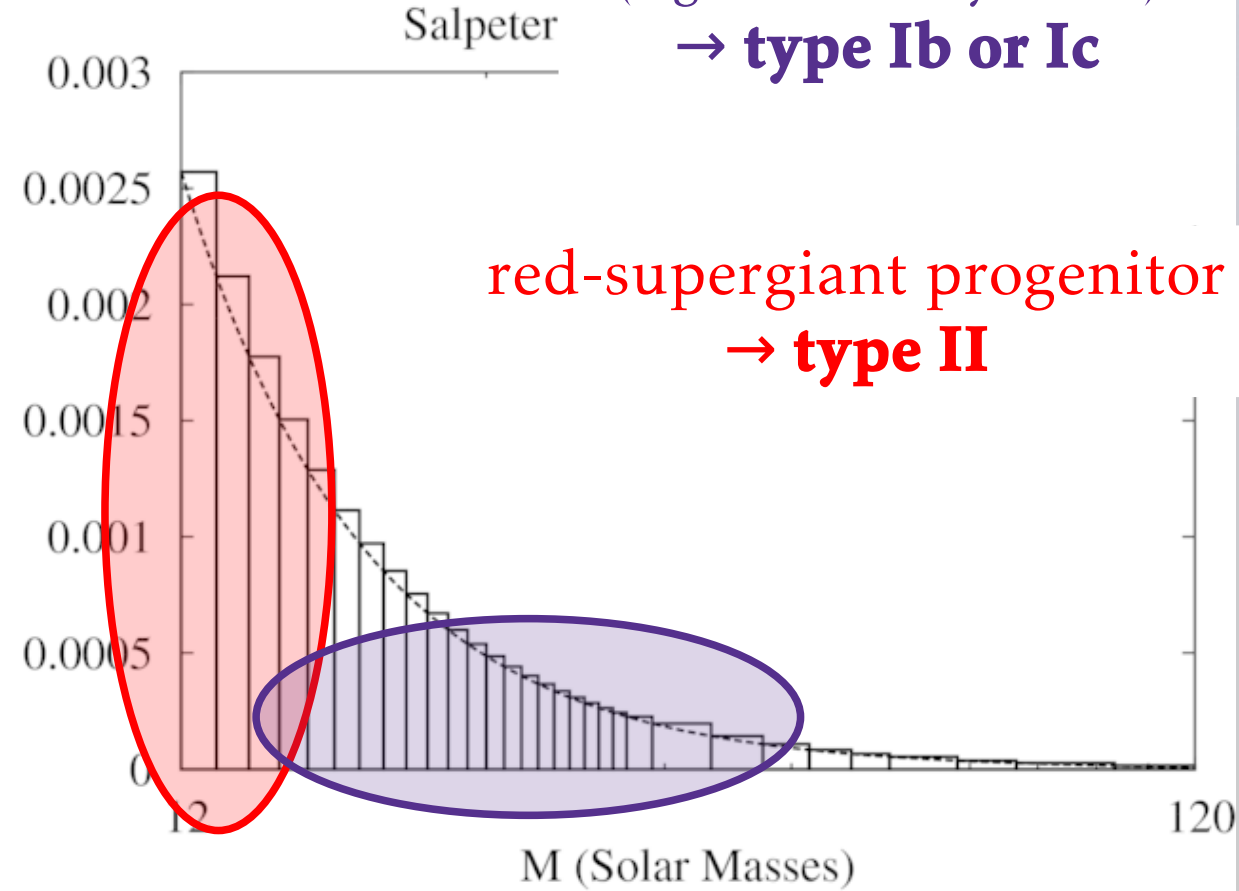
Core-collapse supernova

Only true for: single stars
 at solar metallicity
 no (or slow) rotation

*stripping = loss of H-rich top layers
 In the context of *single* stars:
 'stripping' is due to losing mass in the strong wind
 In the context of *binary* stars:
 mass transfer



'stripped' progenitor*
 (e.g. a Wolf-Rayet star)
 → **type Ib or Ic**



What are compact objects? ^{stellar 'corpses'} = **remnants**

- three main types:

- white dwarf

- neutron star

- black hole

**degenerate
stars**

other (speculative) degenerate stars:

- quark star

- preon star

- boson star

- ... (see e.g. Wikipedia)

- WDs: electron degeneracy

- nuclei (He/O/C/Ne/Mg) are *not* in degenerate state

- NSs: neutron degeneracy too

degeneracy pressure → **stability** against
(self-)gravity

composition depends on mass
(i.e. stellar evolution of the
low-mass star in question)

What

- three main

- white dwarf
- neutron
- black hole

- WDs: electron

- nuclei (He/O/C/Ne)

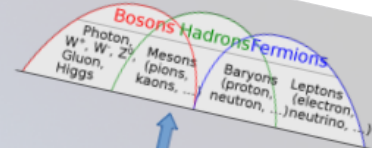
- NSs: neutron degeneracy too

degeneracy pressure → **stability** against (self-)gravity

Degeneracy

- Imagine: plasma (of fermions, i.e.: e^- , p^+ , n^0 ...)
 - at normal densities: thermal pressure (ideal gas)
 - let's cool it and compress it repeatedly!
 - at some point, **Pauli exclusion principle** turns on
 - forbids the fermions to occupy identical quantum states
 - thus, if they are forced closer, they must be placed at different energy levels → extra pressure (a *very* strong one)
- can happen to: only e^- (=WD) **or** p^+ & n^0 & e^- (=NS)

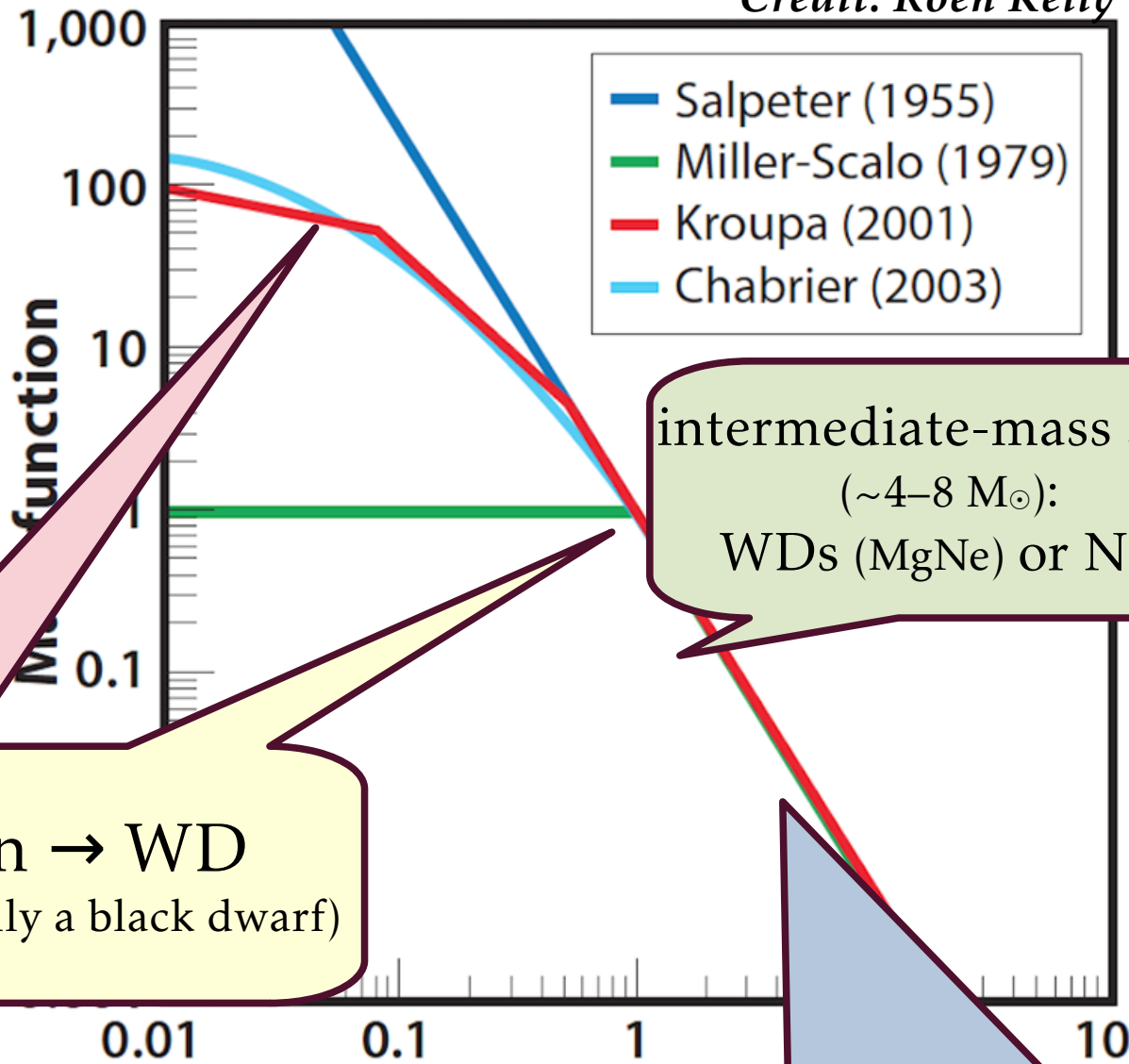
Funfact: degeneracy pressure depends only weakly on the temperature.
Increasing the temperature of degenerate stars has a minor effect on the structure.



remember: γ is a boson

Credit: Roen Kelly

#stars: $\Phi(m) \sim m^{-2.35}$



$\Phi(M)$

sub-Solar masses:

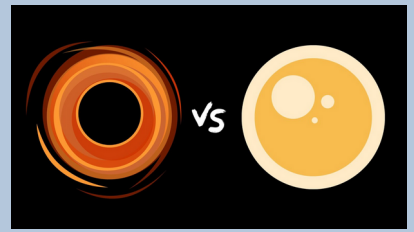
– also white dwarfs
(=compact object,
stellar remnant)

– *however*:
brown dwarf stars
may live longer than
the Universe...

Sun → WD
(eventually a black dwarf)

intermediate-mass stars
(~4–8 M_{\odot}):
WDs (MgNe) or NSs

Massive stars:
NSs or BHs*

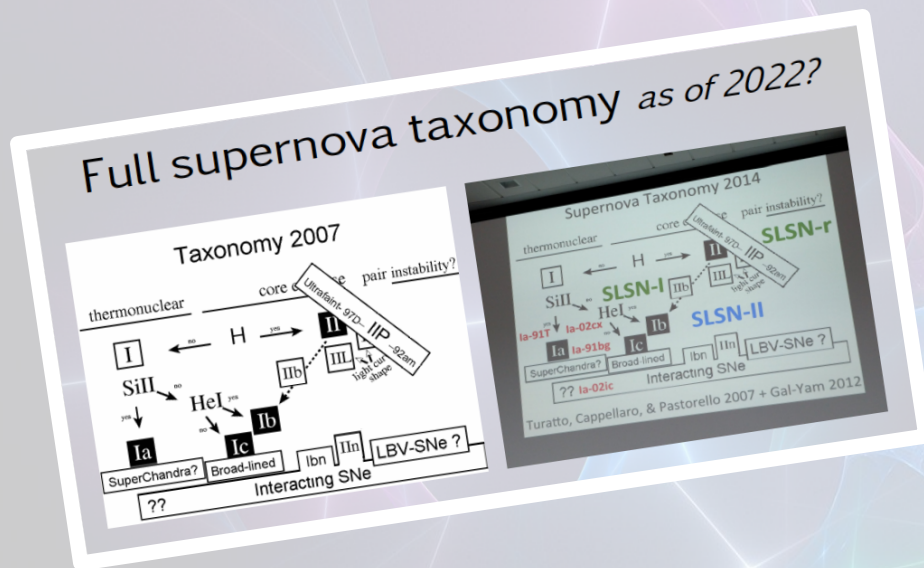


THIS HAS BEEN: single massive stars' lives at solar metallicity

(without rotation)

**Our strategy: start with
Massive Stars at Solar Z**

- sub-Solar metallicities?
- fast-rotating stars?
- stars in a binary system?

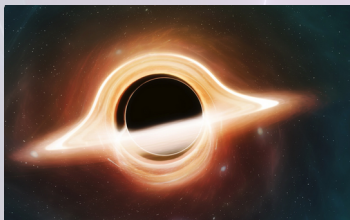


Sub-Solar metallicities

(and still no rotation and no binary companion)

- Main effect: mass loss becomes WEAKER
 - stars live their lives with more mass retained
 - also *end* their lives with more mass retained

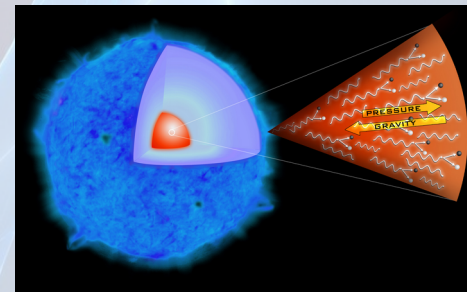
Consequence #1:



direct fall-in into
a black hole
(of mass $\sim 20\text{-}40 M_{\odot}$)

*key question: is there something to STOP
the collapse? if yes: CCSN (type II, Ib/c)
if no: direct fall-in into a BH (no explosion)*

Consequence #2:



pair-instability developing, leading to
a PISN (or maybe a pPISN)
or again to direct fall-in to a BH
(*but this will be a very heavy BH with $>150 M_{\odot}$*)

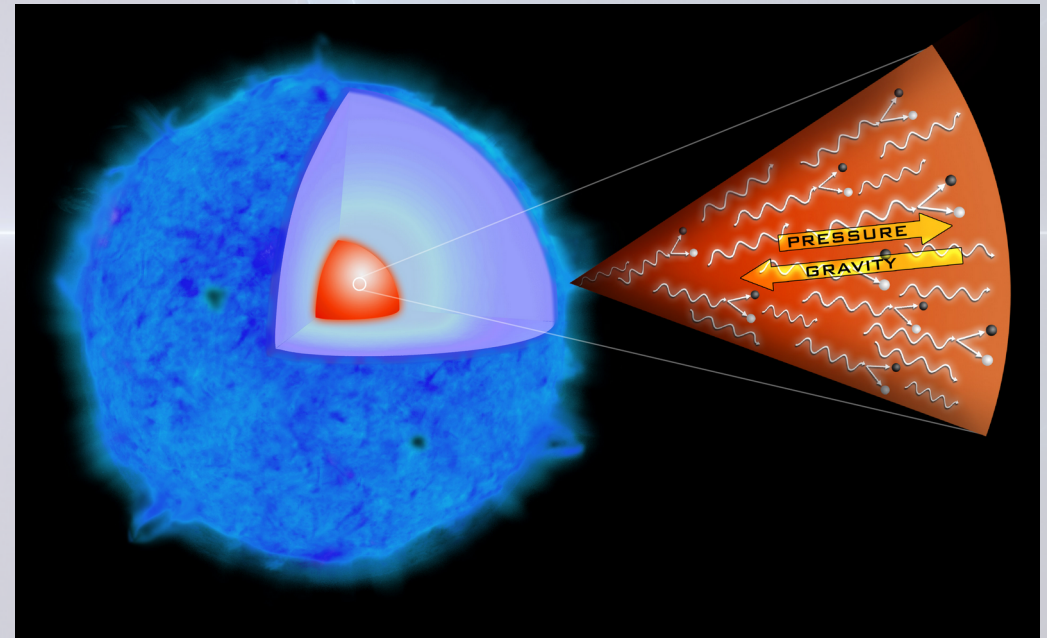
Why?

Pair Instability

happens in *quite* massive stellar cores
mass values quoted here mean M_{ZAMS}

Photon pressure
drops due to
 $\gamma\gamma \rightarrow e^- \text{ \& \ } e^+$

can happen
already in stars
with $\approx 60 M_{\odot}$



Collapse

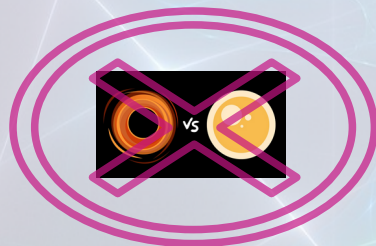
*key question, as always:
is there something to stop it?
...if not:*

Explosive O-burning
→ supernova

happens with stars
 $\sim 140-260 M_{\odot}$

pair-instability supernova (PISN)

No remnant!



above $260 M_{\odot}$:
again direct collapse into BH
(gravity wins)

Pair Instability

happens in *quite* massive stellar cores
mass values quoted here mean M_{ZAMS}

Photon pressure
drops due to
 $\gamma\gamma \rightarrow e^- \text{ \& \ } e^+$

can happen
already in stars
with $\gtrsim 60 M_{\odot}$

Collapse

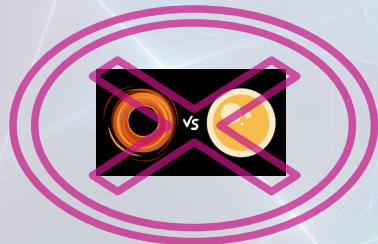
*key question, as always:
is there something to stop it?
...if not:*

Explosive O-burning
→ supernova

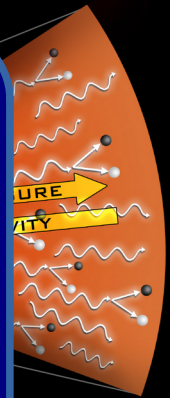
happens with stars
 $\sim 140\text{-}260 M_{\odot}$

pair-instability supernova (PISN)

No remnant!



Note:
– iron-core stage is not even reached yet
– **whole star explodes**
– nucleosynthetic yield (ejected material's composition) is different from classical CCSNe
– have we ever observed such a SN?
...who knows

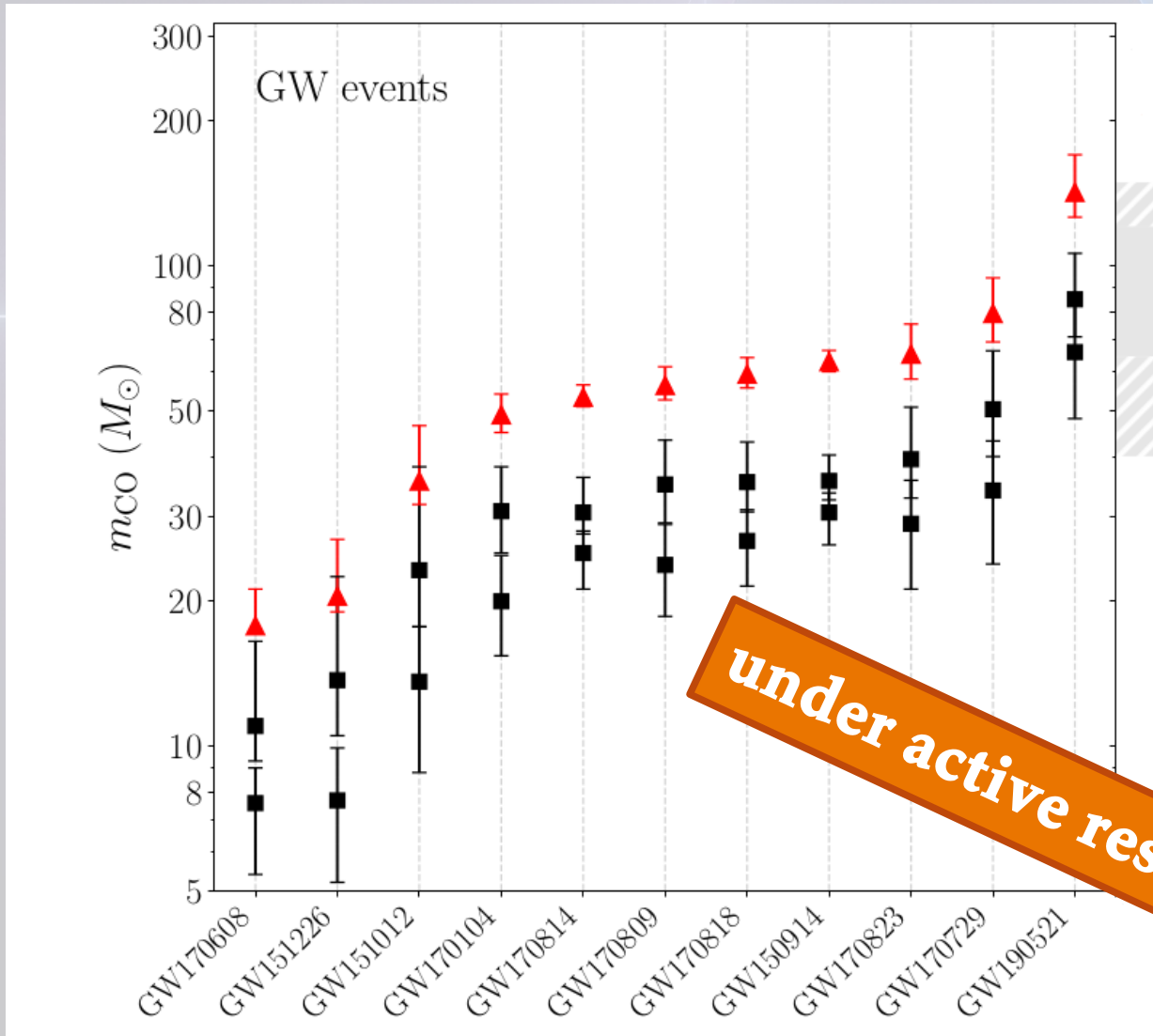


stars between $60\text{-}140 M_{\odot}$:
collapse is stopped by the star re-gaining its hydrostatic stability

might* lead to a
'pulsational pair-instability supernova' (pPISN)

because layers lost in the pulsations
might collide and emit light

The BHs of GW190521 shouldn't exist...



BH no go zone

GW190521:

$m_1 = 85 (+21/-14)$
Msun

$m_2 = 66 (+17/-18)$
Msun

What happens at

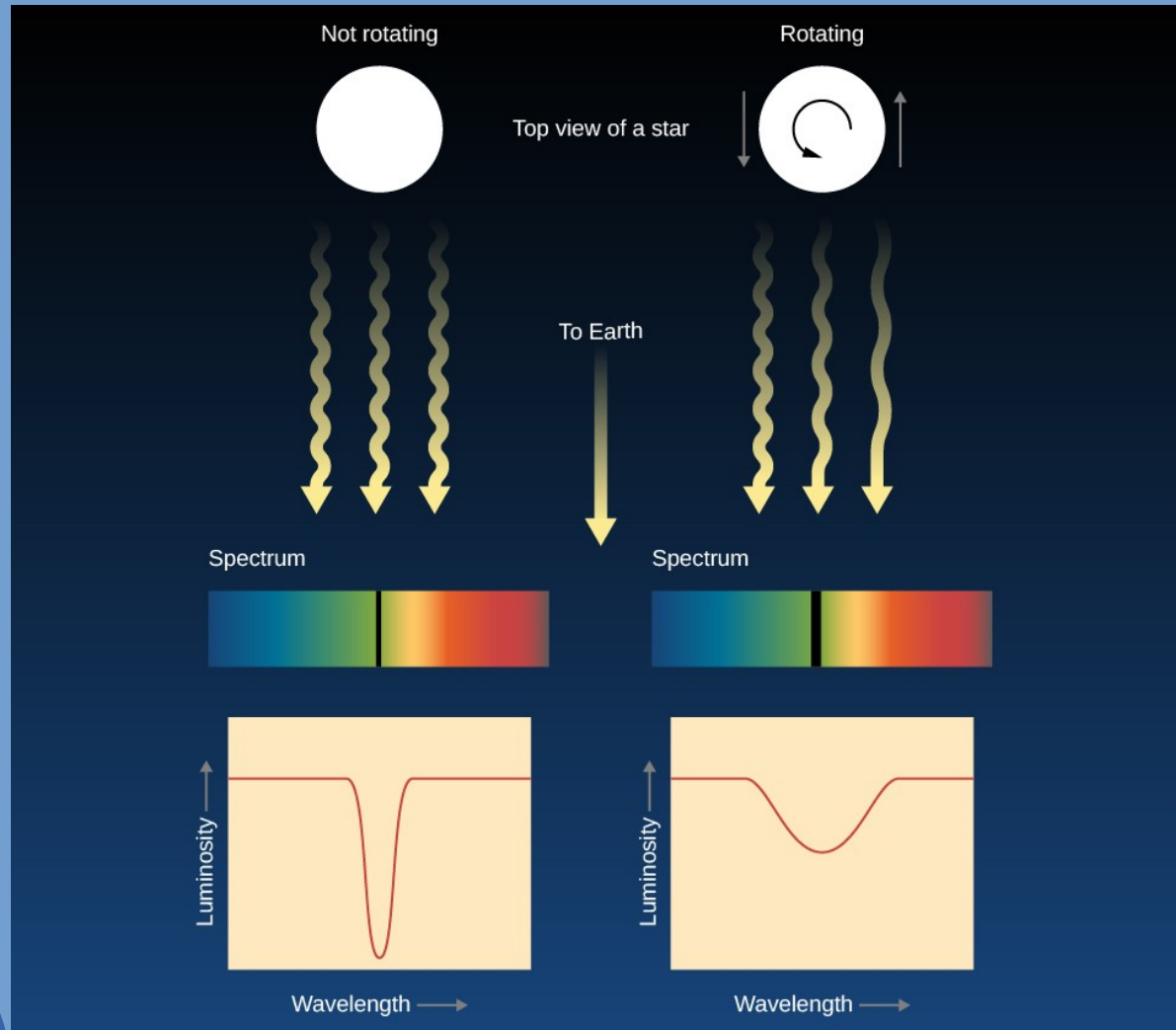
→ sub-Solar metallicities? ✓

→ fast-rotating stars?

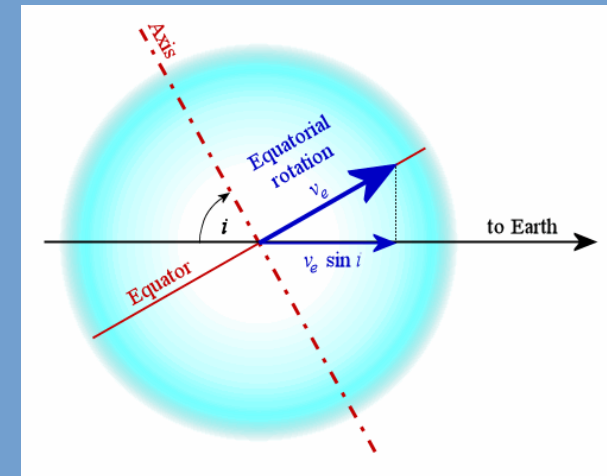
→ stars in a binary system?

Massive stars rotate... sometimes quite fast

How do we know that? → line profile

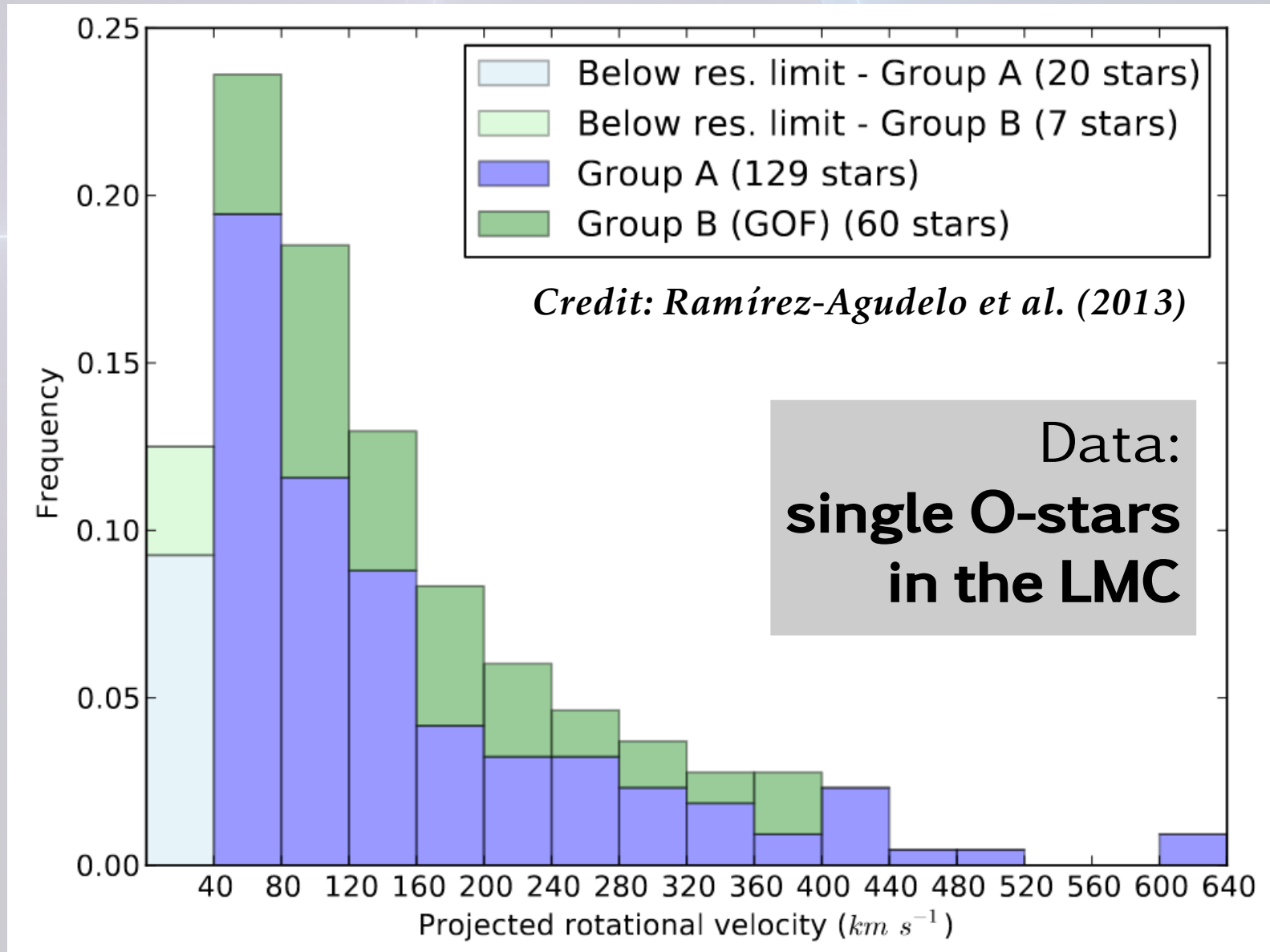


inclination?



$v \cdot \sin(i)$
("projected rotational velocity")

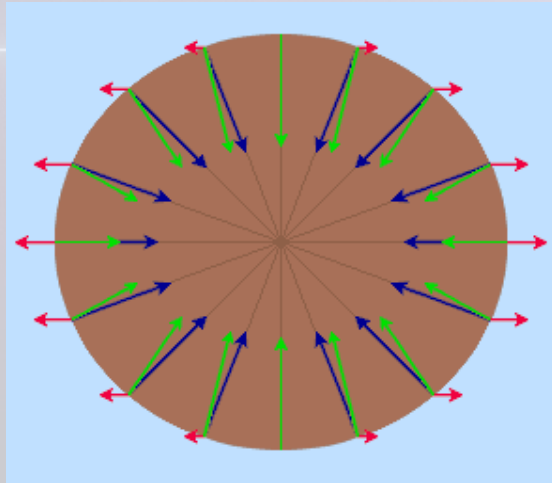
Massive stars rotate... sometimes quite fast especially at low Z!



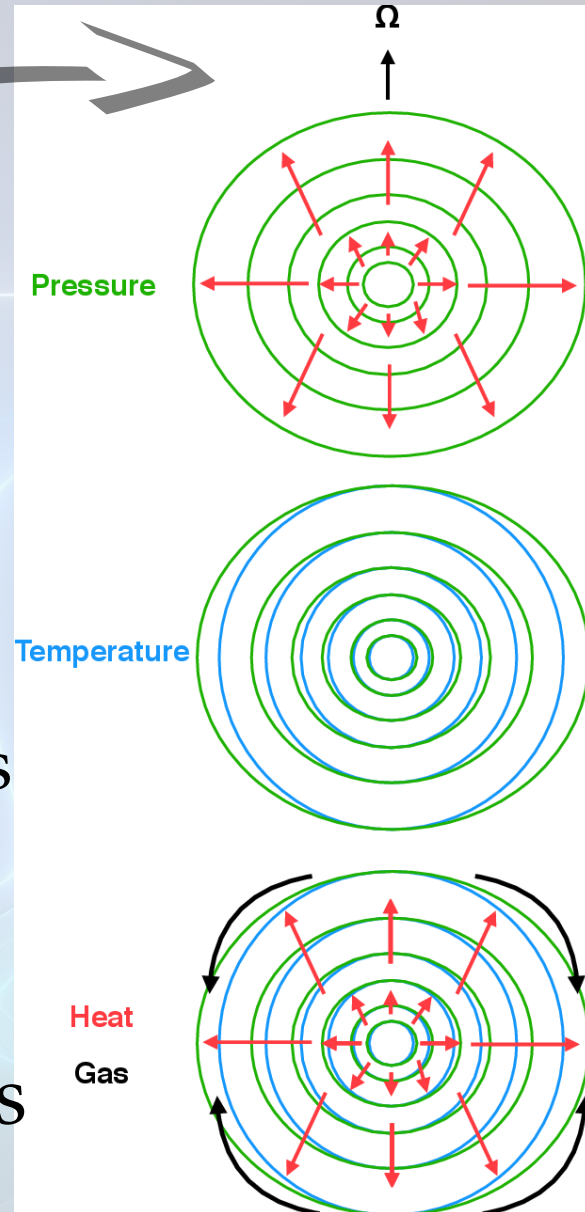
Theoretically considered:

Rotation can effect the structure

- centrifugal force
 - oblate shape
 - extra mixing inside!
- extreme case:
 - “break-up” rotation
“critical rotation”
 - $F_{\text{cen}} \geq F_{\text{grav}}$ “Keplerian break-up frequency”
 - leads to extra mass loss
 - mass dependent
e.g. “B[e] star” phenomenon



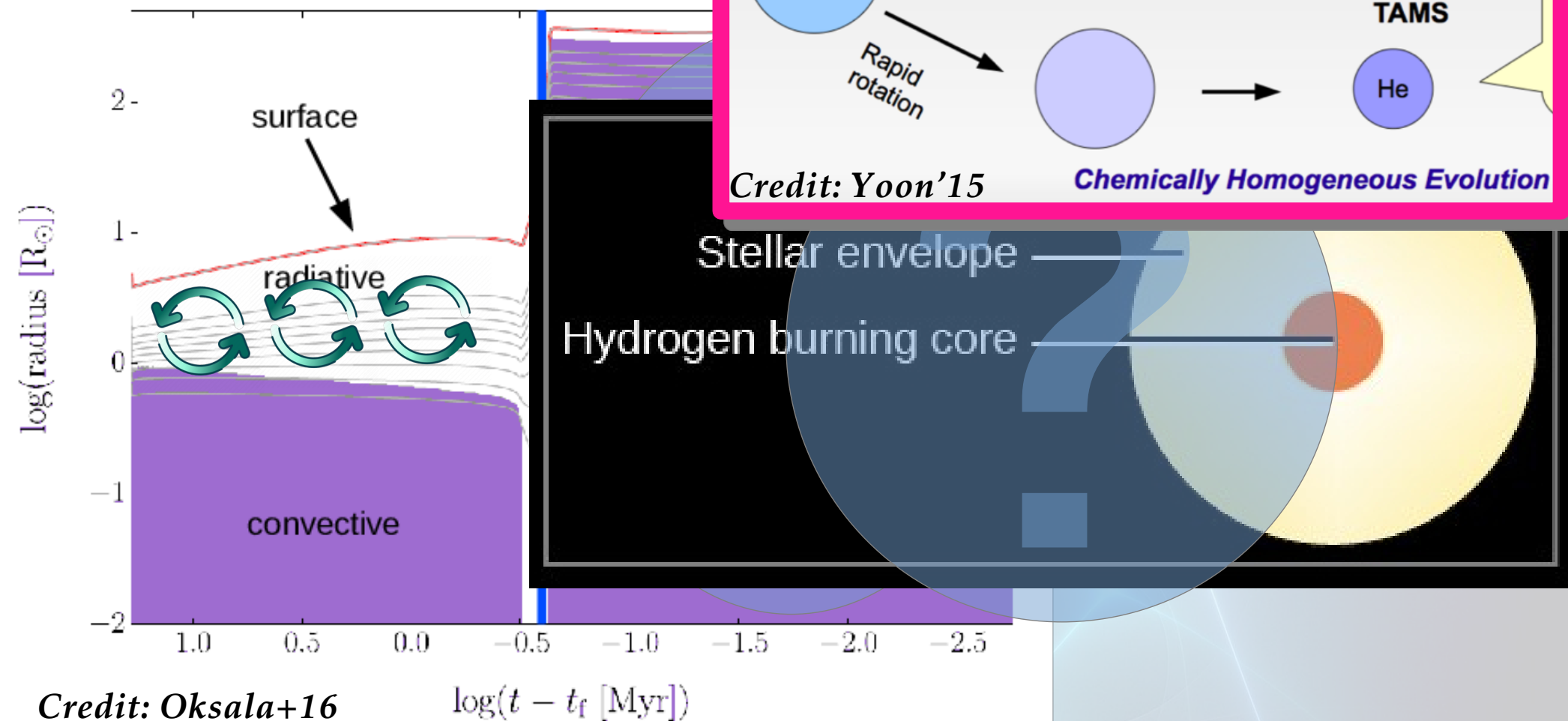
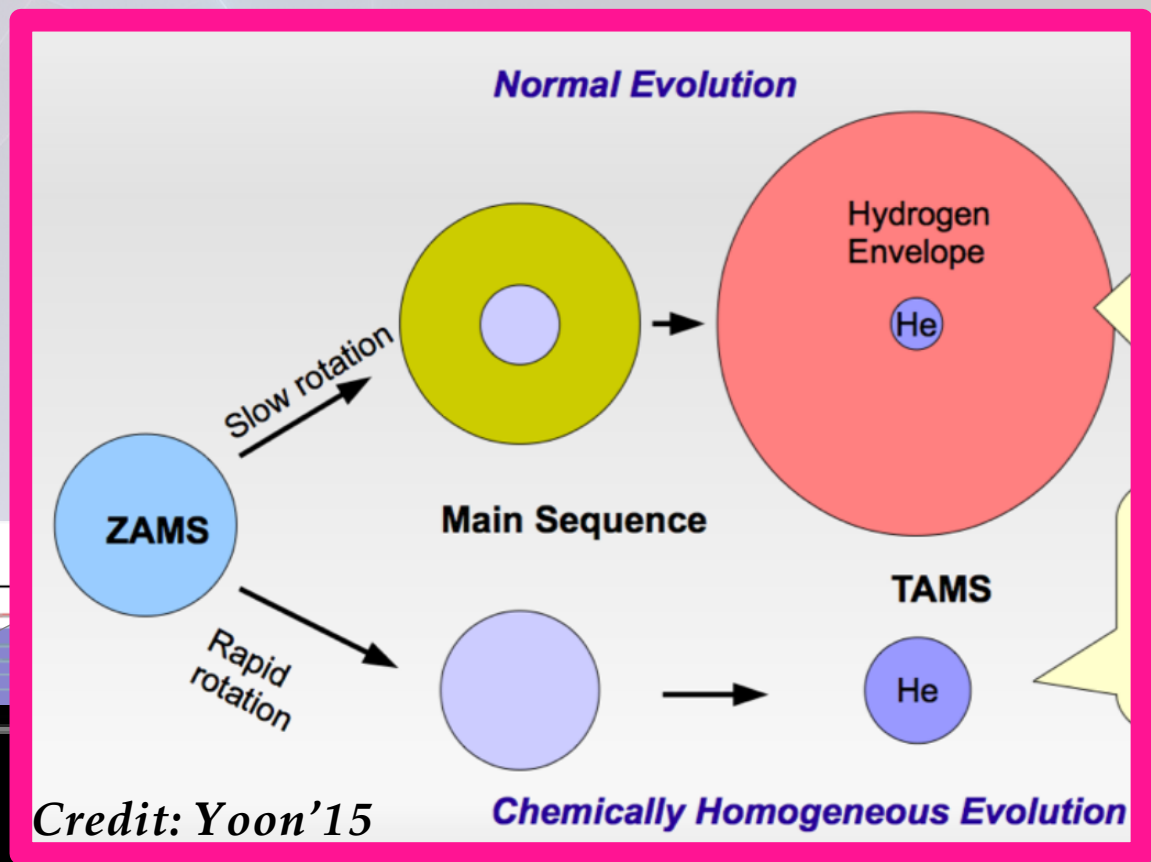
Credit: Jermyn+18



- non-extreme case: mixing & mass loss

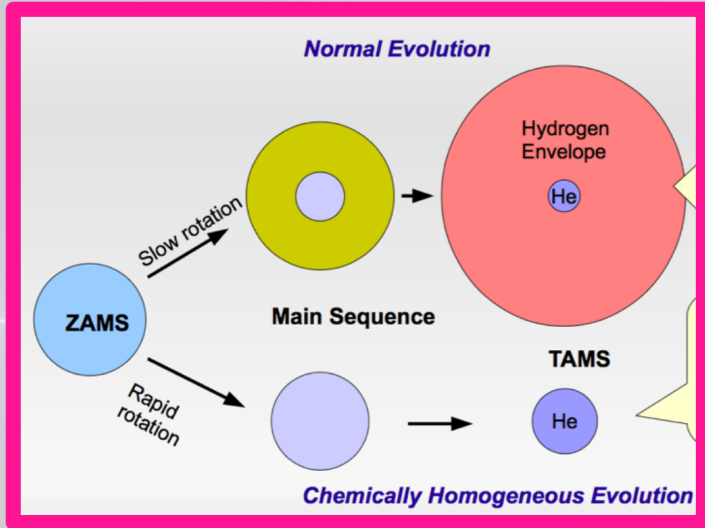
Rotational mixing

...but depends on Z too:
 metallicity mass loss;
 mass loss \rightarrow angular
 momentum loss

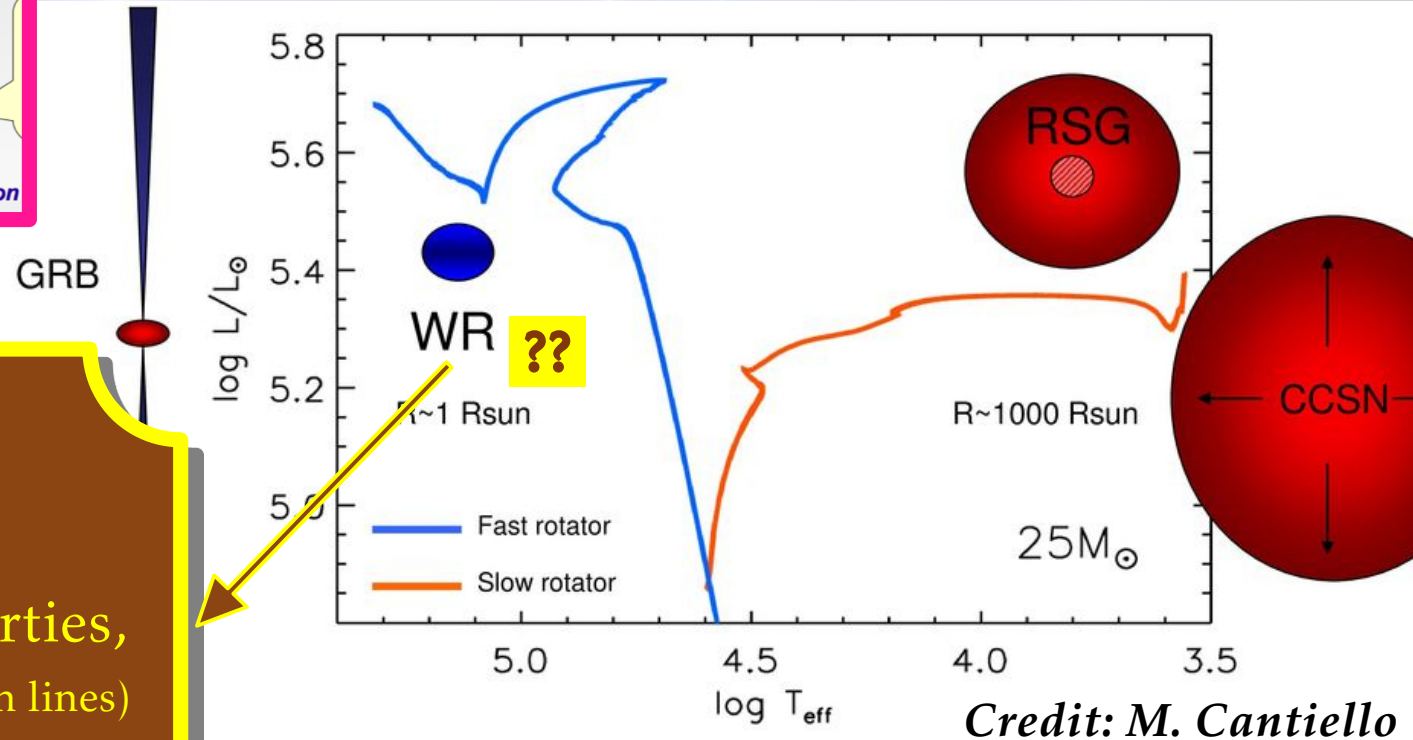


Chemically homogeneous evolution

= *Quasi-chemically homogeneous evolution*



In the Hertzsprung–Russell diagram:



a hot, He-rich star

depending on wind properties, might be a WR star (emission lines) or something else? (absorbtion lines)

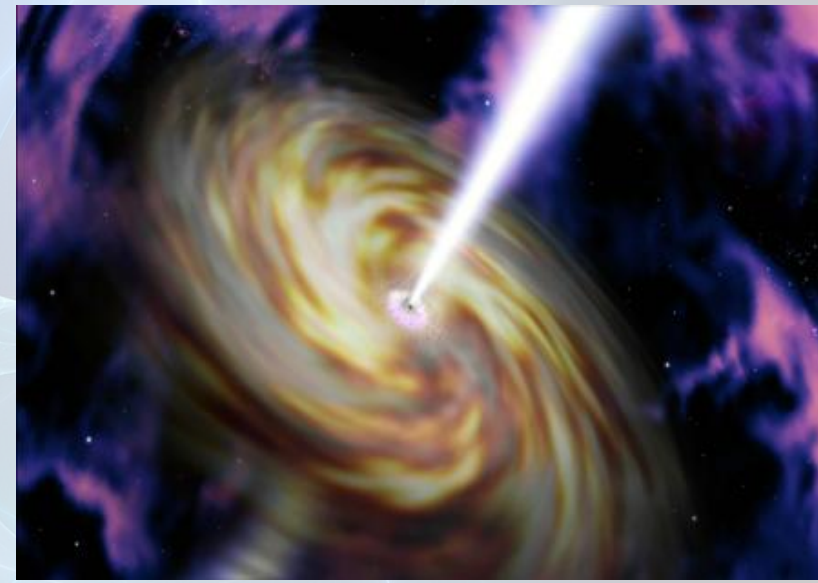
*Type of final explosion?
type Ib/Ic (core collapse)
but ROTATING!! → a 'collapsar'*

Collapsar

- “core collapse” \neq “collapsar”
- core collapse + fast rotation = collapsar
- collapsar \rightarrow accretion disc & jets
- if the jet aligns with the line of sight:
long-duration gamma-ray burst
may be observed (L-GRB)
 - accompanied by a SN Ib/Ic
- if not aligned: SN Ib/Ic

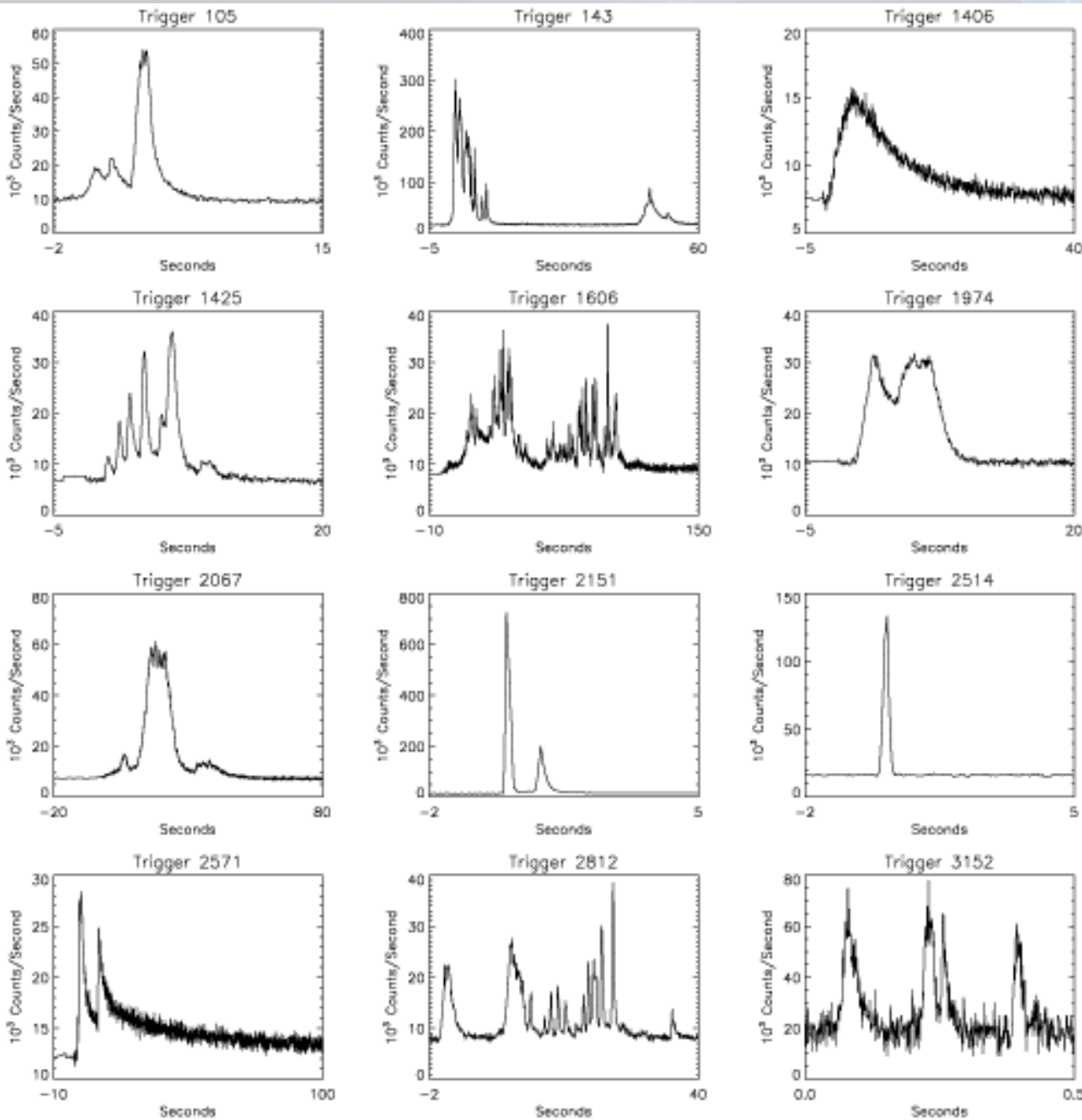
A BH or a NS forms
in the middle.
The proto-NS is probably
highly magnetized.

Synchrotron radiation
accelerated in the jet.
 γ -rays emitted.



What are GRBs?

Observationally...



– during the cold war...

– today: satellite missions

e.g.:

Fermi Gamma-ray Space Telescope
Neil Gehrels Swift Observatory etc.

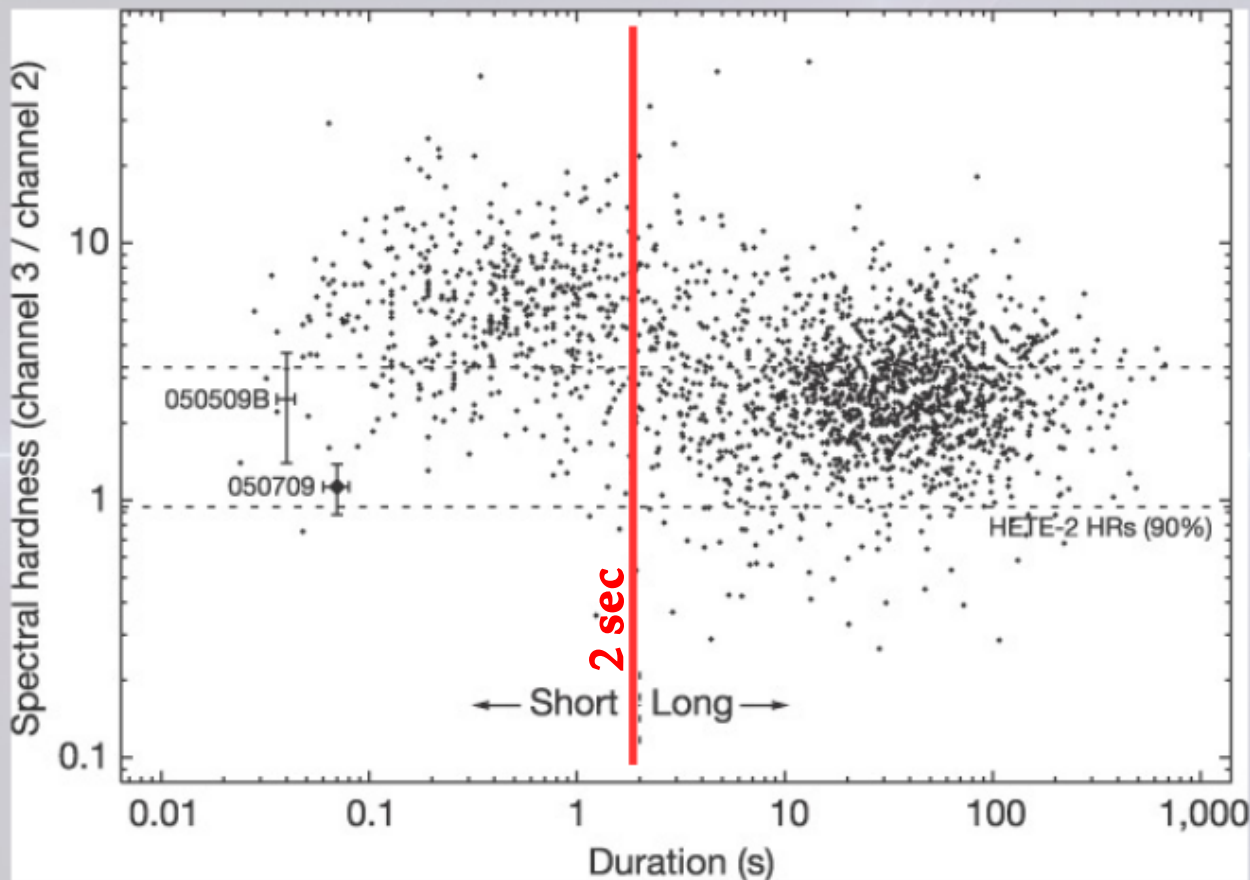
– daily observations

– majority of the energy is measured in γ -rays

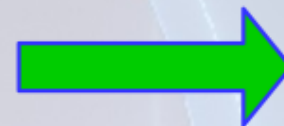
– there is a so-called “afterglow” observed at softer wavelength (X-ray, optical, IR, radio...) after the prompt γ -emission

What are GRBs?

At least two, physically distinct types of objects

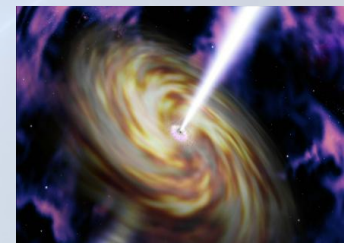


Credit: Hjorth+2005



Long/soft:
Massive Stars
at
collapse

a “collapsar”



Short/hard: two Compact Objects at merger

binarity!
GWs!

Our strategy:

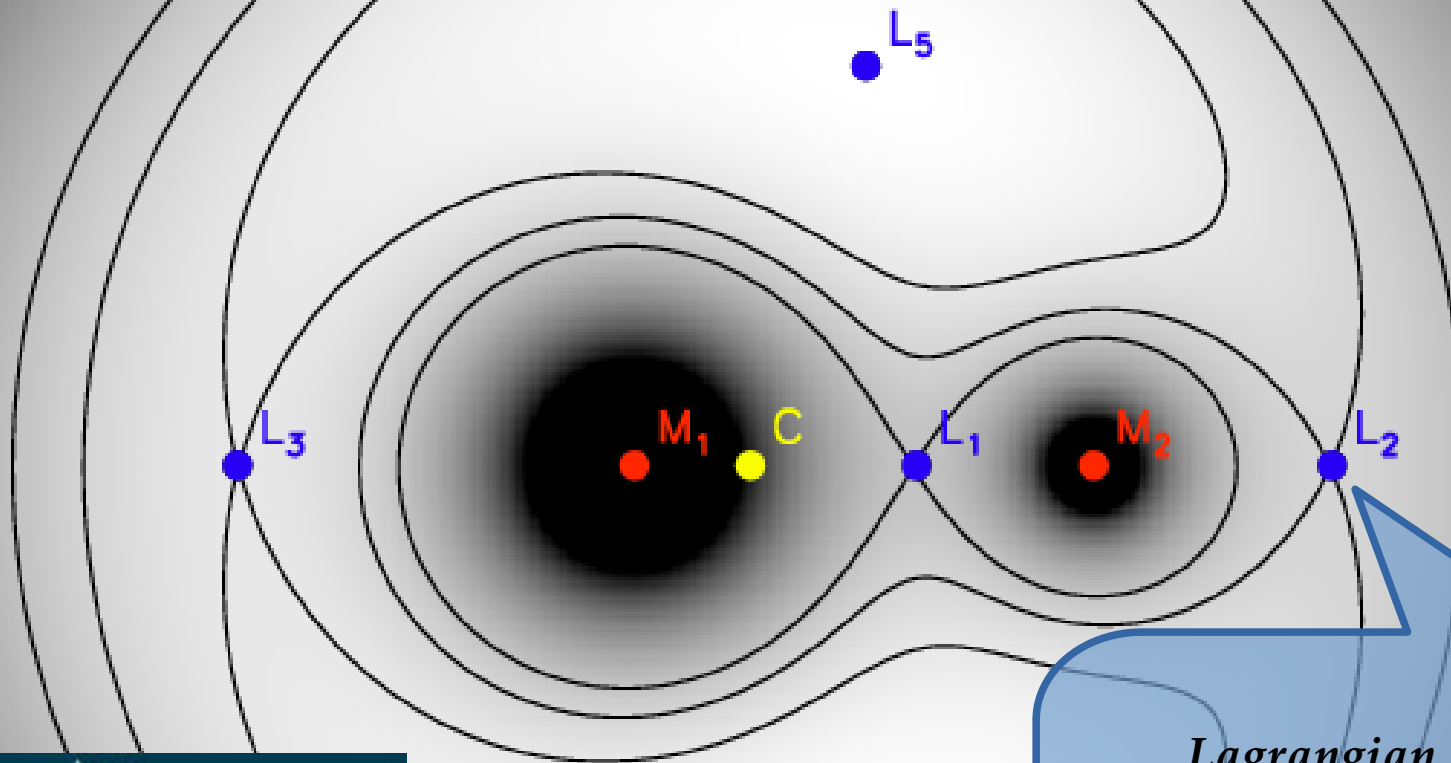
**start with
Massive Stars at Solar Z**

→ sub-Solar metallicities?

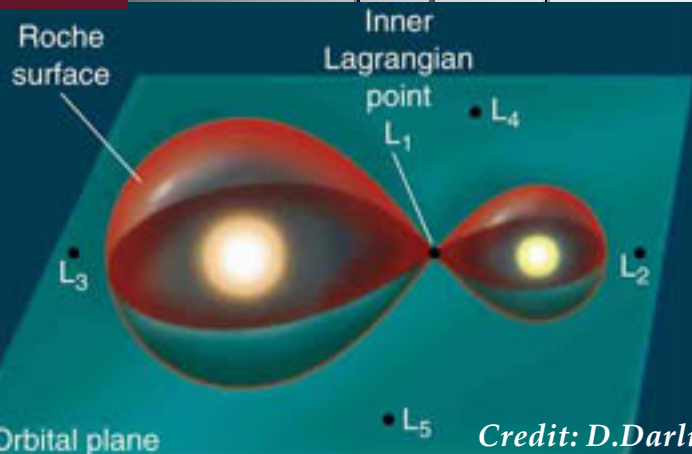
→ fast-rotating stars?

→ stars in a binary system?

The most important concept: Roche-lobe



in 3D:



Credit: D.Darling

Lagrangian points:
where the gravitational forces of the two bodies and the centrifugal force balance each other

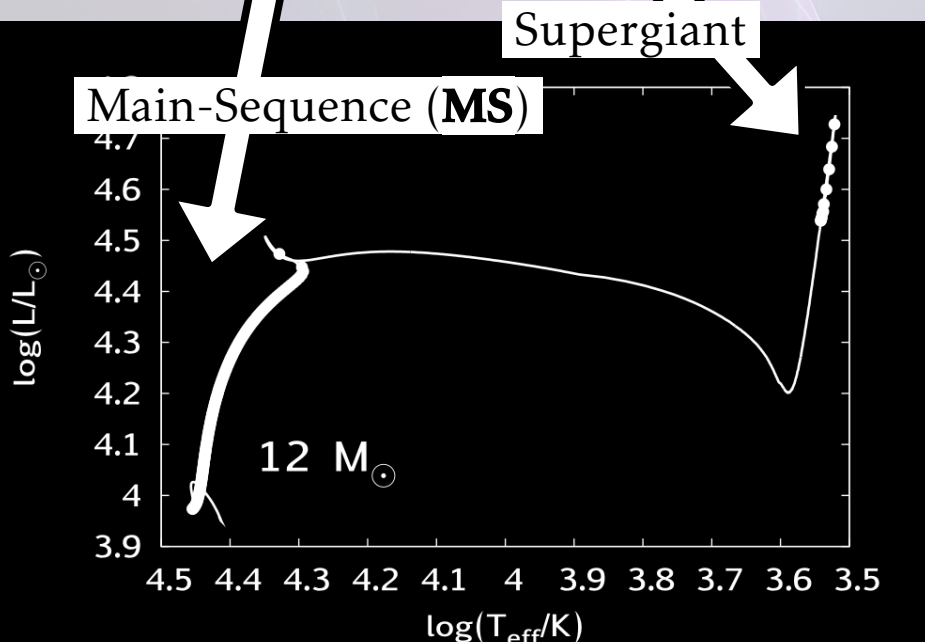
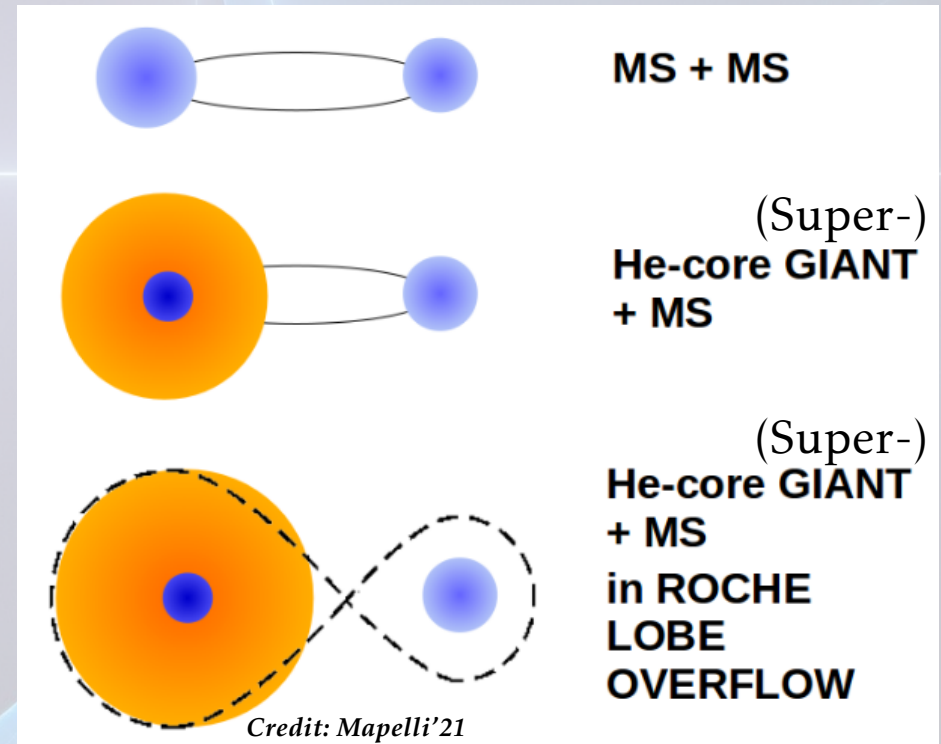
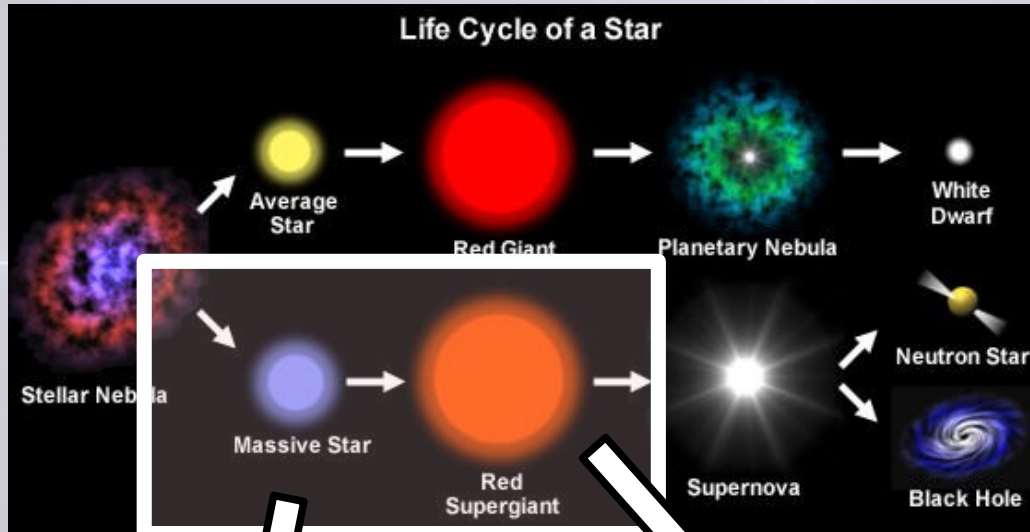
Credit: Bonneau+15

with Solar Z, no rotation

Imagine two (massive) stars!

One (massive) star alone:

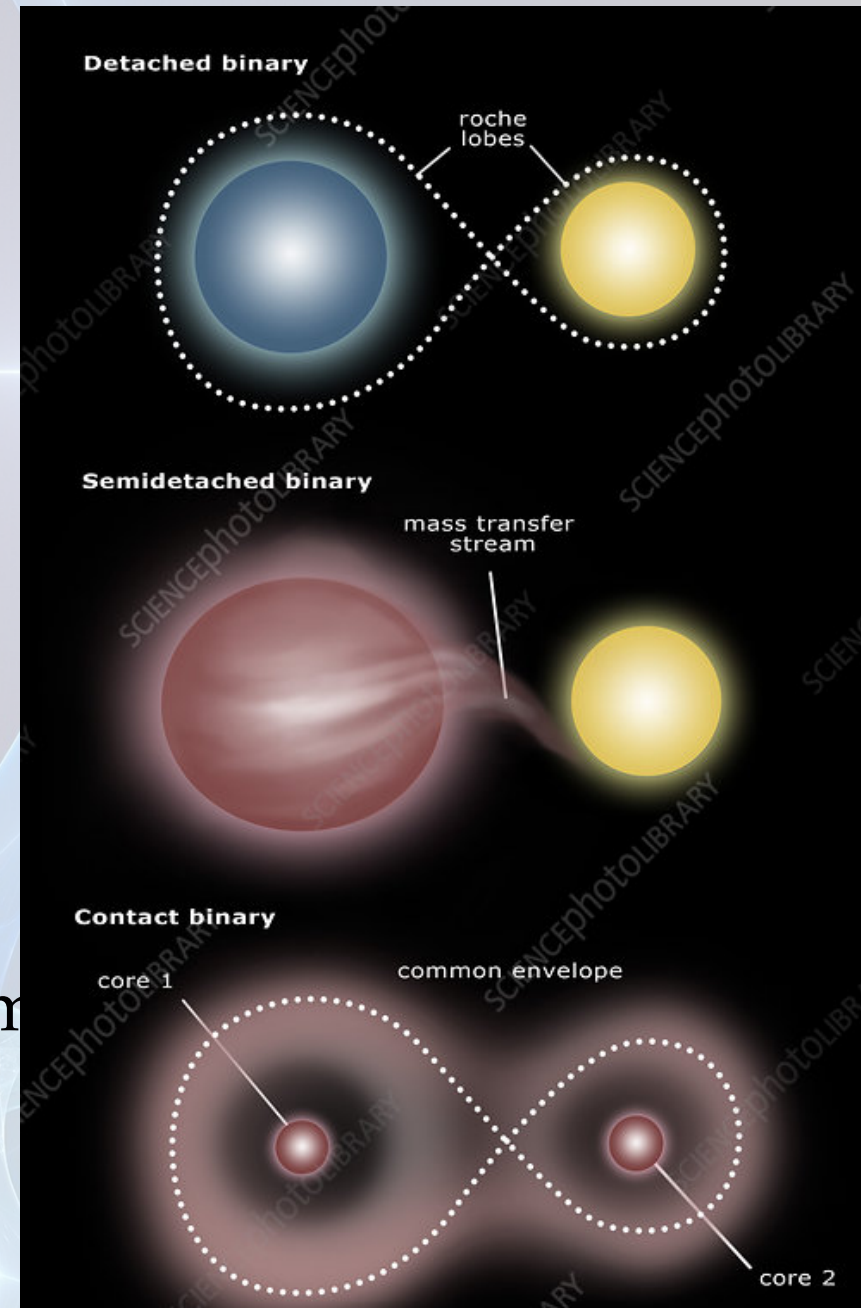
Two of them next to each other:



- $\tau(m) \sim m^{-2.5}$
 - Sun's lifetime: $\sim 10^{10}$ yrs
 - an $8 M_{\odot}$ star's lifetime: $\sim 5 \times 10^7$ yrs
 - a $100 M_{\odot}$ star's lifetime: $\sim 2 \times 10^6$ yrs

Why does the Roche-lobe matter?

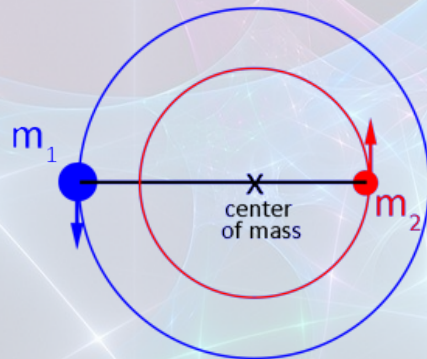
- Mass transfer.
- Some important terms:
 - primary/secondary (companions)
 - donor/accretor **mass gainer**
 - M_1/M_2 losing mass / gaining mass
 - detached system
 - Roche-lobe overflow
 - semi-detached, contact system
 - ‘common envelope’ (...)
 - ▶ *stellar envelope*



Some more terms

- orbital separation = orb. distance
- period = orbital period
 - \neq rotational period!!
(though cf. *synchronization*)
e.g. due to tidal forces
- initial orbital separation *vs.* actual
- initial period *vs.* actual
- Connection between distance & period?

Kepler's 3rd law:



$$P^2 = \frac{4\pi^2}{G(M_1 + M_2)} r^3$$

'Case A', 'Case B', 'Case C' mass transfer

- Historical categorization (cf. stellar classes O, B, A, F... or supernova classification type Ia, Ib, II...) – **useful to know**
even if its getting outdated

- case A: MS
- case B: HG
- case C: He-b.
(donor's evolutionary status)

MS = Main Sequence
HG = Hertzsprung-gap
He-b. = helium-burning

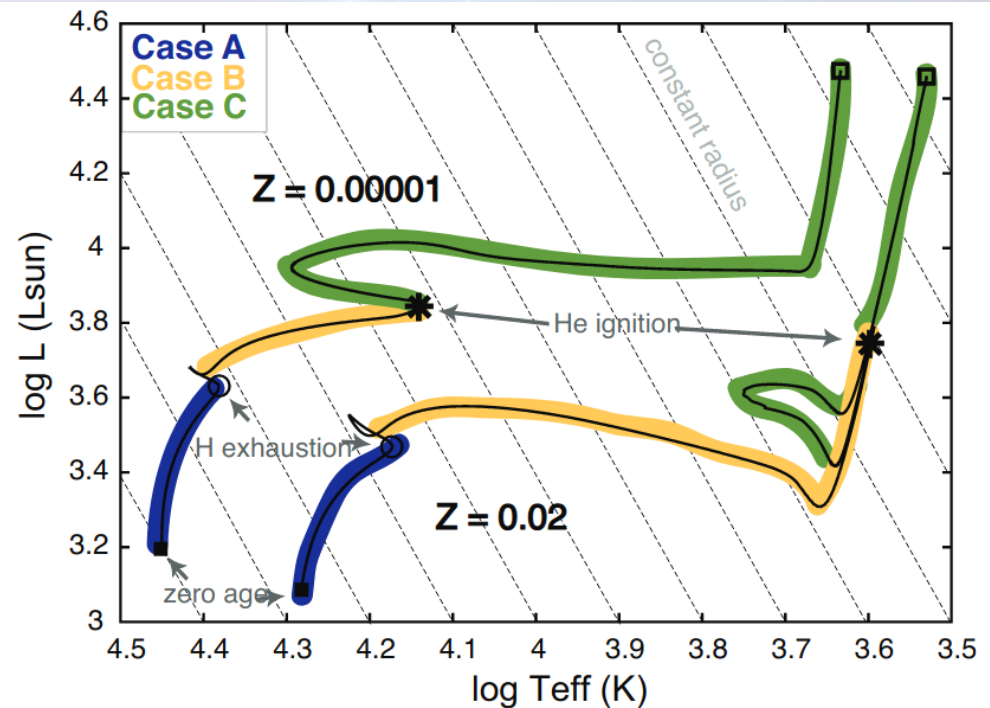


Figure 1.1: Evolutionary tracks in the HR-diagram of a $6 M_{\odot}$ star illustrating the effect of metallicity on the occurrence of the different cases of mass transfer. The dashed diagonal lines indicate lines of constant radii. Cases A, B and C are defined in the text of Section 1.5.1. Figure adapted from De Mink et al. (2008b).

Orbital evolution during mass transfer

- suppose conservative mass transfer:
 - orbit shrinks if $M_{\text{donor}} > M_{\text{acc}}$
 - orbit expands if $M_{\text{donor}} < M_{\text{acc}}$
- if the mass transfer is non-conservative:
 - then we also need to take into account how much angular momentum is lost from the system...

cf. prof. Onno Pols'
lecture notes on binaries
[\[LINK\]](#)

- Roche-lobe is effected:

⇒ approximation of Roche lobe
(Eggleton 1983) $q = m_1/m_2$

- And remember:
massive stars have
WINDS...

and winds carry away ang.mom. too

$$RL_1 = A \frac{0.49 q^{2/3}}{0.6 q^{2/3} + \ln(1 + q^{1/3})}$$

orbital separation: A

What happens to the donor after losing layers?

- Can the donor regain its stability after RLOF?
 - if yes: *stable* mass transfer – or detachment (depending also on RL-evolution)
 - if no: *unstable* mass transfer (🙄)
- Stable mass transfer:
 - donor remains in thermal equilibrium while continuing mass transfer driven by stellar evolution related expansion (or by orbital shrinkage due to ang. mom. loss)
 - donor does not remain in thermal eq. but the mass transfer may still be stable, driven (self-regulatingly) by thermal readjustment of the donor

hardcore
stuff

$$\tau_{\text{nuc}} \gg \tau_{\text{KH}} \gg \tau_{\text{dyn}}$$

What happens to the donor after losing layers?

- Can the donor regain its stability after RLOF?
 - if yes: *stable* mass transfer – or detachment (depending also on RL-evolution)
 - if no: *unstable* mass transfer

- Stable mass transfer:

- donor remains in thermal equilibrium while continuing mass transfer related expansion (or by ...)

Detailed calculations show that stars with **radiative envelopes** shrink rapidly (τ_{dyn}) in response to mass loss, while stars with **convective envelopes** tend to expand or keep a roughly constant radius (τ_{KH}).

hardcore stuff

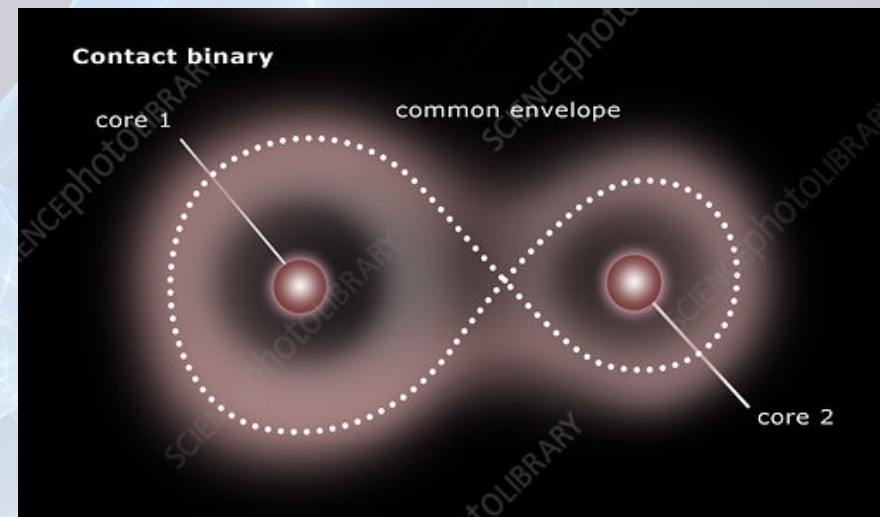
$$\tau_{\text{nuc}} \gg \tau_{\text{KH}} \gg \tau_{\text{dyn}}$$

Unstable mass-transfer

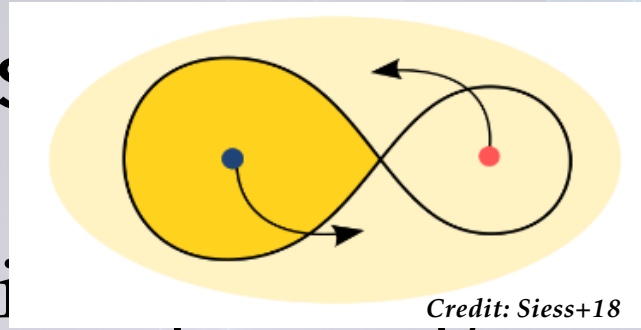


- if the donor is expanding too quickly (τ_{dyn}) and thus cannot stay within its Roche lobe: ever-increasing mass-transfer rates
- this is an unstable, runaway situation secondary cannot accrete fast enough
- has dramatic effects: “common envelope” situation

$$\tau_{\text{nuc}} \gg \tau_{\text{KH}} \gg \tau_{\text{dyn}}$$

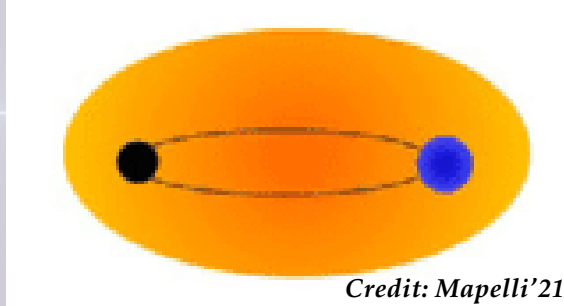


Unstable mass-transfer



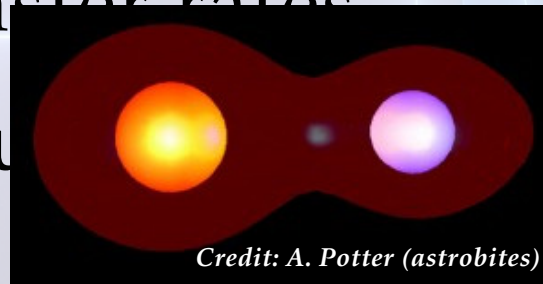
Credit: Siess+18

- if the donor is rotating quickly ($\tau_{rot} \ll \tau_{KH}$) and thus cannot stay within its Roche lobe:

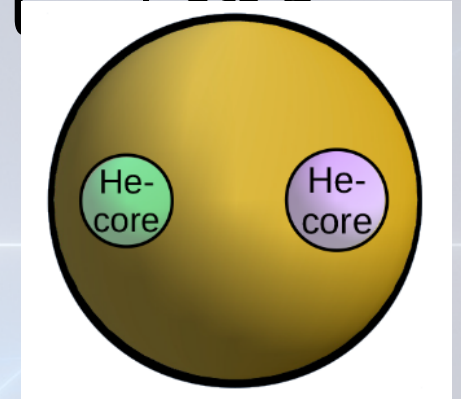


Credit: Mapelli'21

- mass-transfer rates



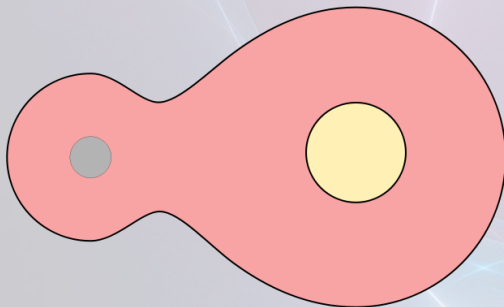
Credit: A. Potter (astrobit.es)



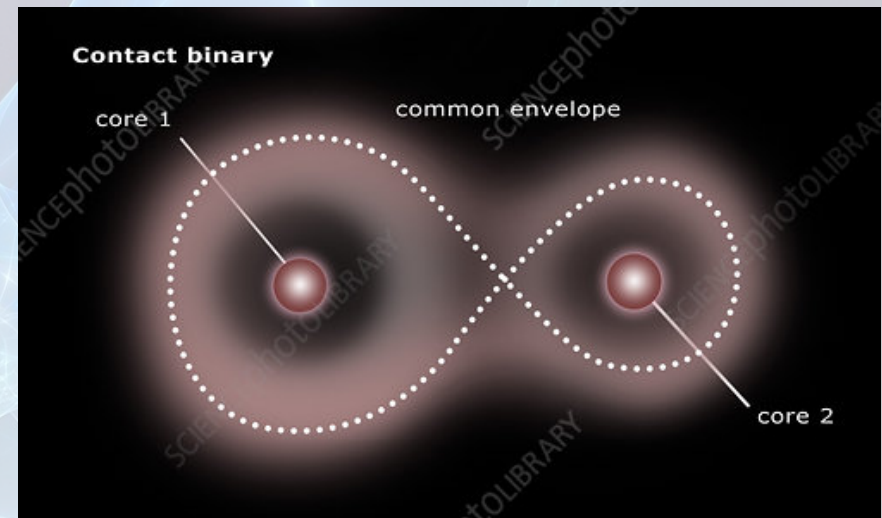
Credit: Yours Truly ;) [Vigna-Gomez+18]

- are comparable, run on

- has dramatic effects: “common envelope” situation



Credit: Wikipedia



$$\tau_{nuc} \gg \tau_{KH} \gg \tau_{dyn}$$

What we know about CE

- short lived phase
 - observed?? how??

Movies :)

Passy+12:
0.88 M_⊙ (RG)
+ 0.15 M_⊙
companion

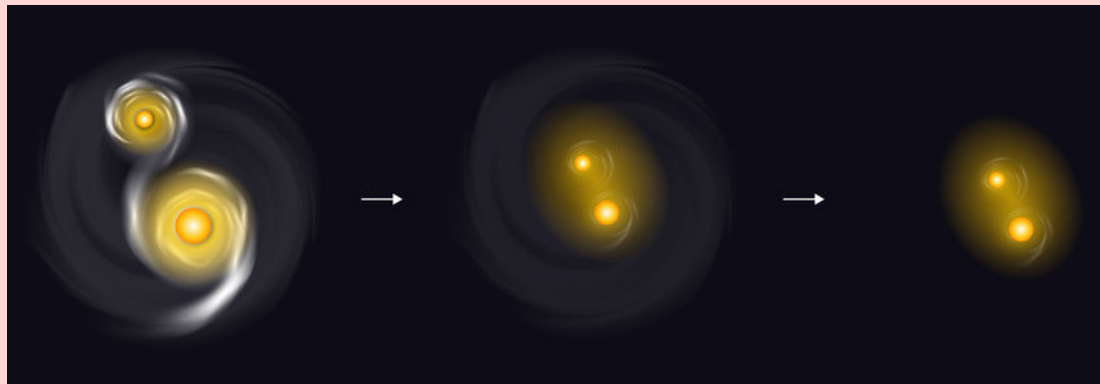
Moreno+21:
10 M_⊙ (RSG) +
BH
companion

- but it probably occurs
 - explaining close white dwarf-binaries
(WD=ex-Red Giant: no other way to get that close)
- 3D simulations are still very expensive
 - in practice: derived relations between
orbital energy & binding energy of the envelope
- Result: envelope is (probably?) ejected due to friction. (If not: merger. *No GW possible.*)
of the two stellar cores

What we know about CE

**Leads to the 'hardening'
(=shrinking) of the orbit.**

(If the system survives, and not merge.)



Credit: MPIA

result: envelope is (probably?) ejected due to
interaction. (If not: merger. *No GW possible.*)
of the two stellar cores

Let's play!

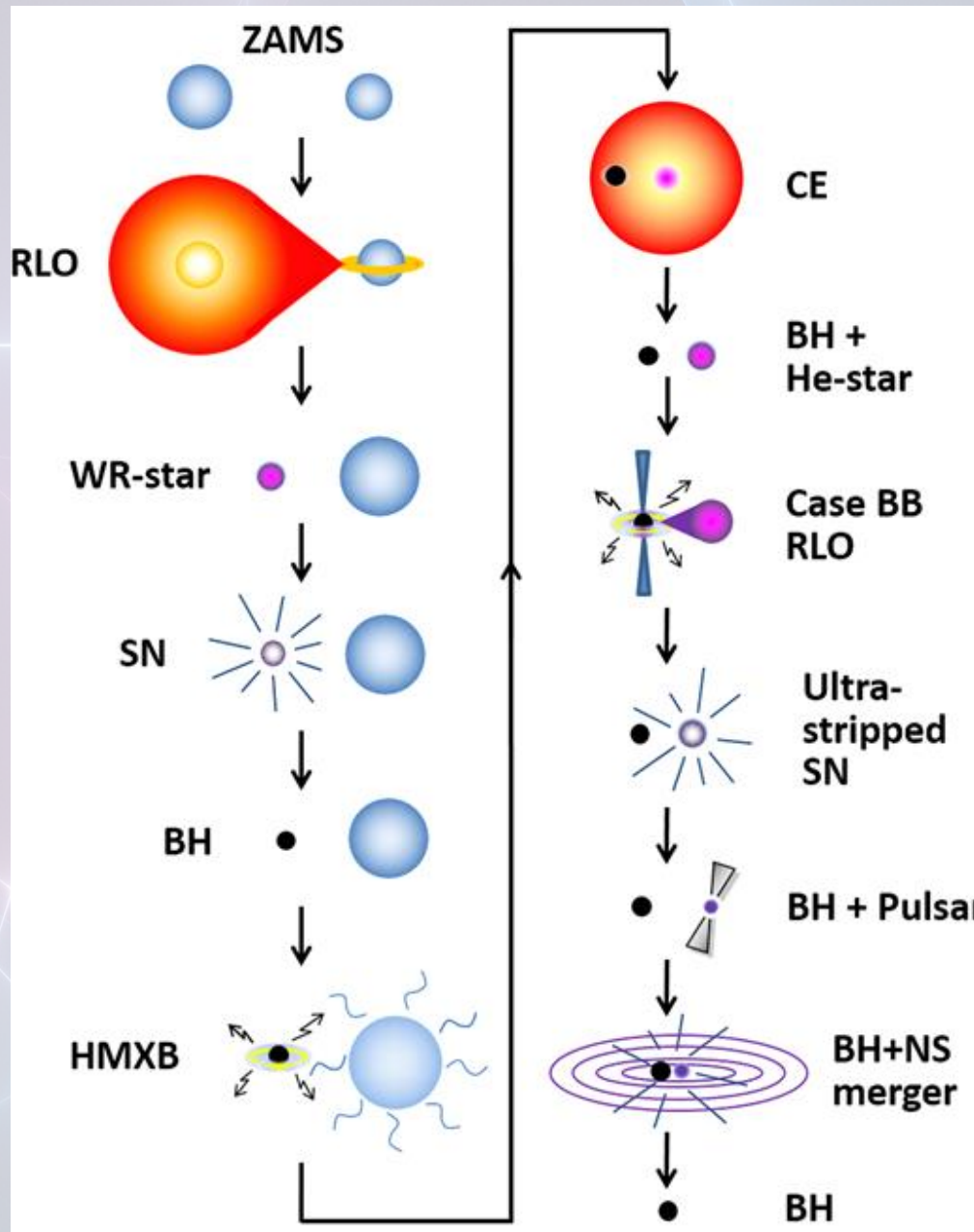
Zero-age Main Seq.

Roche-lobe overflow:
stable mass transfer

Wolf-Rayet star
(naked He-star with
strong emission lines)

Supernova may kick out
the companion! Survival
rate?

Accreting black hole:
High-Mass X-ray Binary
(observed: periodic
pulsations in X-rays)



Common Envelope!



Probably a HMXB?

Stripped = type Ib
Ultra-stripped = type Ic

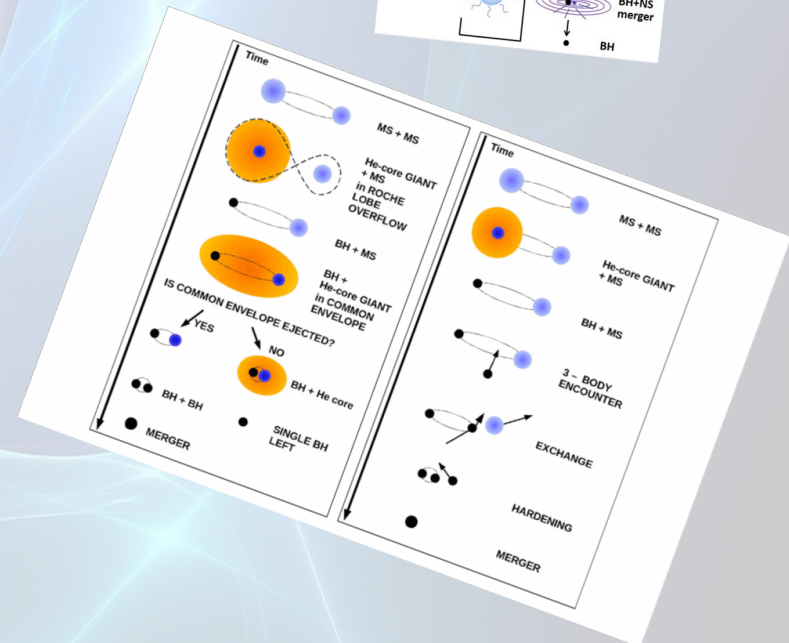
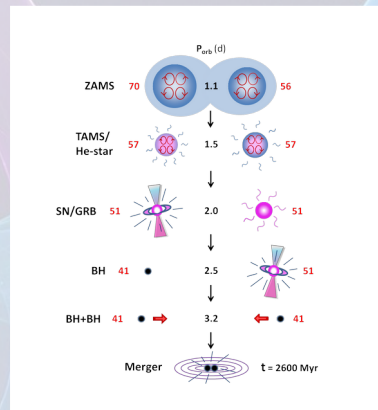
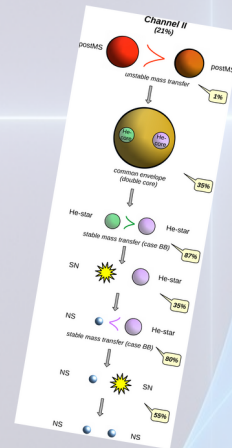
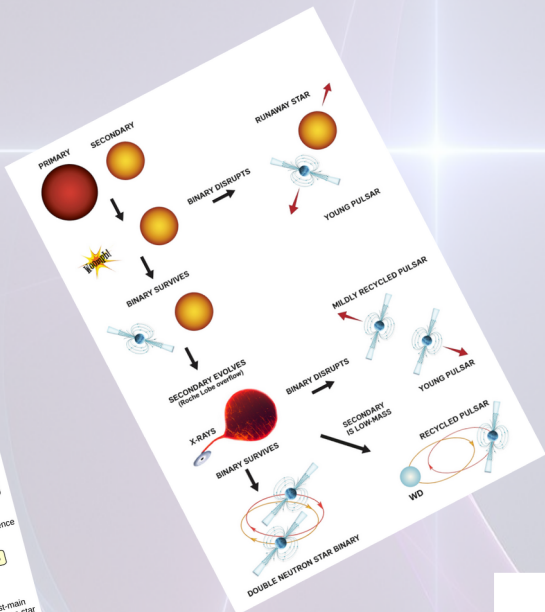
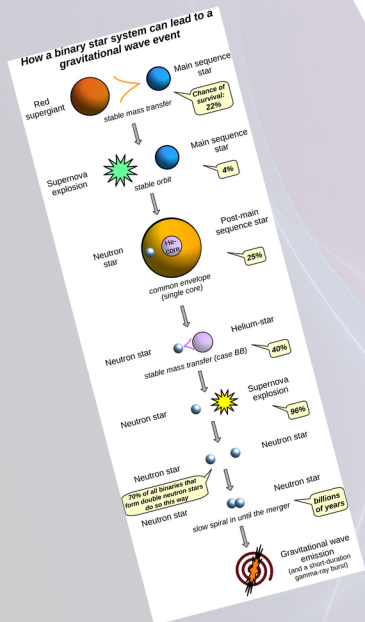
(Pulsar: a rotating,
magnetized neutron star)

GRAV. WAVES!!!

Credit: Kruckow+18

Possible exam question ;)

- explain a binary evolution cartoon scientifically!

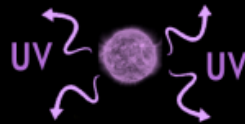


- sub-Solar metallicities? ✓
- fast-rotating stars? ✓
- stars in a binary system? ✓

*What about a metal-poor,
fast rotating binary system?*

*Chemically-homoge-
neously evolving star:*

single

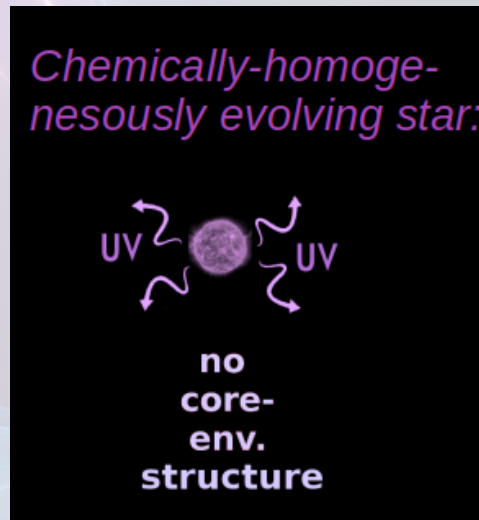


no
core-
env.
structure

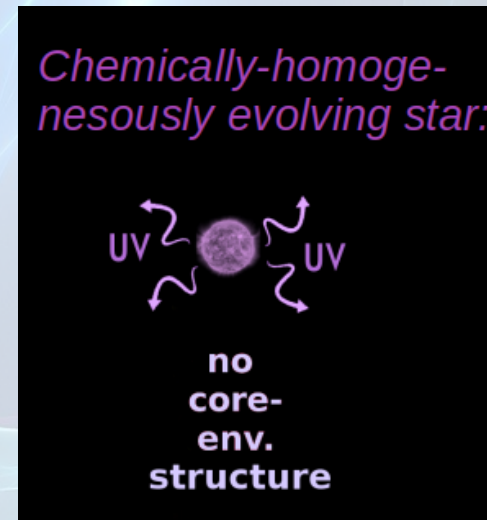
- sub-Solar metallicities? ✓
- fast-rotating stars? ✓
- stars in a binary system? ✓

*What about a metal-poor,
fast rotating binary system?*

Let's put two
of them next
to each other
on a (very) close
orbit!

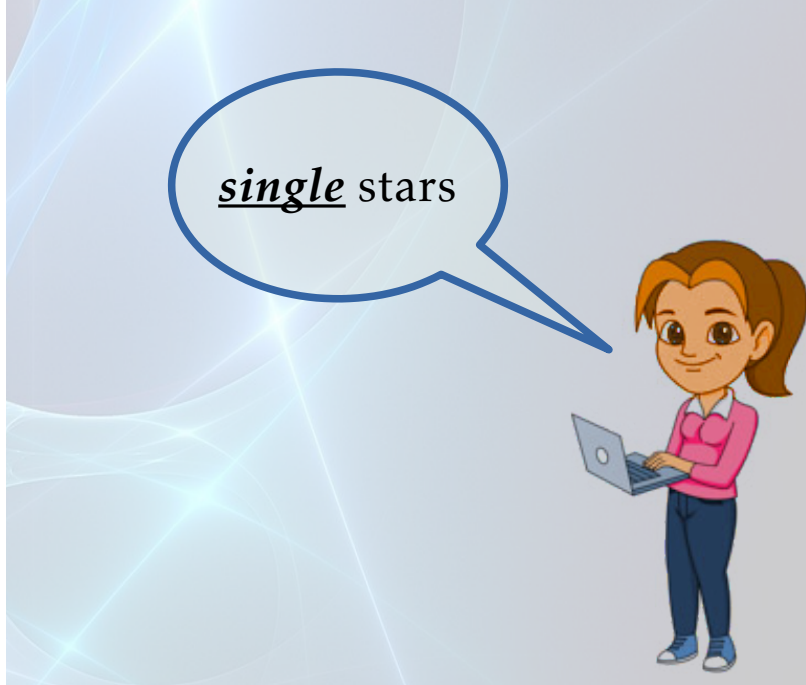
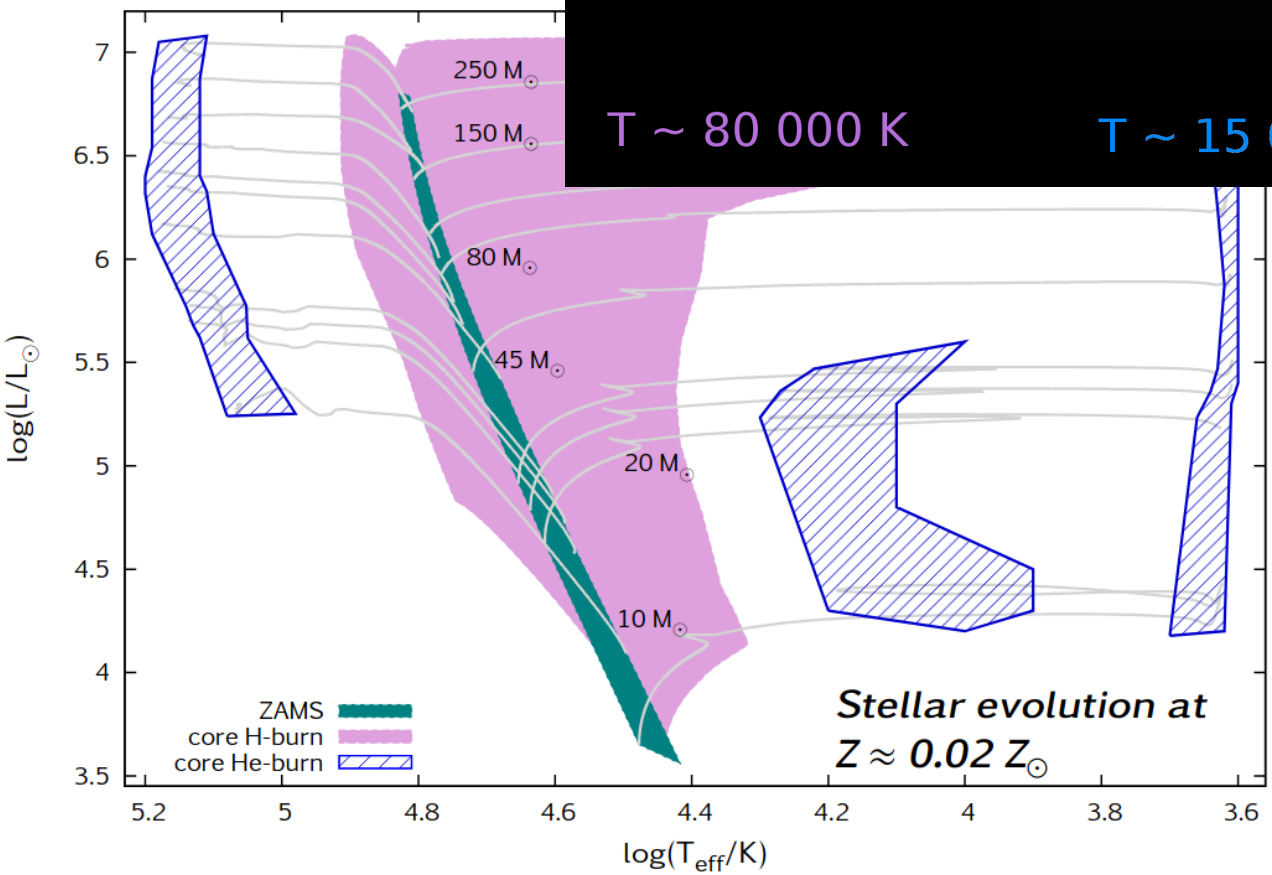
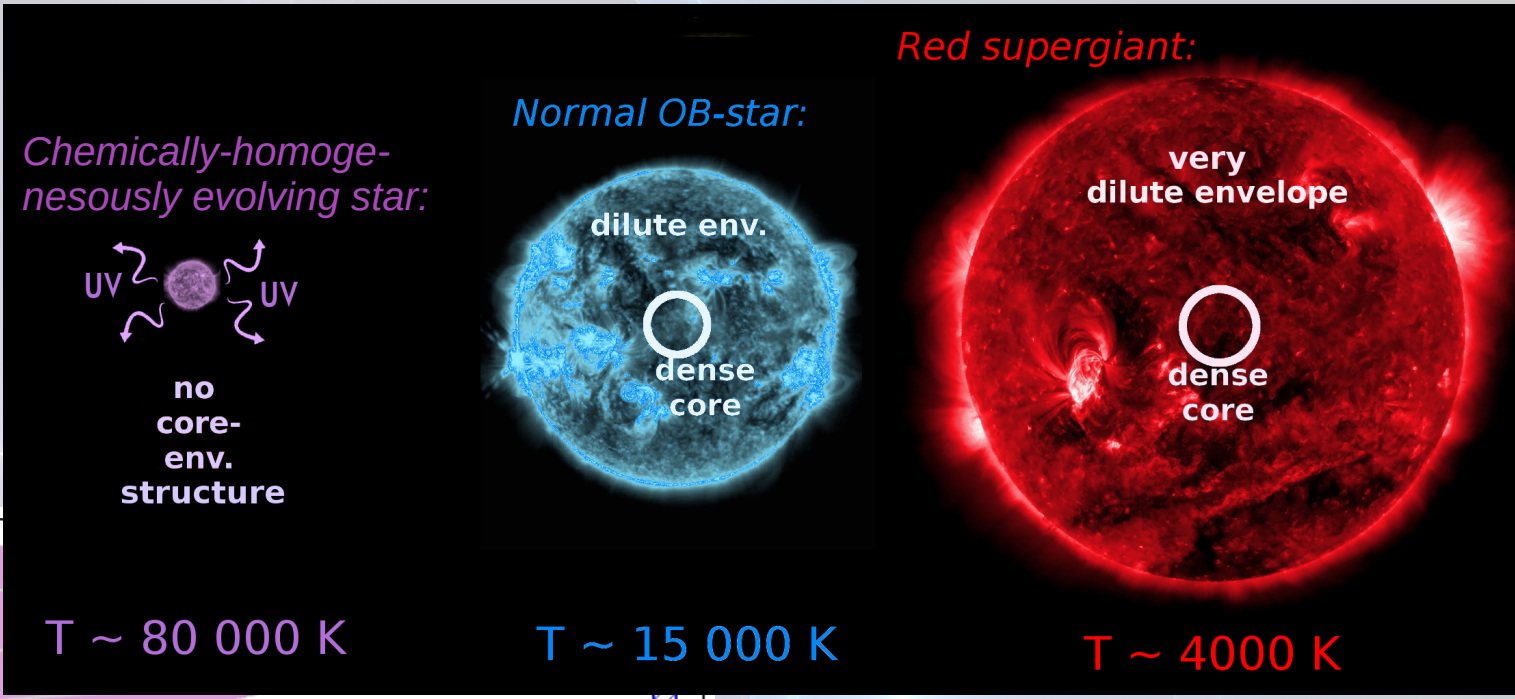


+

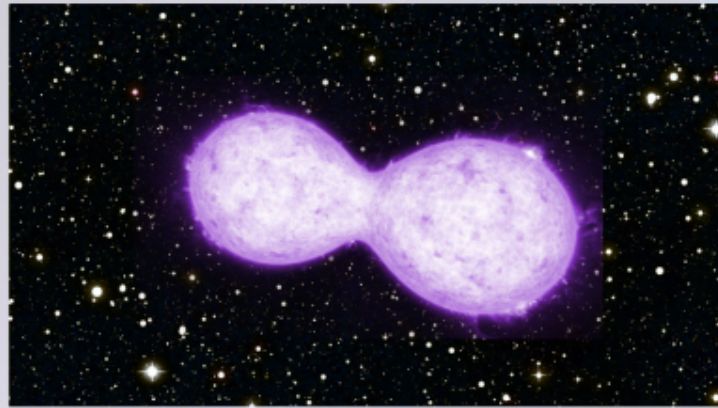


= ?

What do chem.hom. evolving stars look like?



Gravitational waves... theoretical origin!



e.g. [Szécsi'17a](#)

[Szécsi'17b](#)

Bagoly,[Szécsi+16](#)

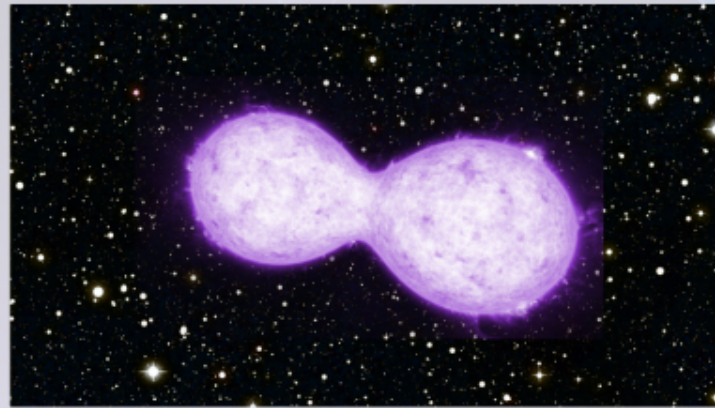
Marchant+16,17

Gravitational waves... theoretical origin!

Life

Death

Afterlife



Massive binaries

Explosions

2 Black Holes
(or Neutron Stars)



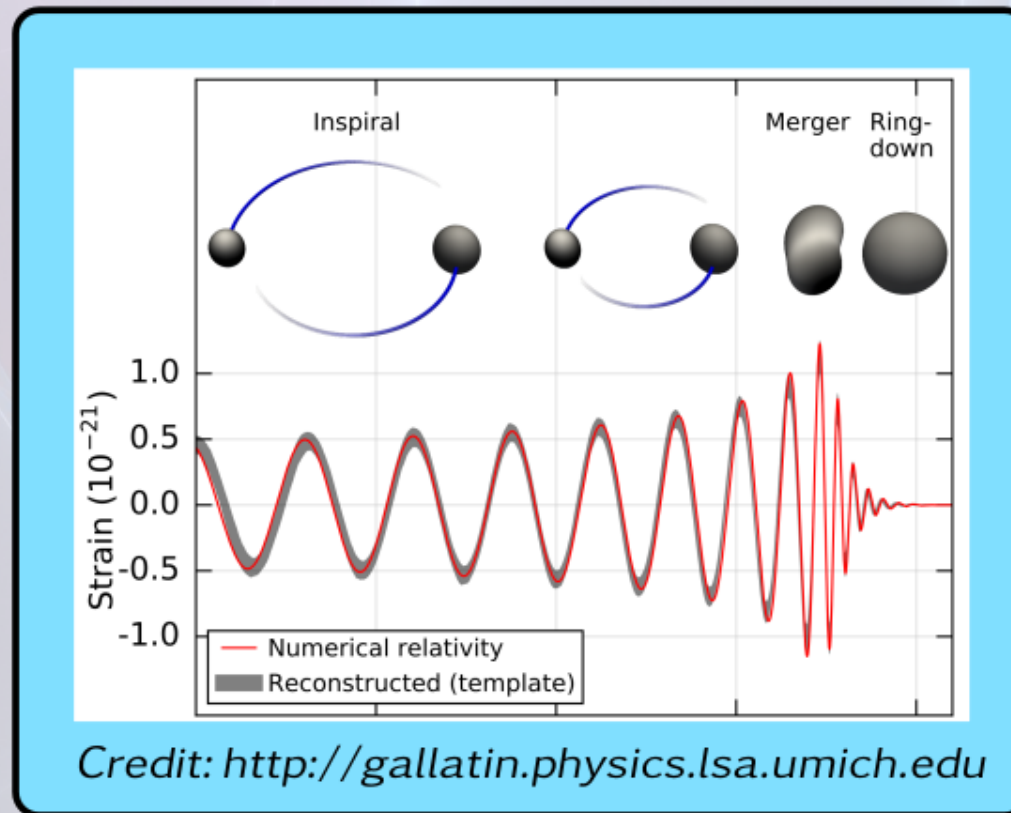
'Second
death'

e.g. [Szécsi'17a](#)

[Szécsi'17b](#)

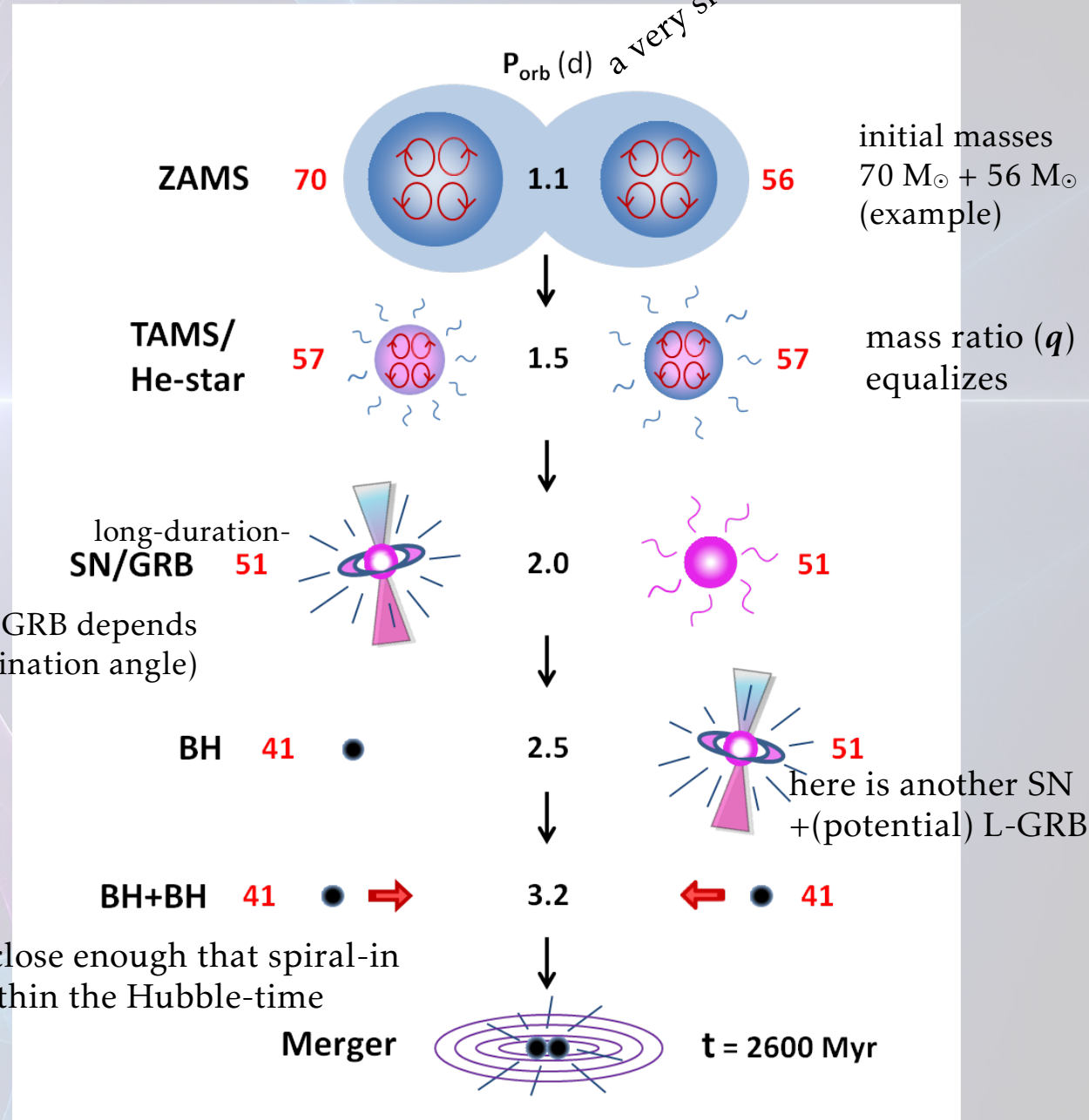
Bagoly,[Szécsi+16](#)

Marchant+16,17



Merger

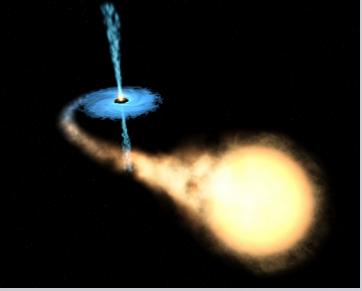
To "cartoonize" the scenario:



Remember: to see a GRB, we need to look right into the jet!

system is still close enough that spiral-in can happen within the Hubble-time

Credit: Marchant+16



HMXB = High-mass X-ray binary

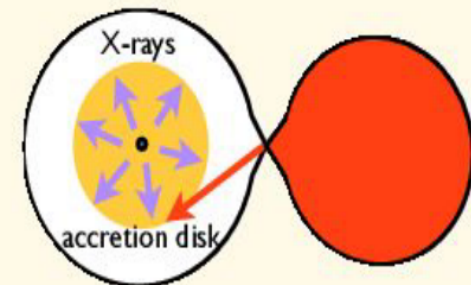
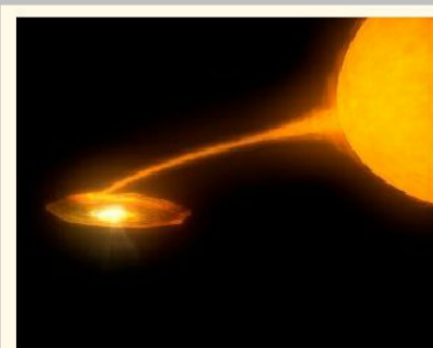
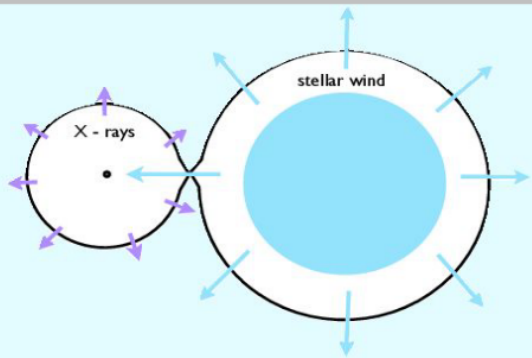
Observed:
~ 200 LMXB in the MW
some more in other gals.
> 100 HMXB in MW
e.g. *Cygnus X-1*

- sister object: LMXB = Low-mass X-ray binary
- X-rays are produced by the matter falling from the (stellar) companion to the NS or BH
 - if the companion is a low-mass star (or a WD): LMXB
 - if it's a massive star: HMXB
- Massive stars have strong winds! It contributes.

*periodic
X-ray pulses*

HMXB's

LMXB's

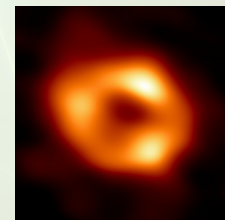


Credit: Palit 2020

Microquasars

- basically HMXBs which also emit in radio
 - the source of the radio emission is two jets* (*see next slide)
 - Cygnus-X1 is also a microquasar

- name comes from ‘quasars’ also known as ‘quasi-stellar object’ (QSO)
 - discovered in the 50s as radio sources of unknown origin
 - *galaxies where the central BH eats up the stars...*
 - → active galactic nucleus (AGN)
 - powered by a *supermassive* BH ($\geq 10^6 - 10^9 M_{\odot}$)
(as opposed to a *stellar mass* BH as in a HMXB/microquasar)
 - **THIS WEEK'S MOST EXCITING NEWS!!**
Capturing our MW's central BH by the
"Event Horizon Telescope" (not a real telescope;
but a collaboration of radio observatories & clever data reduction techniques :D)



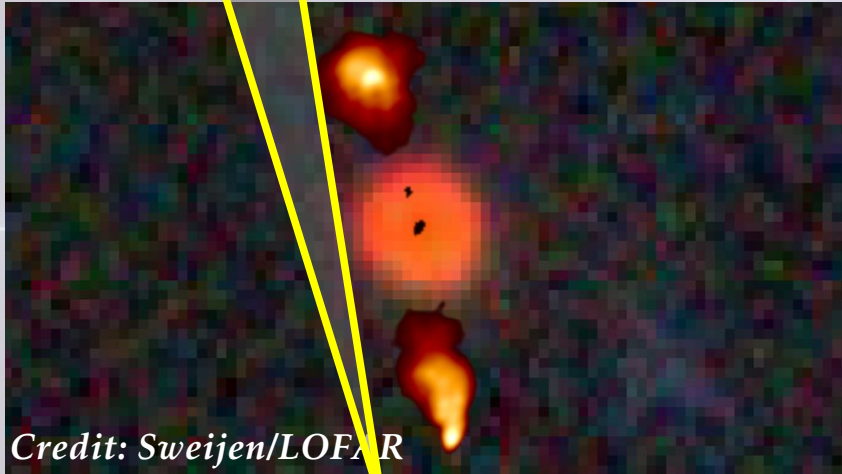
Sgr A*
 $4 \times 10^6 M_{\odot}$

not a very
active
nucleus
(fortunately)

Jets (in astronomy)

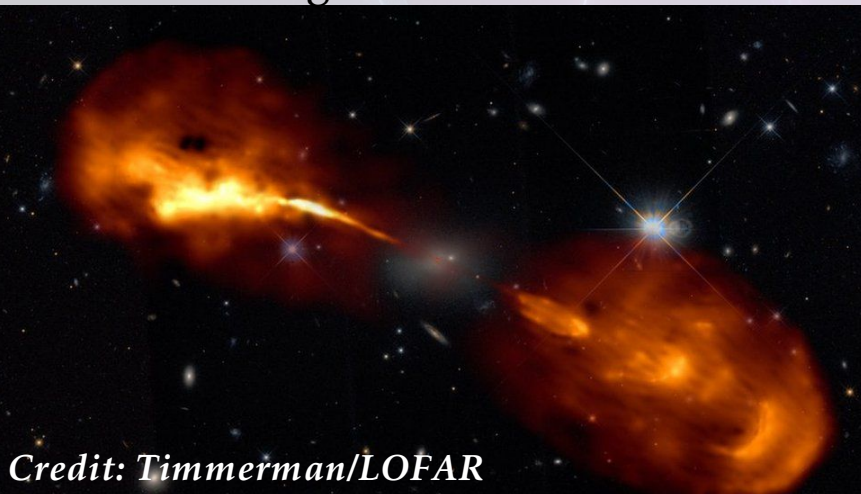
And also
microquasars,
of course.

Actual observation (2021, LOFAR):



AGNs

Artistic image of the same stuff:



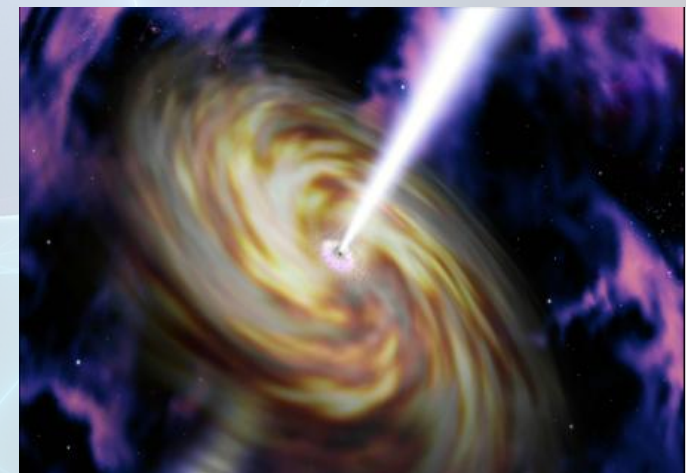
??

spectral features (breaking)
high energies cannot be explained otherwise

short-living

GRBs

Artistic image:

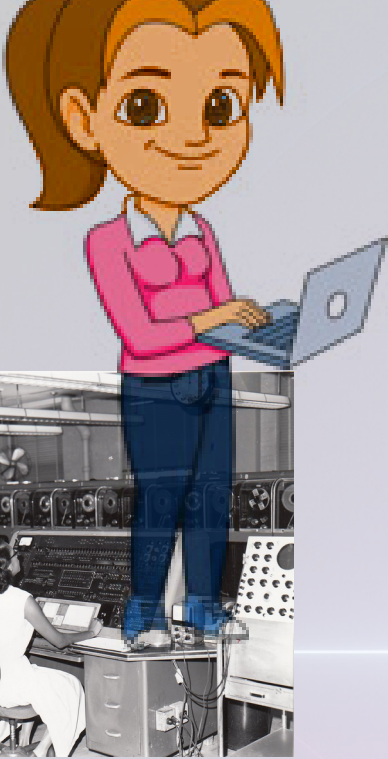


long-living

(timescales
are proportional
to the mass
of the central BH)

The background features a large, faint circle in the center. Overlaid on this are numerous thin, glowing lines in shades of blue, cyan, and magenta. These lines form a complex, web-like pattern that resembles a fractal or a network diagram. The lines are most concentrated in the lower half of the image, where they form a dense, star-like structure. The overall effect is a soft, ethereal glow against a light gray background.

*From individual systems
to
populations*



HR-diagram



Age, Mass, Radius, T_{eff} [K], $\log(L/L_{\odot})$, Massloss rate...



```

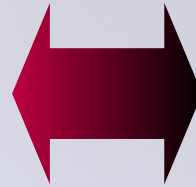
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6# -----
7#      initial mass  N_pts  N_EEP  N_col  phase  type
8# 1.9999727046E+01  808     8     73    YES   high-mass
9# EEPs:      1     202    353    454    605    631    707    808
10# -----
11#              1              2              3              4              5
12#              star_age      star mass      star mdot      log dt      he_core mass
13# 2.7320575584293762E+005    1.9999727045763130E+001    -6.6667141481350412E-009    4.6121780058570057E+000    0.0000000000000000E+000
14# 2.7345019073205121E+005    1.9999725407394834E+001    -6.6668930715861210E-009    4.6125719424045064E+000    0.0000000000000000E+000
15# 2.7369462562116480E+005    1.9999723769026541E+001    -6.6670719950372001E-009    4.6129658789520063E+000    0.0000000000000000E+000
16# 2.7393906051027833E+005    1.9999722130658245E+001    -6.6672509184882791E-009    4.6133598154995070E+000    0.0000000000000000E+000
17# 2.7418349539939192E+005    1.9999720492289949E+001    -6.6674298419393581E-009    4.6137537520470087E+000    0.0000000000000000E+000
18# 2.7442793028850551E+005    1.9999718853921653E+001    -6.6676087653904380E-009    4.6141476885945094E+000    0.0000000000000000E+000
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```

IMPORTANT . . .

Exam
warning!
:P

- Stellar evolution modelling



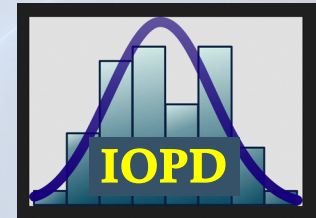
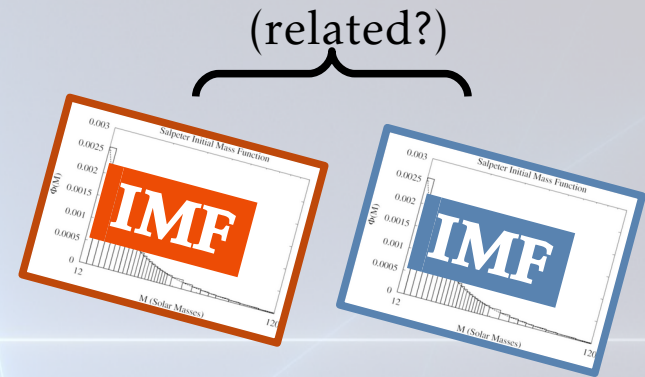
- Synthetic population modelling

- based on first principles
(5 stellar equations)
- follows one star's life at the time
- IMF is not yet considered
- result is *a line* ('track') in the HR-diagram

- relies on stellar evolution modelling
- does not simulate the individual star's life (typically)
- IMF is taken into account
- result is a *statistically meaningful* prediction about a *population*

Population synthesis on *binaries*

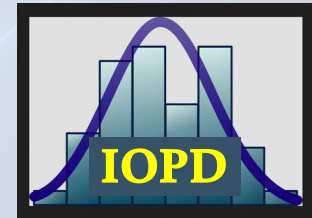
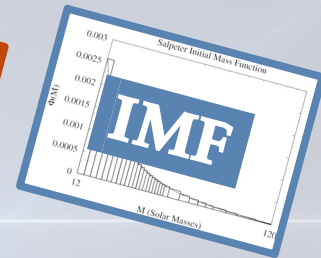
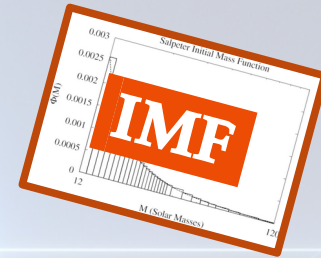
- 2 stars instead of 1
 - both have their individual IMFs
- orbital separation!
 - Initial Orbital Period Distribution
same kind of thing as the IMF but for the period, i.e. an observation-based statistical distribution
- plus a *lot* of assumptions about the evolution
 - mass transfer (stable/unstable? conservative/non-conservative? ...)
 - Common Envelope phase (outcome: merger or survival?
separation afterwards?)
 - supernova physics... and the kick.



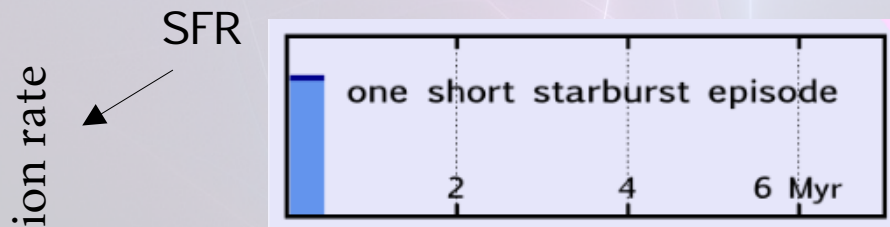
on top of what we already don't know about *single stars'* evolution

Star-formation history

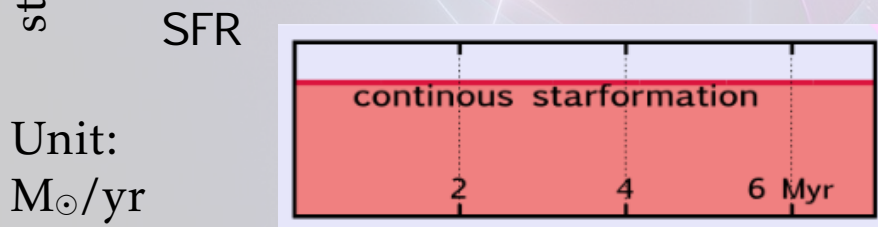
- We need to know the *history* of how the stars are being born...



Not enough!



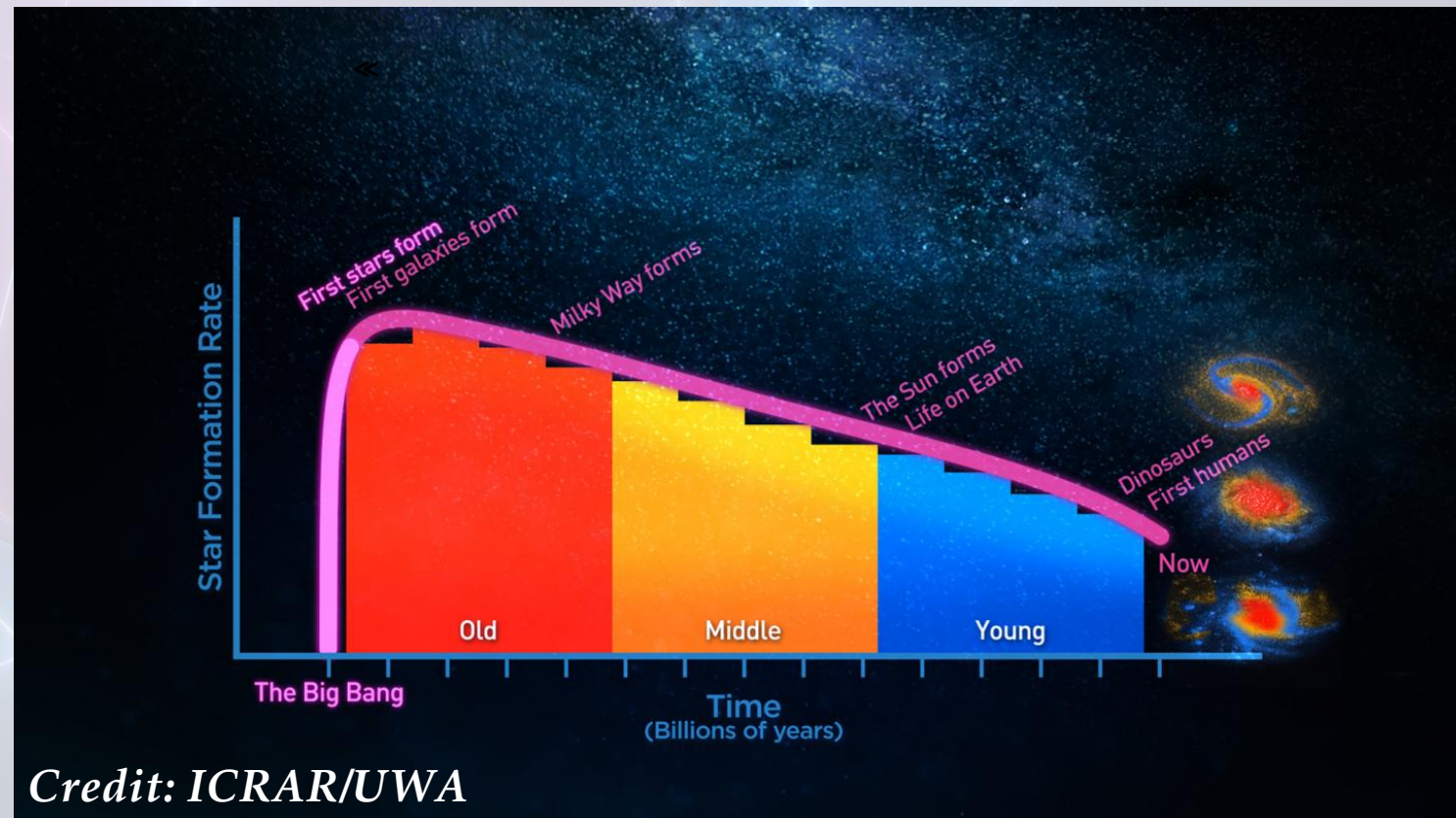
or anything else



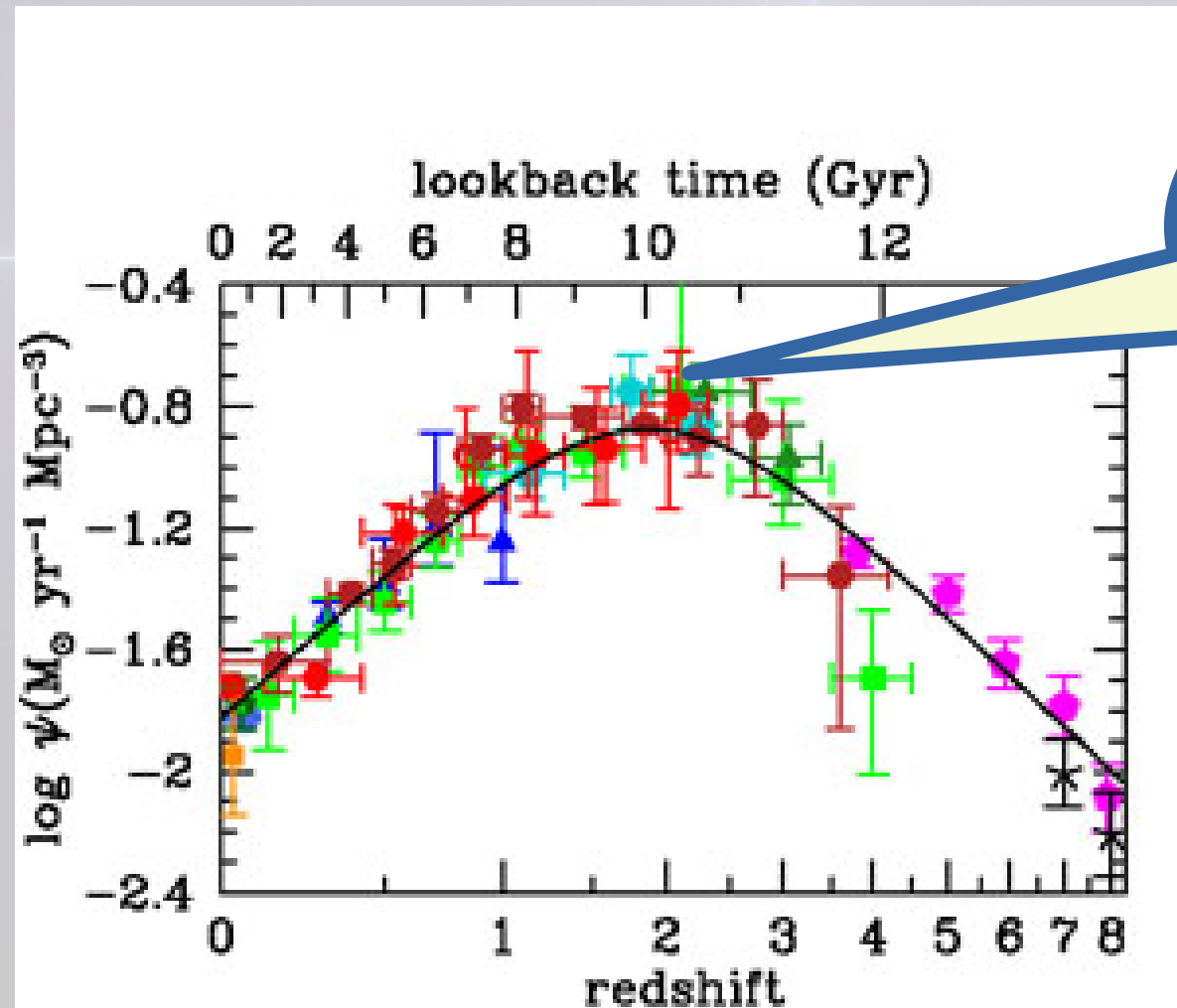
We need all these to do
(binary) population synthesis.

From star-formation history to *cosmic* star-formation history

- This is what we need to predict GW-event rates from synthetic populations



From star-formation history to *cosmic* star-formation history



Peaking: somewhere around $z = 2$, when the Universe was ~ 3.5 Gyr old

Note:
massive stars live short lives!
 $2\text{-}20 \text{ Myr} \ll 13 \text{ Gyr}$

Credit: Madau & Dickinson (2014)

Now we can answer the original *(kind of)* question of this whole lecture series

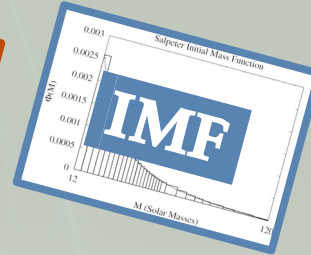
stellar models

```

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2# MESA revision number = 11701
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4# Yinit  Zinit  [Fe/H]  [alpha/Fe]  v/crit
5# 0.2511  1.42857E-03  1.00  0.00  0.00
6# .....
7# initial mass  N_pts  N_EEP  N_col  phase  type
8# 1.9999727046E+01  808  8  73  YES  high-mass
9# EEPs: 1 202 353 454 665 631 707 808
10# .....
11# .....
12# 1 star age 2 star mass 3 star mdot 4 log dt 5 he core mass
13# 2.732857584293762E+005 1.9999727045763130E+001 -6.6668939715061210E-009 4.6121780058570057E+000 0.000000000000000E+000
14# 2.7345019072051121E+005 1.9999725407394030E+001 -6.6668939715061210E-009 4.6125719424945504E+000 0.000000000000000E+000
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17# 2.7418349539039192E+005 1.9999725407394030E+001 -6.6668939715061210E-009 4.6125719424945504E+000 0.000000000000000E+000
18# 2.744279302885051E+005 1.9999725407394030E+001 -6.6668939715061210E-009 4.6125719424945504E+000 0.000000000000000E+000
19# 2.7467236517761904E+005 1.9999725407394030E+001 -6.6668939715061210E-009 4.6125719424945504E+000 0.000000000000000E+000
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24# 2.7589453962318092E+005 1.9999725407394030E+001 -6.6668939715061210E-009 4.6125719424945504E+000 0.000000000000000E+000
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27# 2.7662784429825763E+005 1.9999725407394030E+001 -6.6668939715061210E-009 4.6125719424945504E+000 0.000000000000000E+000
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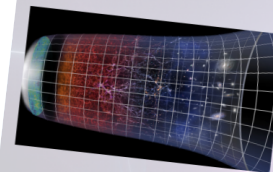
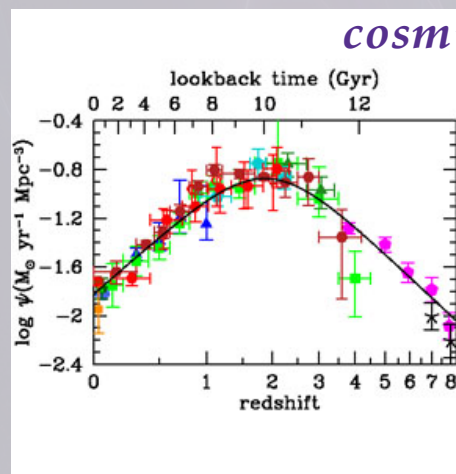


initial distributions



+ a lot of assumptions about binary physics

cosmic SFH



? How many GW events happen **IN THE UNIVERSE** (per year)?



a star-cluster or galaxy: one star-formation event of size (e.g.) $10^7 M_{\odot}$
aLIGO/Virgo detectors observe GWs from the whole Universe...

Now we can answer the original *(kind of)* question of this whole lecture series

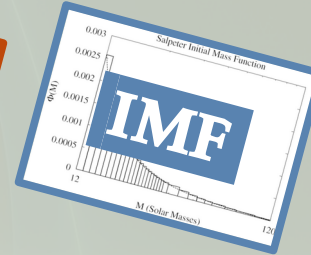
stellar models

```

1# MST version number = 10.1
2# MESA revision number = 11701
3# -----
4# Yinit  Zinit  [Fe/H]  [alpha/Fe]  v/crit
5# 0.2511  1.42857E-03  1.00  0.00  0.00
6# -----
7# initial mass  N_pts  N_EEP  N_col  phase  type
8# 1.9999727046E+01  800  8  73  YES  high-mass
9# EEPs: 1 202 353 454 605 631 707 800
10# -----
11# -----
12# 1 2 3 4 5
13# star age star mass star mdot log dt he core mass
14# 2.732857584293762E+005 1.9999727045763130E+001 -6.6667141481350412E-009 4.6121780058570057E+000 0.000000000000000E+000
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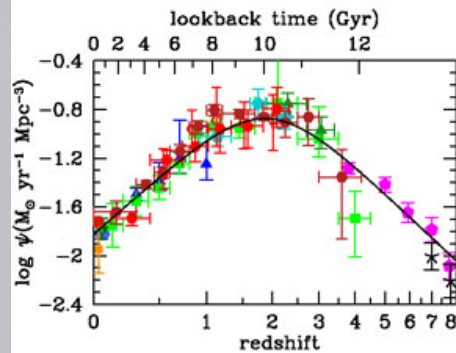


initial distributions



+ a lot of assumptions about binary physics

cosmic SFH

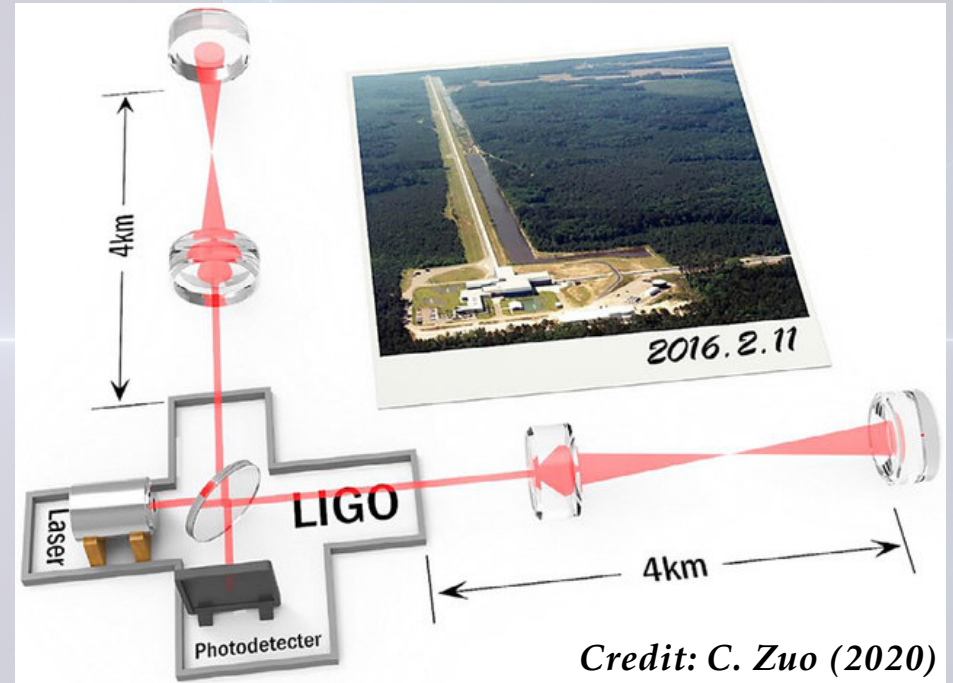


Important piece of math:
Convolution
of two functions

$$(f * g)(t) := \int_{-\infty}^{\infty} f(\tau)g(t - \tau) d\tau.$$

And some names you MUST know

- LIGO:
 - Laser Interferometer Gravitational-wave Observatory (USA)
- **aLIGO**
 - advanced LIGO
 - the current version
- **Virgo**
 - LIGO's important little sister in Europe



The Einstein equations are canonical 2

Einstein equation!

$$\underbrace{G(g)} = 8\pi T(g)$$
$$R_{ab} - \frac{1}{2}S \cdot g_{ab} + \cancel{\Lambda} \cdot g_{ab} = 8\pi T_{ab}.$$

- Based on experience in physics, we want to have a differential equation, thus $\alpha \neq 0$ and we can assume $\alpha = 1$ by rescaling.
- The constant turns out to be 8π in our system of units.
- For the sake of simplicity, we will take $\Lambda = 0$ in this lecture.
- We have seen that the Ricci tensor tells us how the volumes change, which plays nicely with the interpretation of curvature as gravity.

Linearization

This is where the linearized theory comes into play: suppose we have a “background” solution g_{ab} of the full Einstein equation

$$G(g) = 8\pi T(g)$$

and look for solutions of the form

$$g_{ab} + \epsilon h_{ab}$$

where h_{ab} is a symmetric tensor.

$$G(g) + \epsilon \cdot \frac{d}{d\epsilon} \Big|_{\epsilon=0} G(g + \epsilon h) + O(\epsilon^2) = 8\pi T(g) + \epsilon \cdot 8\pi \cdot \frac{d}{d\epsilon} \Big|_{\epsilon=0} T(g + \epsilon h) + O(\epsilon^2)$$

Plane waves

- Plane wave ansatz:

$$\bar{h}_{ab} = A_{ab} \cos(k_m x^m)$$

constant matrix of amplitudes

wave number vector

- This is a single Fourier mode
- Divergence-freeness implies $k^a A_{ab} = 0$.

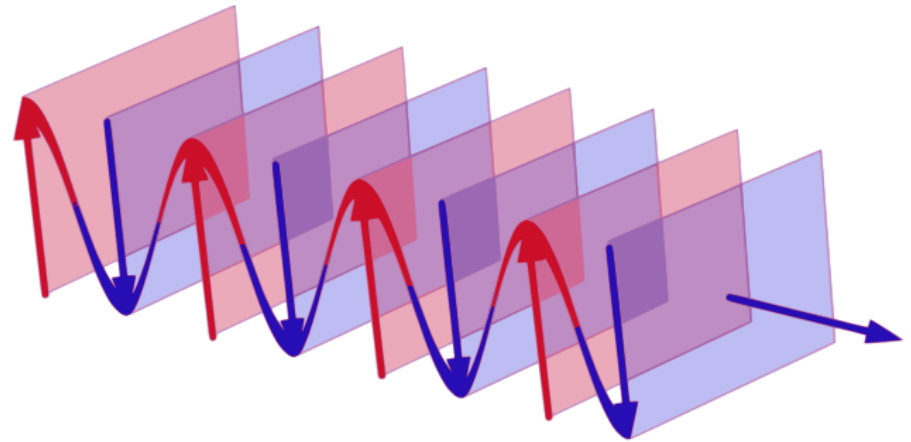


Image credit Wikipedia user Constant314

Our plane wave has only two degrees of freedom

Next suppose we orient our spatial coordinate axes so that the wave is travelling in the positive z -direction, i.e.

$$k^t = \omega, \quad k^x = k^y = 0, \quad k^z = \omega$$

and

$$k_t = -\omega, \quad k_x = k_y = 0, \quad k_z = \omega$$

Then $A_{az} = 0$ for all a .

All in all, we obtain

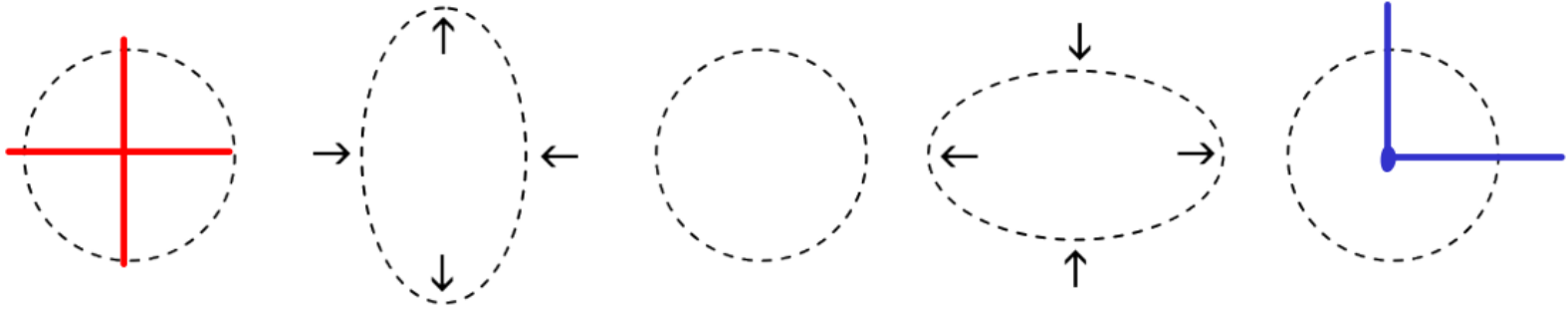
$$\bar{h}_{mn} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & A_{xx} & A_{xy} & 0 \\ 0 & A_{xy} & -A_{xx} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \cos(\omega(t - z))$$

Polarisation states

$A_{xy} = 0$

$A_{xx}^{(TT)} \neq 0$

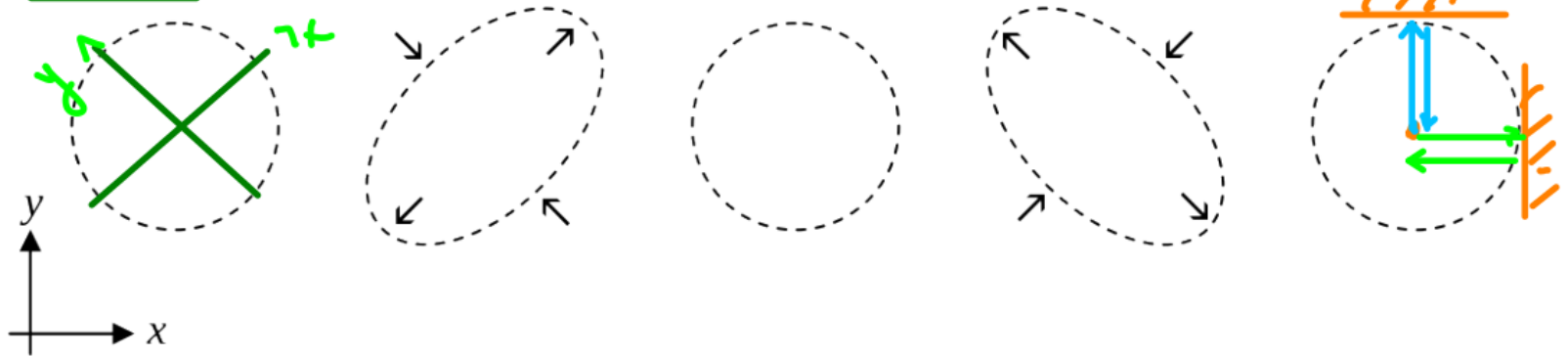
+ Polarisation



$A_{xx} = 0$

$A_{xy}^{(TT)} \neq 0$

× Polarisation



Suggested reading



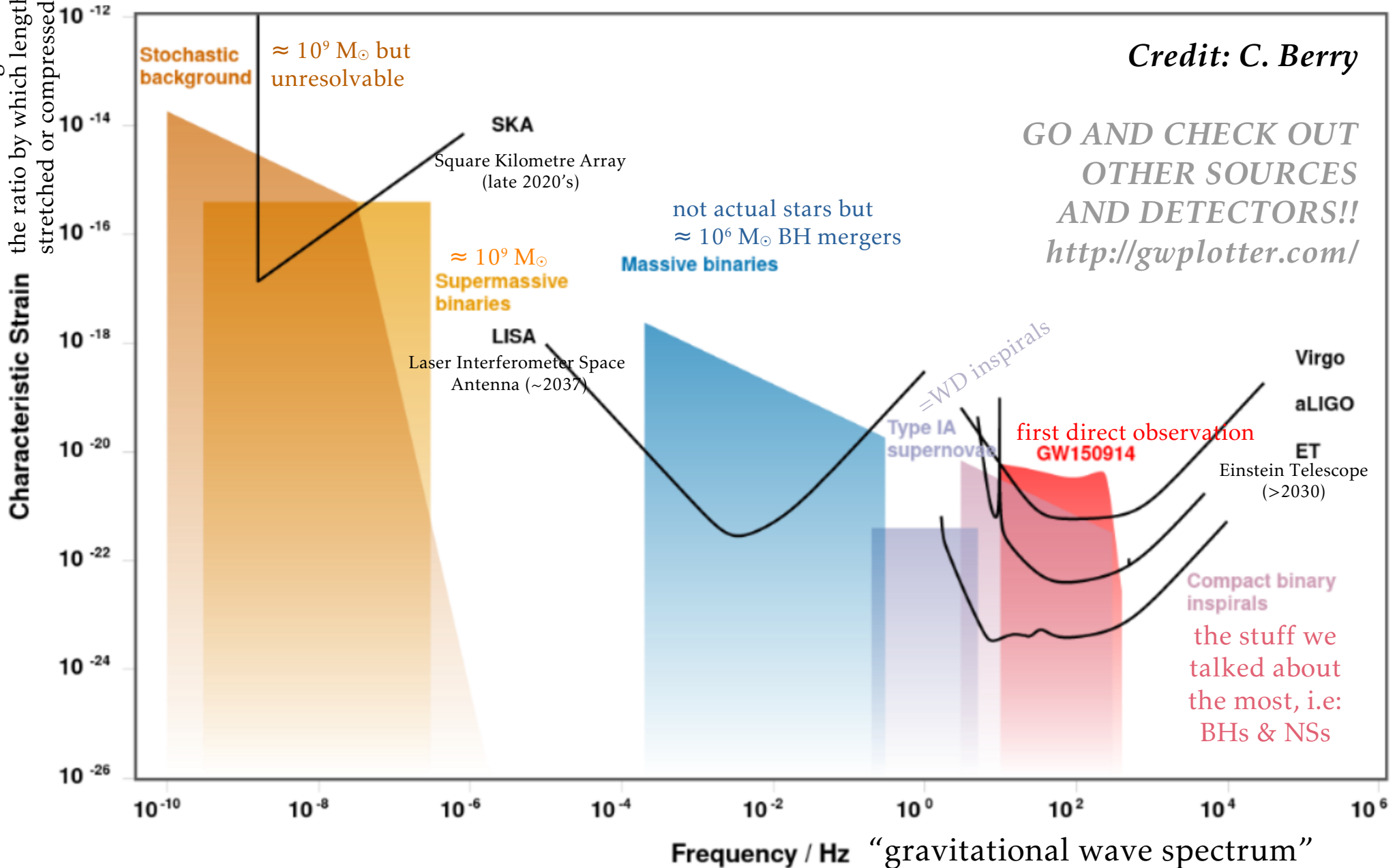
calculation details about the plane wave

- Chapter 20 in R. D’Inverno, *Introducing Einstein’s relativity*, Clarendon Press, 1998
- B. F. Schutz’s lecture notes about *Gravitational Waves* at the 2011 Azores School on *Observational Cosmology* (online) *→ he talks about detectors, too*
- T. Matolcsi, *Spacetime without reference frames*, Minkowski Press, 2020 (online) *→ a clean treatment of elementary spacetimes*

$$\square h_{ab} + R * h = 0$$

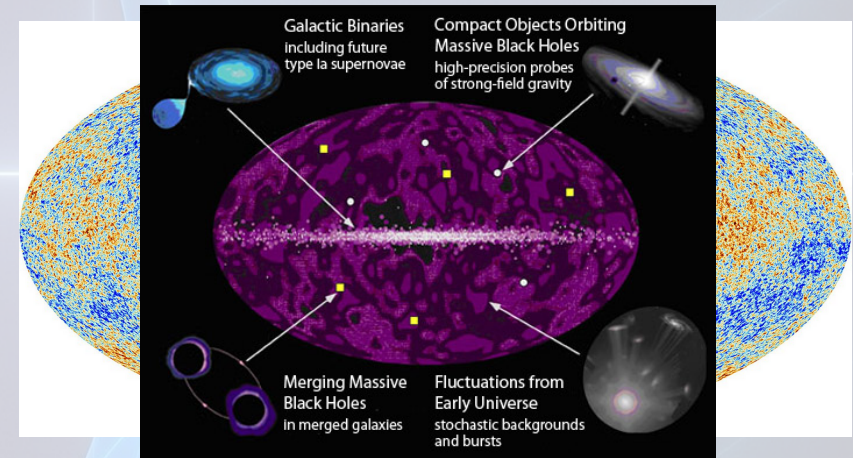
Detector sensibility

a measure of the grav. wave's effect:
the ratio by which lengths are
stretched or compressed (dimensionless)



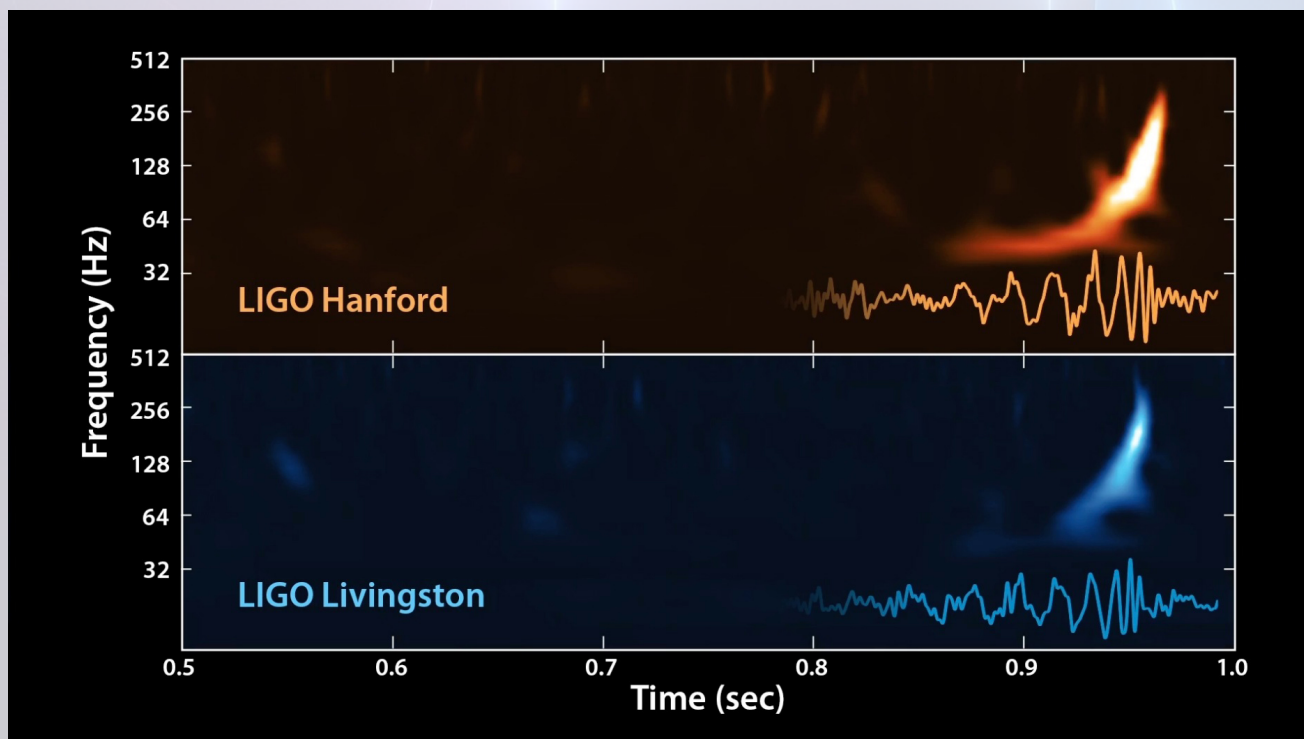
Cosmic grav.wave background

- Heard about the cosmic microwave background?
- GW-background:
 - undetected (yet)
 - cosmological sources
 - processes during e.g. the cosmic inflation (10^{-36} – 10^{-33} sec after the Big Bang)
 - astrophysical sources
 - large number of *unresolvable* BH-BH (or BH-NS, or NS-NS) mergers; additional WD-WD mergers, supernova explosions...



The whispering of the Universe

<https://www.youtube.com/watch?v=2PzbYK1x3Vo>



'GW150914'

$35 M_{\odot}$ & $30 M_{\odot}$

(BH+BH)

=

$64 M_{\odot}$

*$3 M_{\odot}$ converted
into GWs!*