

# Gravitational-wave progenitors

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Lecture #5

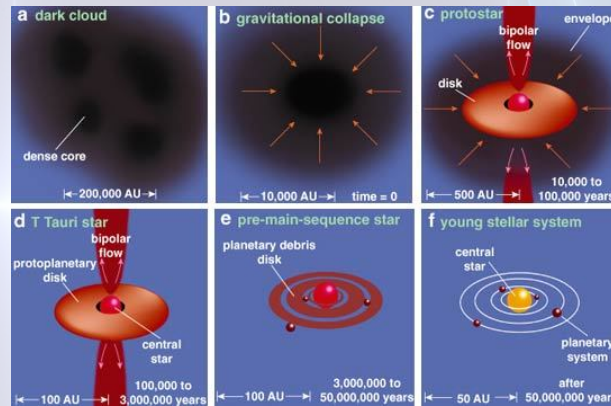
**NCU, Summer Semester 2022**



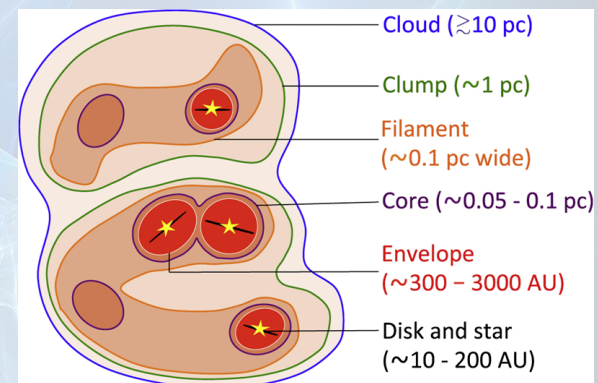
*Previously  
on GW-progenitors...*

# Star-formation (of massive stars)

- under active research
- low-mass stars:

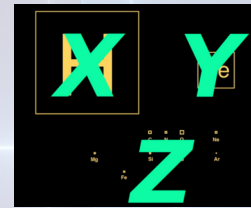


- massive stars?
  - strong radiation may blow away the material
  - hierarchical star formation?



# Onset of stellar evolution: ZAMS

- Zero-Age Main Sequence
  - (core) composition:  
same as the molecular cloud



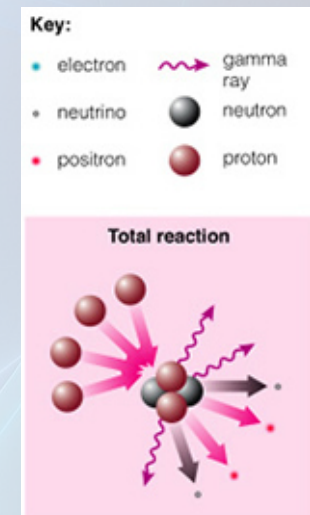
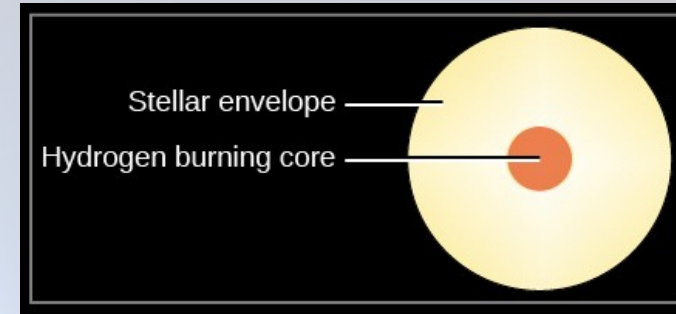
$$\begin{aligned}Z_{\odot} &\sim 0.014 (<2\%) \\Z_{\text{LMC}} &\sim 0.004 \\Z_{\text{SMC}} &\sim 0.002 \\Z_{\text{GCs}} &\sim <0.005 \\Z_{\text{PopIII}} &= 0\end{aligned}$$

- hydrogen burning starts (in the core)
- hydrostatic & thermodynamic equilibrium
  - no bipolar outflows etc.
  - stellar structure equations hold\*

\*"pre-MS": last phases of star-formation modelled using the structure equations

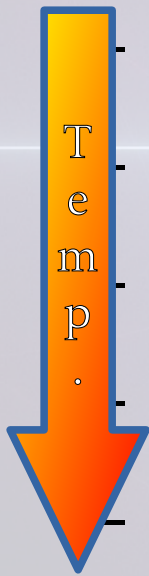
# Longest phase of stellar evolution: MS

- Main Sequence
  - **core**-hydrogen-burning phase
- lasts for ~90% of the lifetime (longest of them all)
- core temperatures: ~40M K
- in massive stars: CNO cycle
  - low-mass stars like the Sun: pp-chain
- $4\ ^1\text{H} \rightarrow\ ^4\text{He} + \gamma$
- end of MS: Terminal-Age Main Sequence (TAMS)



# Post-MS

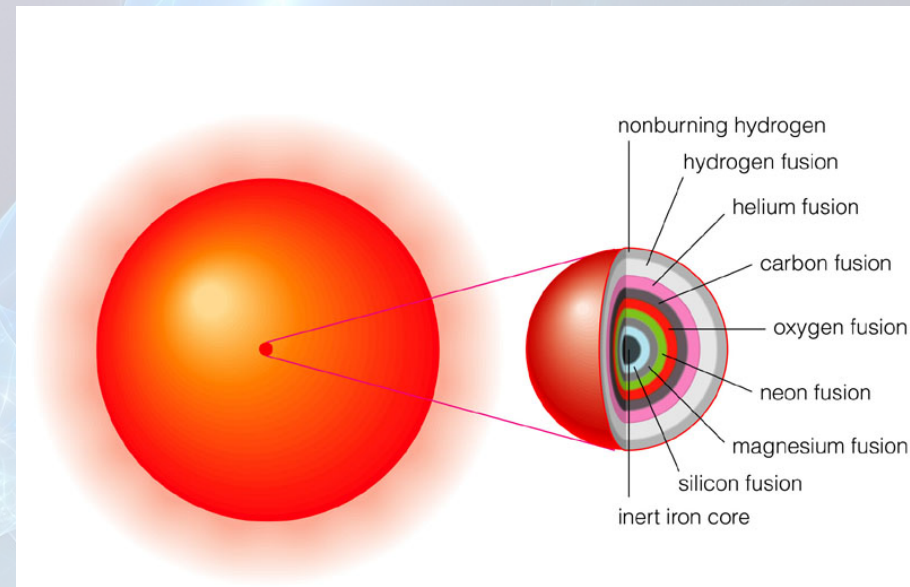
- Includes:



- core-He-burning (& shell-H-burning)
- core-C-burning (& shell-He & shell-H-burning)
- core-O-burning (& shell-C, shell-He, shell-H...)
- core-Ne-burning (& shell...)
- core-Si-burning (& shell...)

- **onion-structure** of massive stars

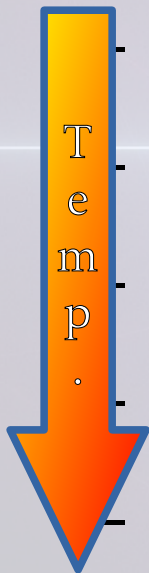
Note: the onion layers become more and more complex nearing the end of the lifetime



**Table 4.1** Major nuclear-burning processes

<i>Nuclear fuel</i>	<i>Process</i>	$T_{\text{threshold}}$ ( $10^6 K$ )	<i>Products</i>	<i>Energy per nucleon (MeV)</i>
H	$p - p$	$\sim 4$	He	6.55 (low-mass stars)
H	CNO	15	He	6.25
He	$3\alpha$	100	C, O	0.61
C	$C + C$	600	O, Ne, Na, Mg	0.54
O	$O + O$	1000	Mg, S, P, Si	$\sim 0.3$
Si	Nuc. eq.	3000	Co, Fe, Ni	$< 0.18$

• Inc



Temperature

Core burning (H, He, C, O, Si, Fe, Ni, ...)

## Stellar Fusion Requirements

<b>Fusion</b>	<b>Fusion By-product</b>	<b>Minimum Core Temperature</b>	<b>Minimum Core Density</b>	<b>Minimum Stellar Mass*</b>
<b>Hydrogen</b>	He	13 million K	100 gm/cc	0.08 solar masses
<b>Helium</b>	C, O	100 million K	100,000 gm/cc	0.5 solar masses
<b>Carbon</b>	O, Ne, Mg, Na	500 million K	200,000 gm/cc	4 solar masses
<b>Neon</b>	O, Mg	1.2 billion K	4 million gm/cc	about 8 solar masses
<b>Oxygen</b>	Mg, Si, S, P	1.5 billion K	10 million gm/cc	about 8 solar masses
<b>Silicon</b>	Si, S, Ar, Ca, Ti, Cr, Fe, Ni	around 3 billion K	30 million gm/cc	about 8 solar masses

Note: the more nearing

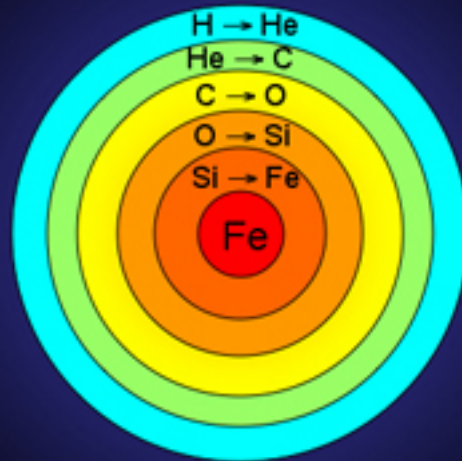
gen fusion  
n fusion  
arbon fusion  
xygen fusion  
on fusion  
esium fusion  
on

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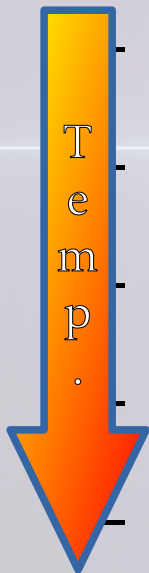
For a 25 solar mass star:



Stage	Duration
H $\rightarrow$ He	$7 \times 10^6$ years
He $\rightarrow$ C	$7 \times 10^5$ years
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O $\rightarrow$ Si	6 months
Si $\rightarrow$ Fe	1 day
Core Collapse	1/4 second

Fusion	Products	Temperature	Density	Mass
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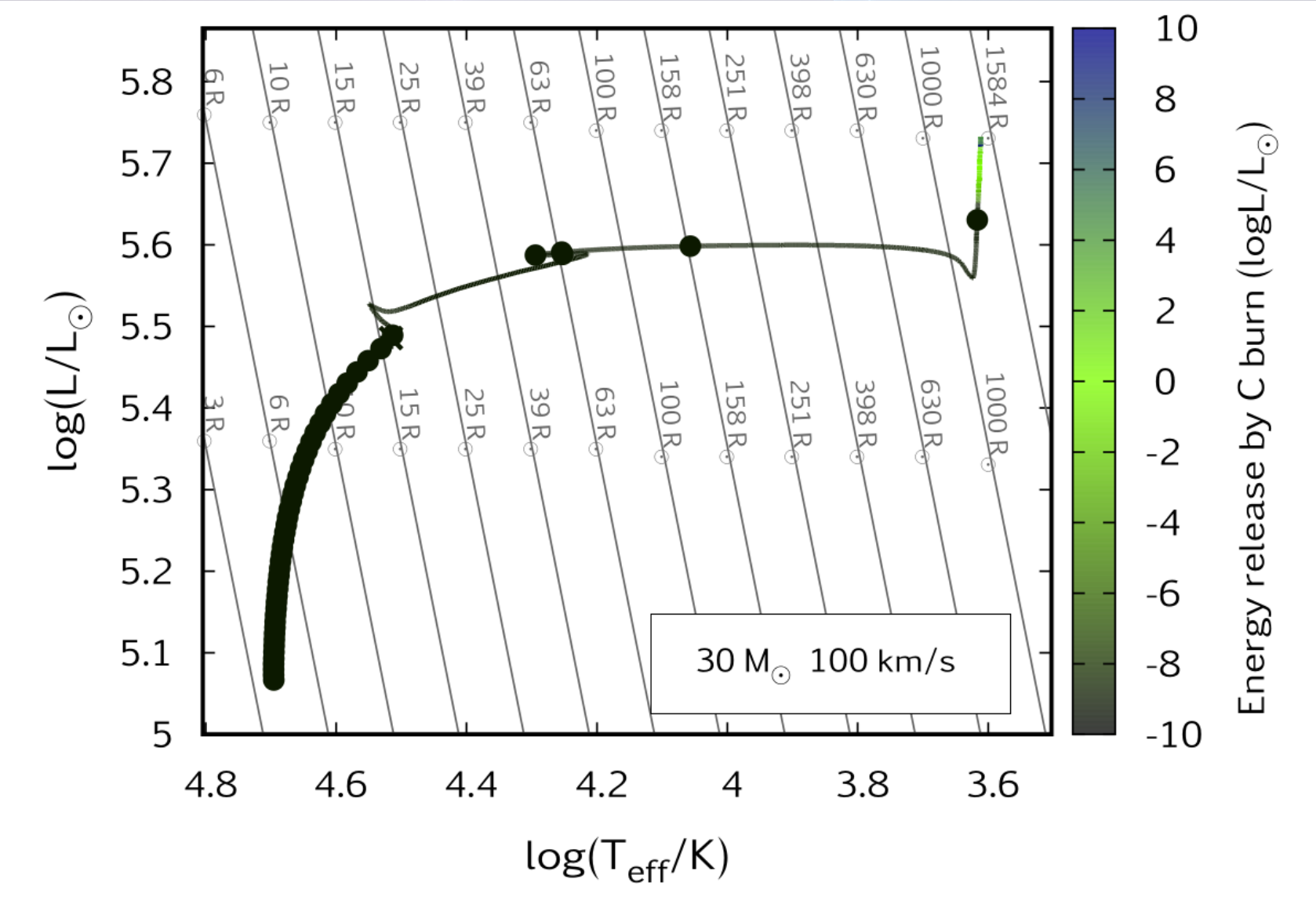


• on

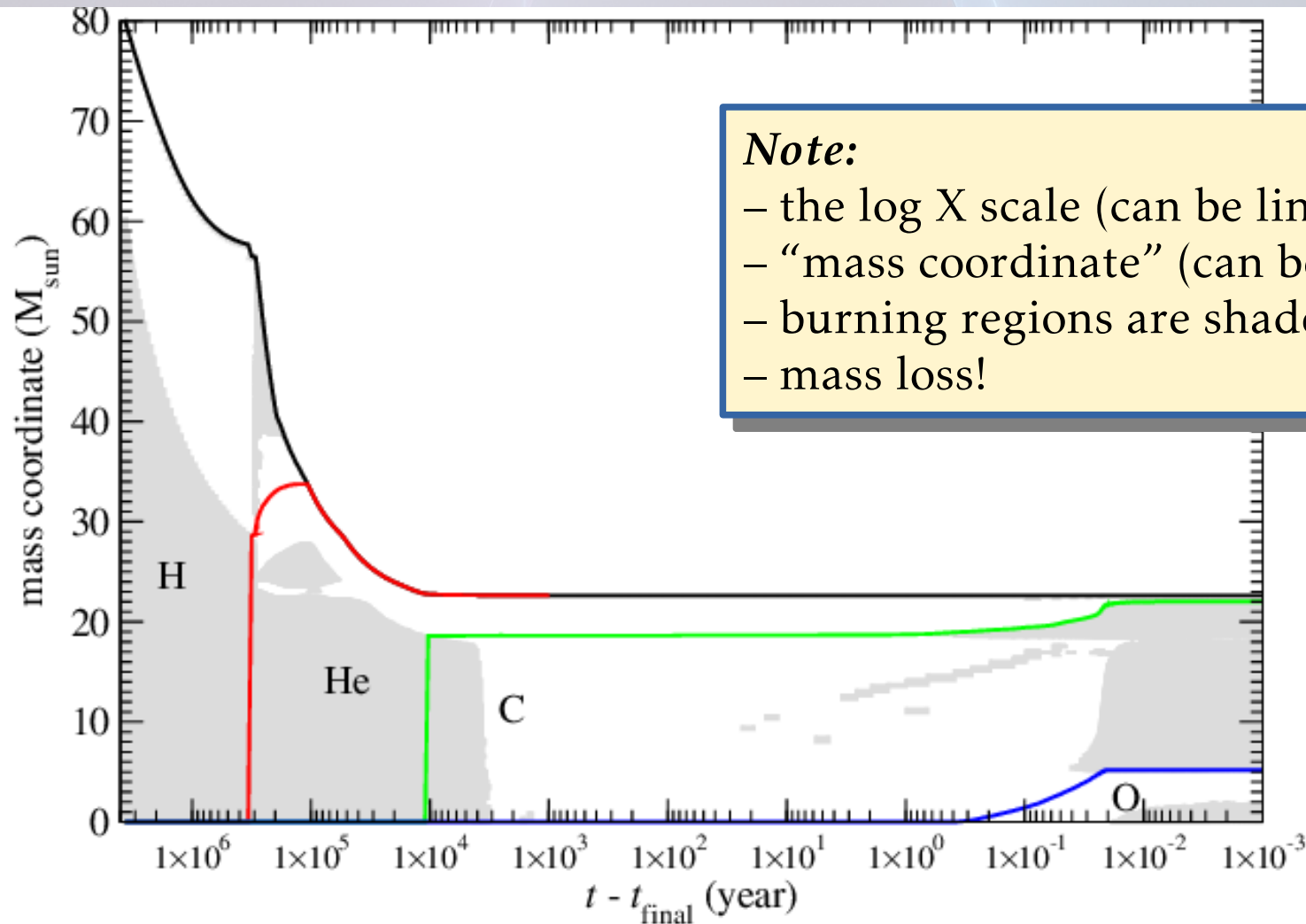
Note: the more nuclear burning stages, the more mass is lost during the star's lifetime.



# How much do we see from this in the HRD?



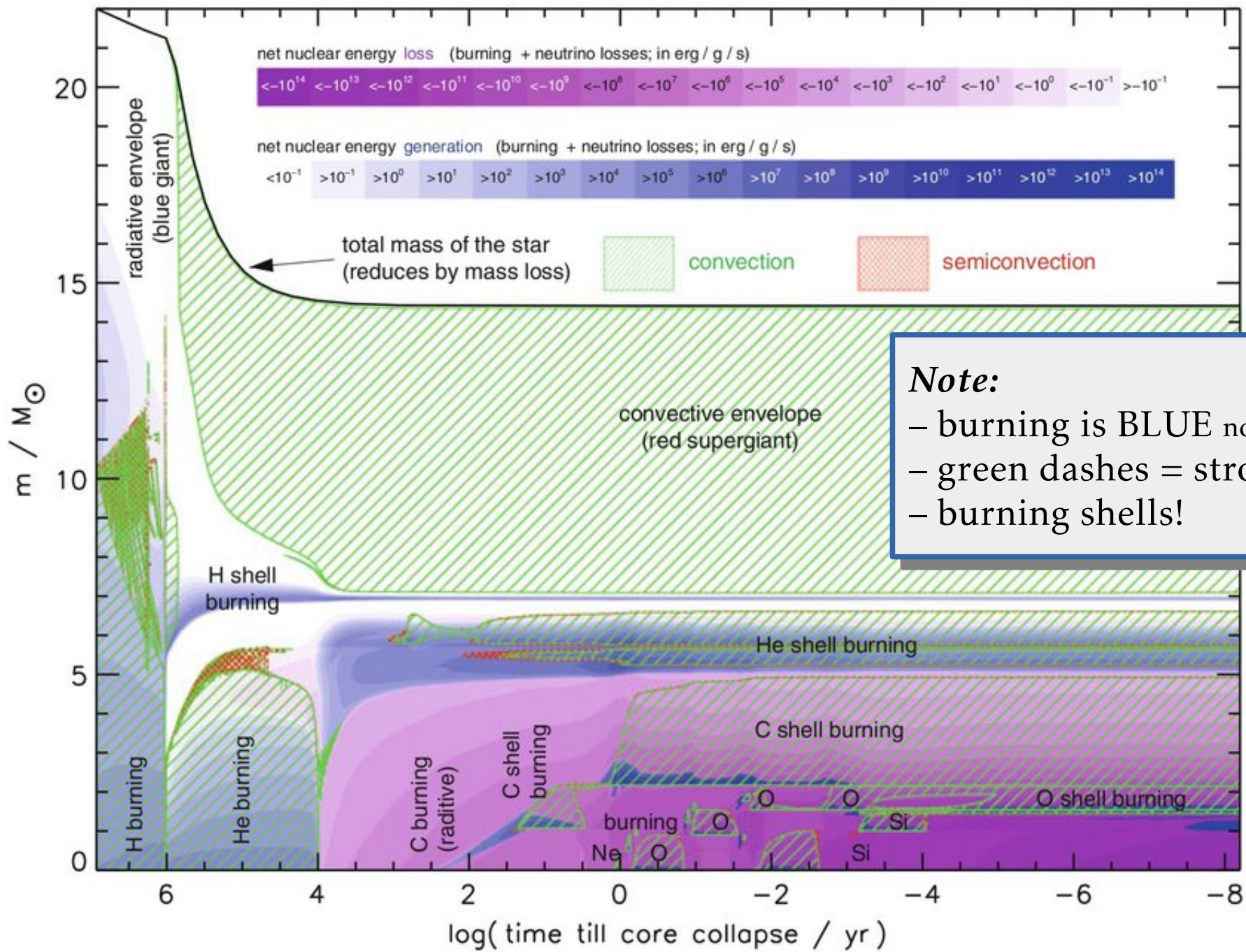
# Kippenhahn diagram



**Note:**

- the log X scale (can be linear too)
- “mass coordinate” (can be radius too)
- burning regions are shaded
- mass loss!

*Credit: Leung, Nomoto & Blinnikov (2019)*

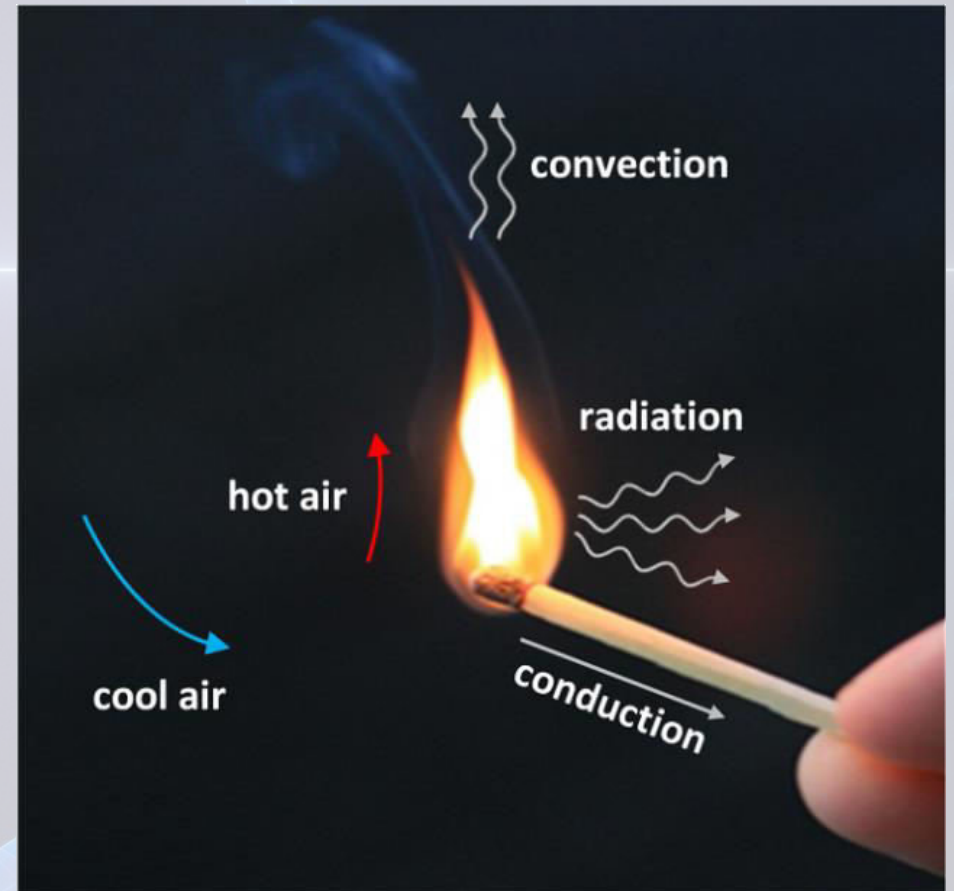
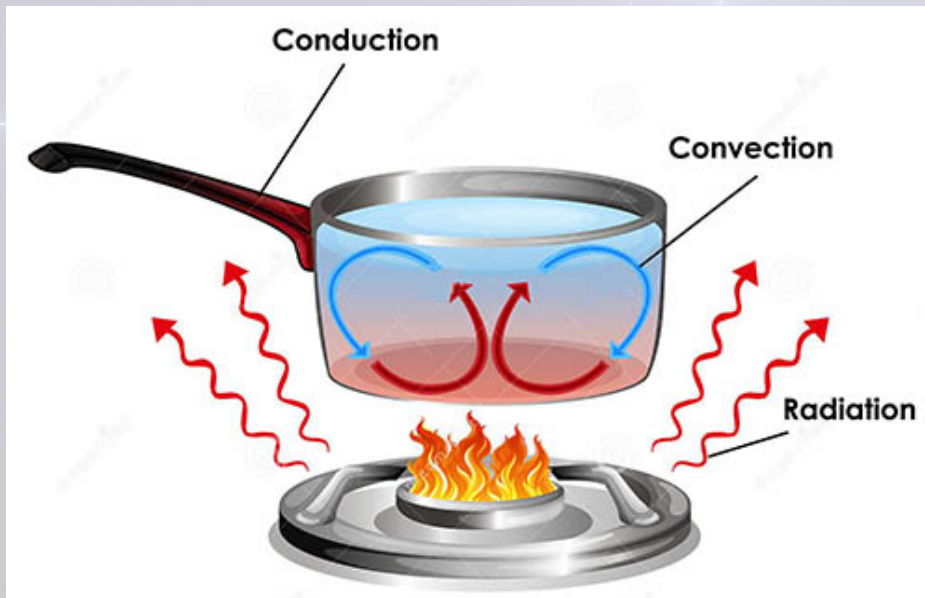


**Note:**

- burning is BLUE not green/purple
- green dashes = strong mixing
- burning shells!

# Some words about convection

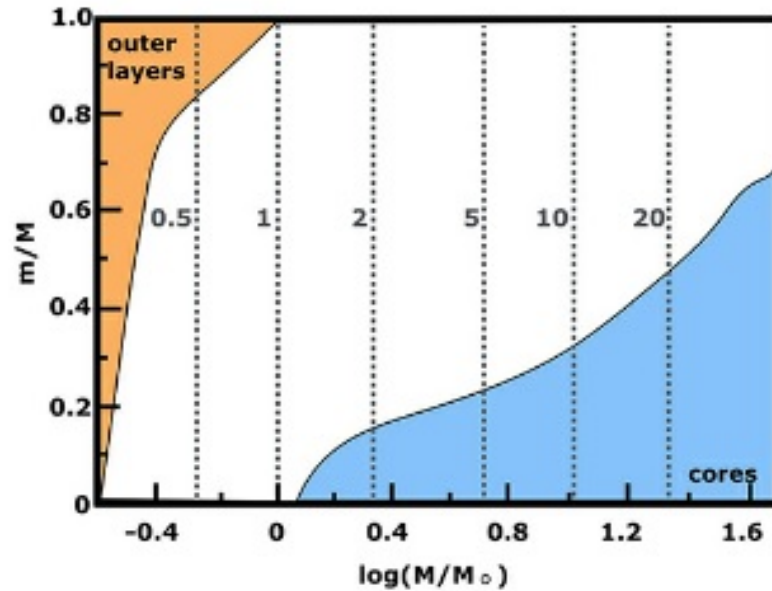
and about *heat transfer* in general



- convection arises wherever heat needs to be transported extra efficiently  
e.g. burning core of massive stars, envelope of (super)giants and low-mass stars...
- leads to strong mixing (cf. boiling soup)

Some

ection



**Figure 7.6.** Occurrence of convection in stars at the beginning of the core H-fusion phase (ZAMS). The mass of convective envelopes (orange) and convective cores (blue) is expressed as a fraction of the stellar mass, from  $m/M = 0$  in the core to  $m/M = 1$  at the surface. The vertical lines indicate the stel-

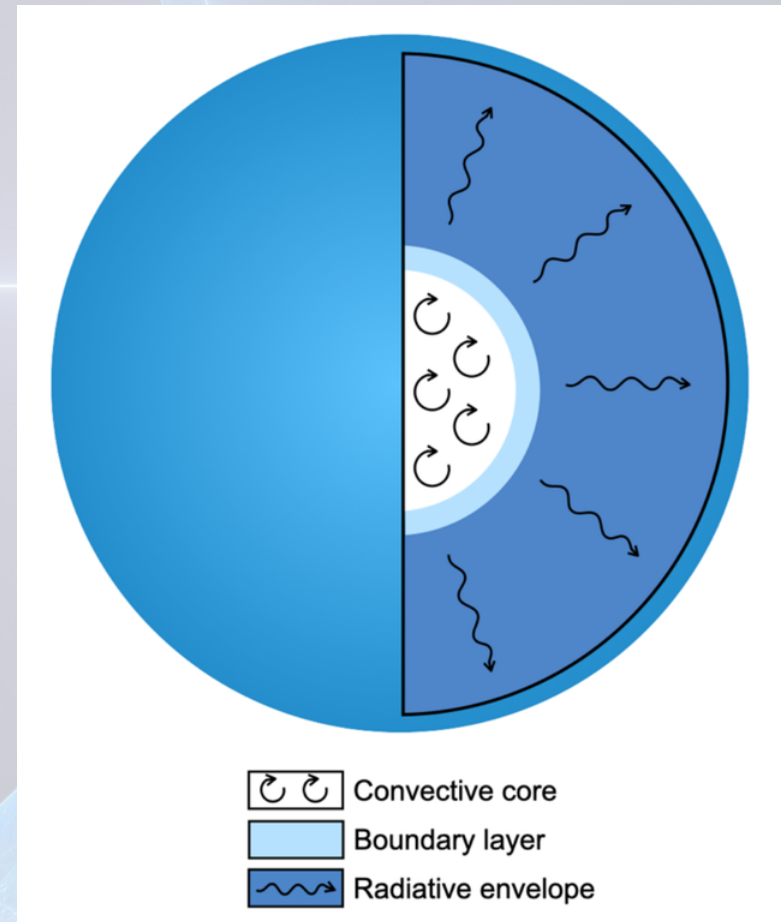


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# Some more words on *internal mixing*

hardcore  
stuff

- convection is just one type of mixing
- other types:
  - convective overshooting
  - rotational mixing
  - sheer mixing
  - “semi-convection”
  - thermohaline mixing
  - ...



*Credit: May G. Pedersen (KITP)*

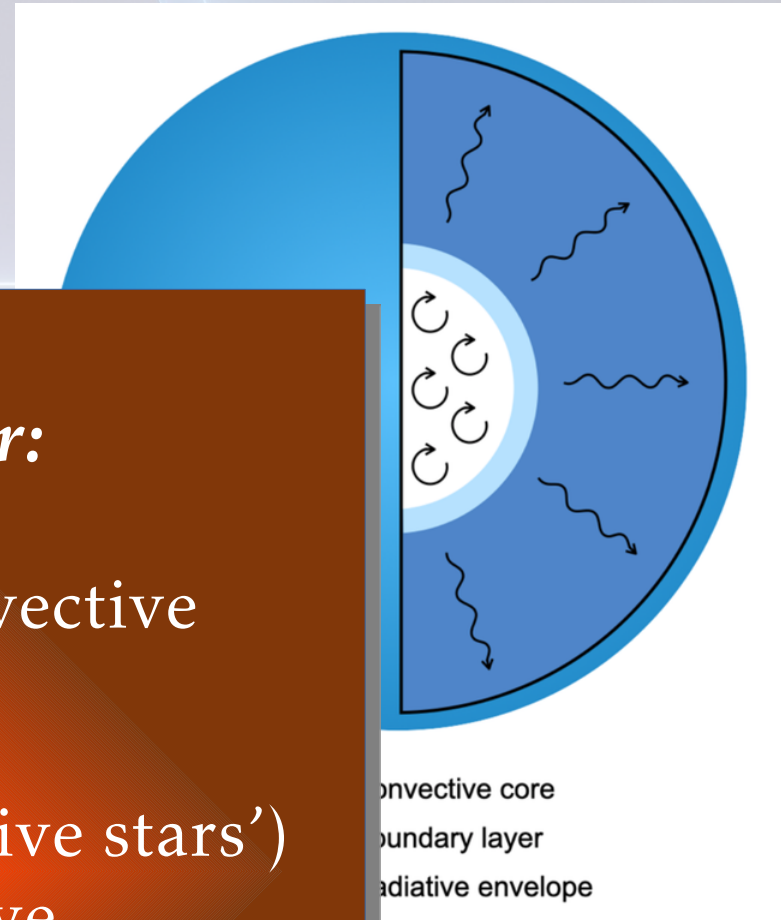
# Some more words on *internal mixing*

hardcore  
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- convection is just one type of mixing

*Make sure to remember:*

- massive stars's cores are convective  
(the Sun's core is radiative!)
- supergiants' (aka post-MS massive stars')  
envelope is *also* convective  
(will be important later, in binary interactions)



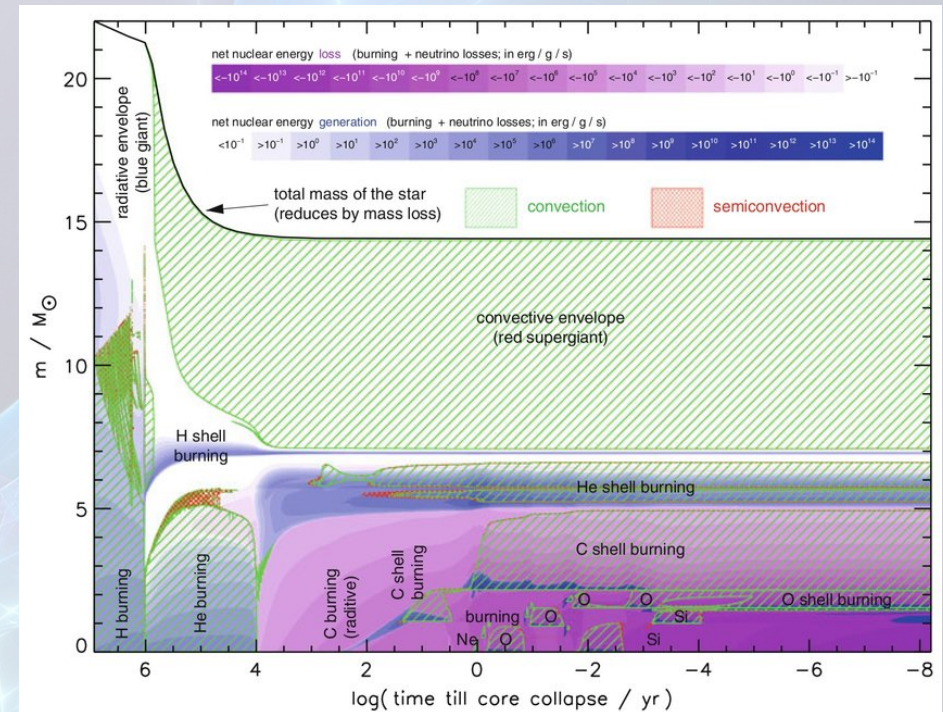
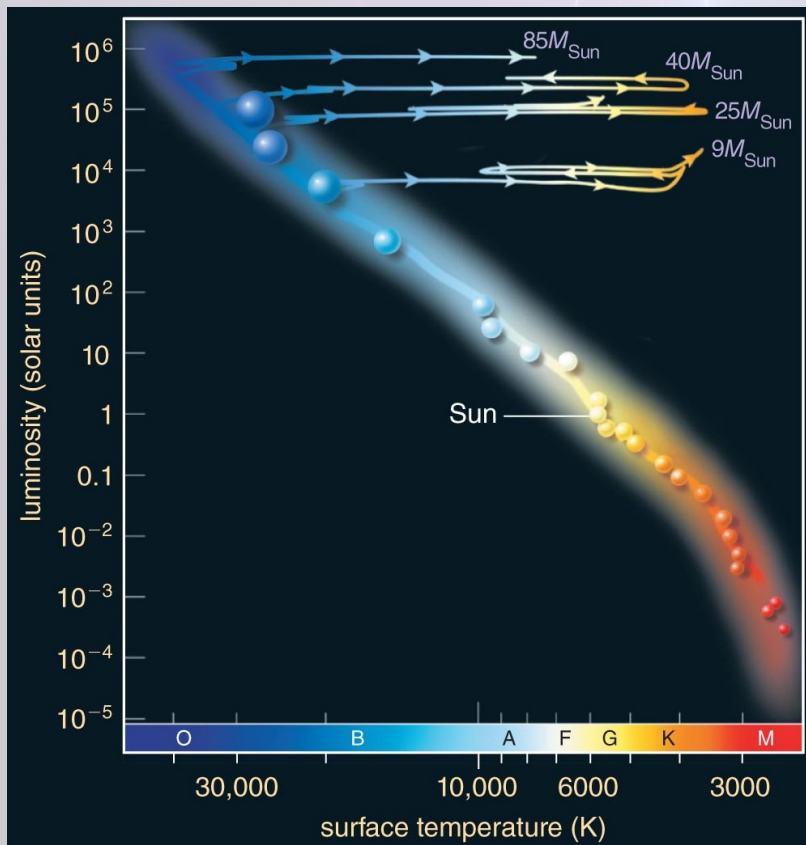
convective core  
boundary layer  
radiative envelope

*J. Pedersen (KITP)*

# HRD vs. Kippenhahn

- surface T, L
  - helps observational comparison

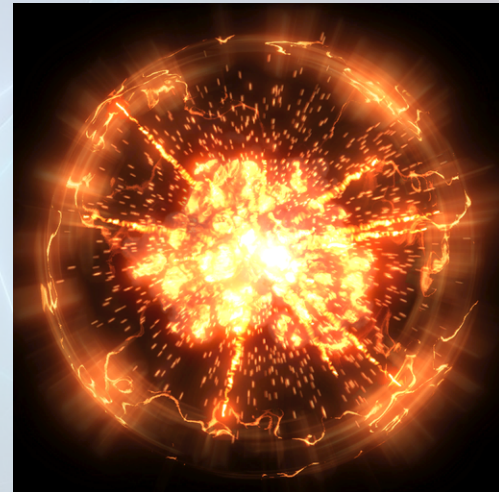
- interior structure
  - e.g. pre-supernova structure, mixing...





*Today...*

**EXPLOSIONS!!**

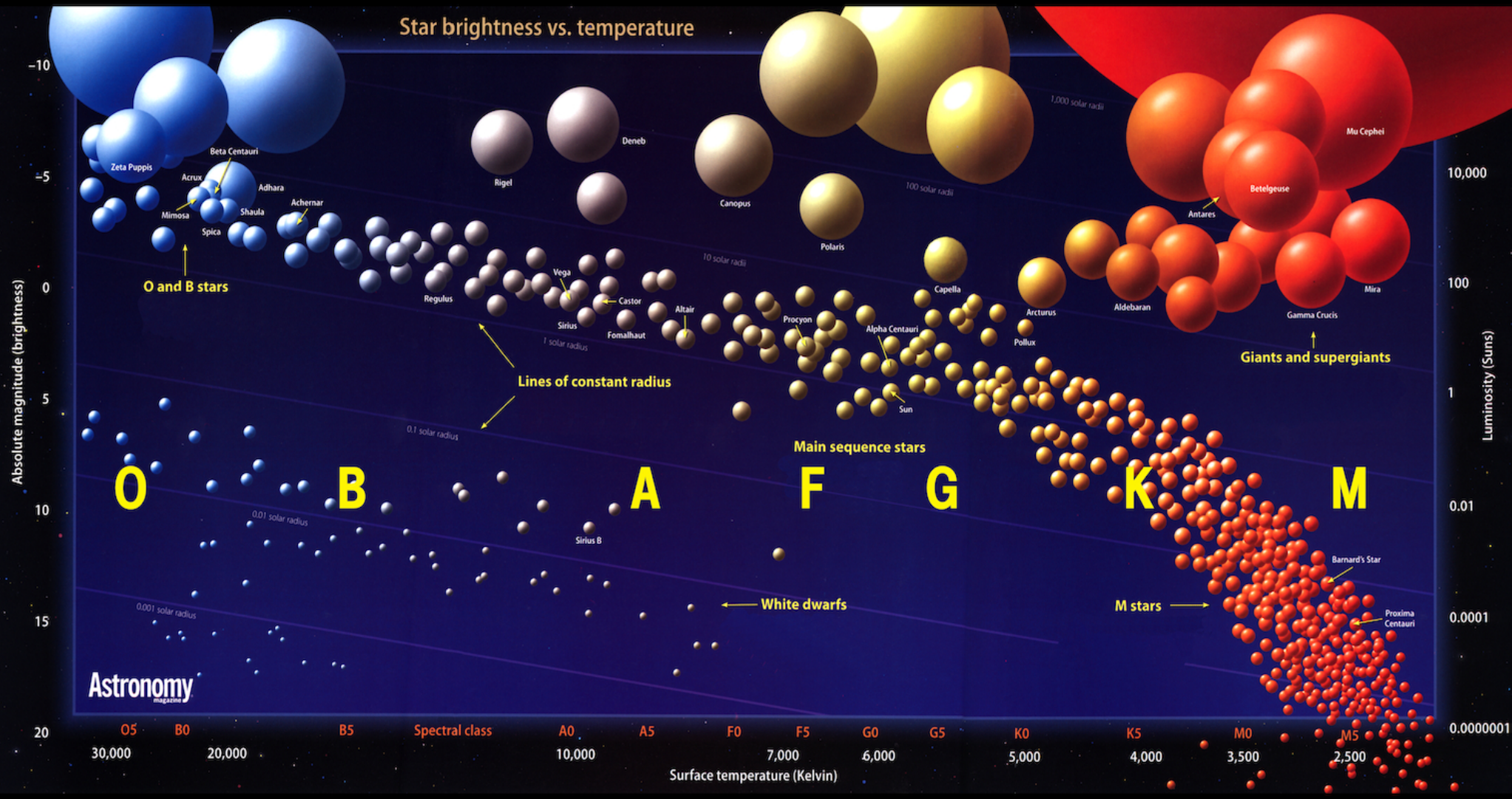


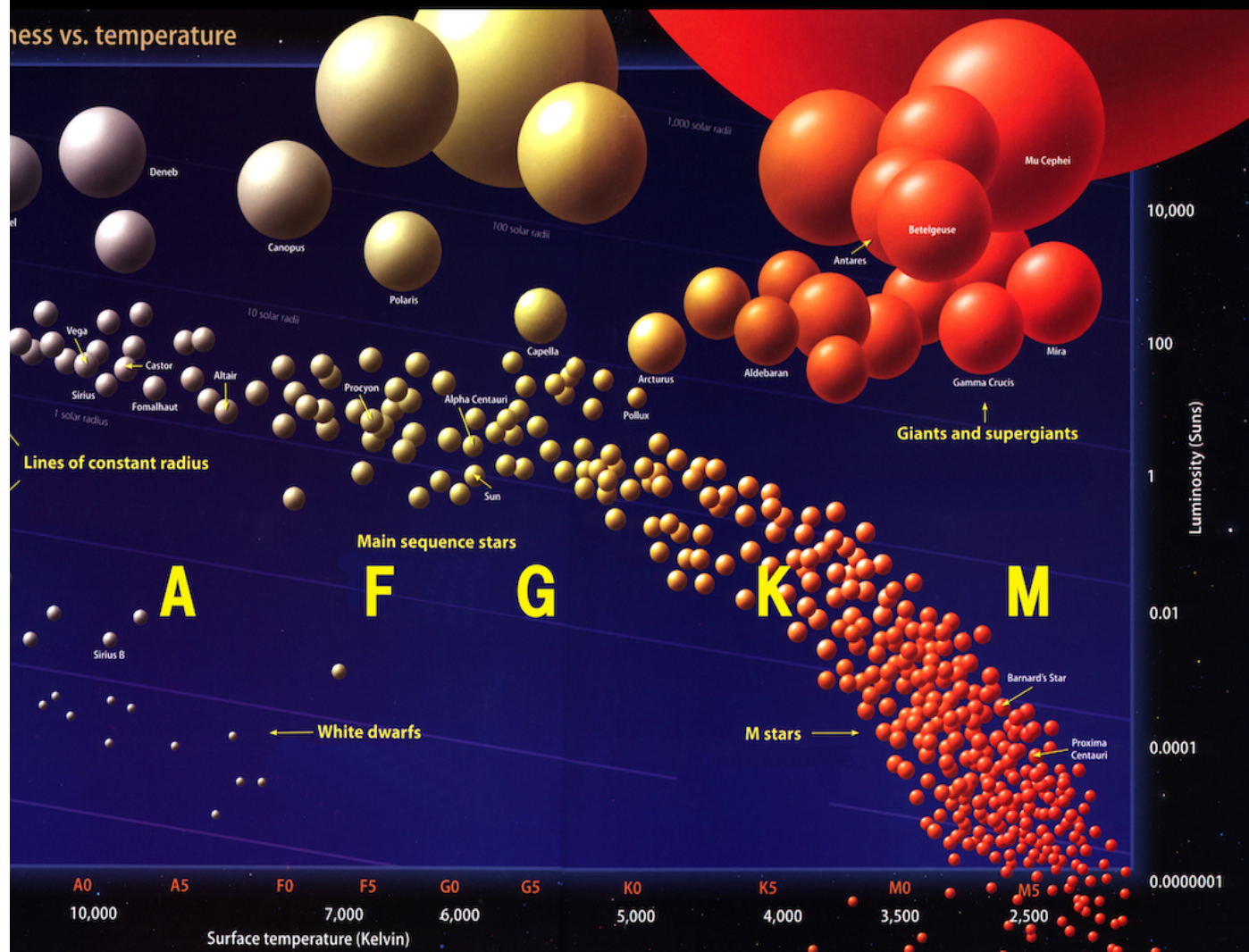
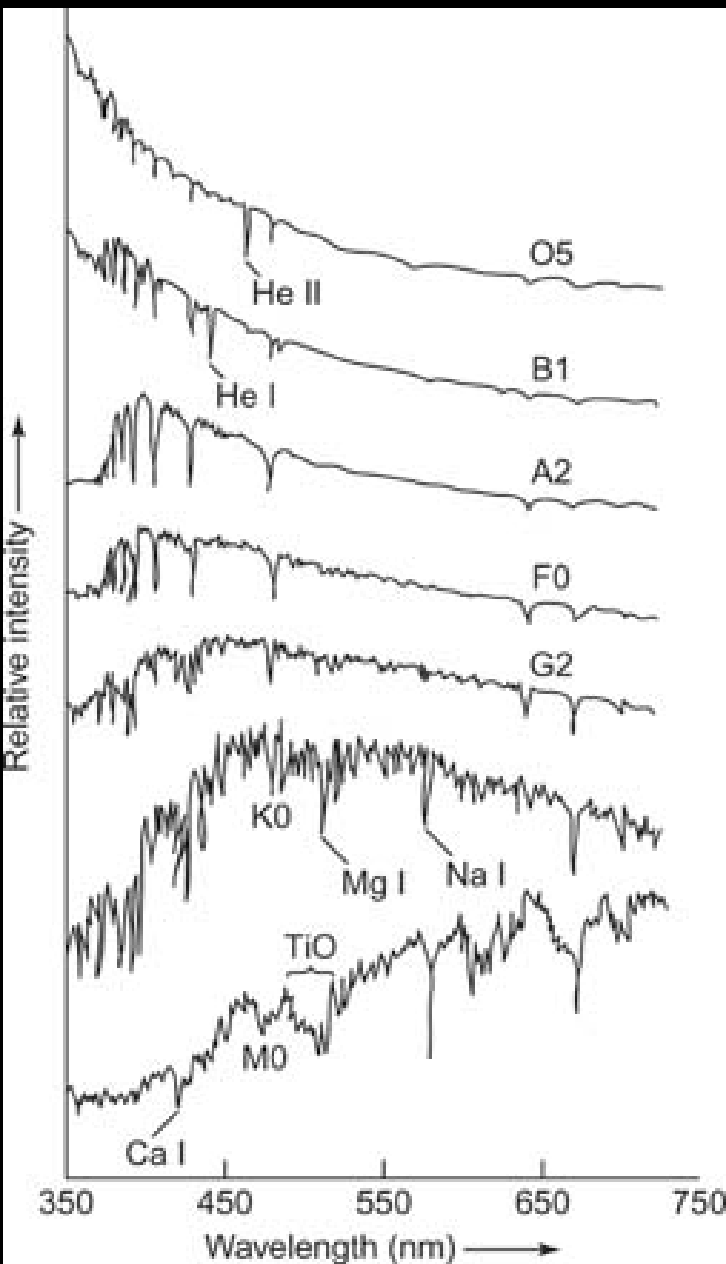
*But before...*

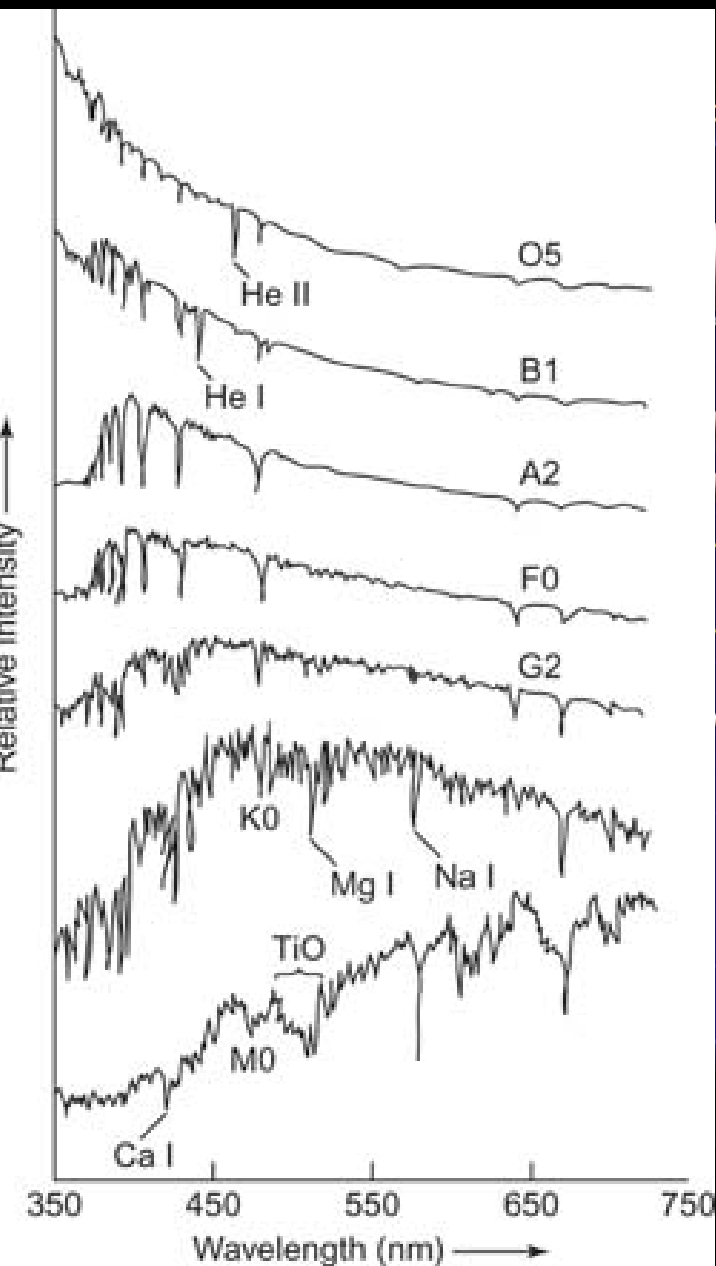
**Stellar classification  
and the Black Body approximation**

*Some history... :)*

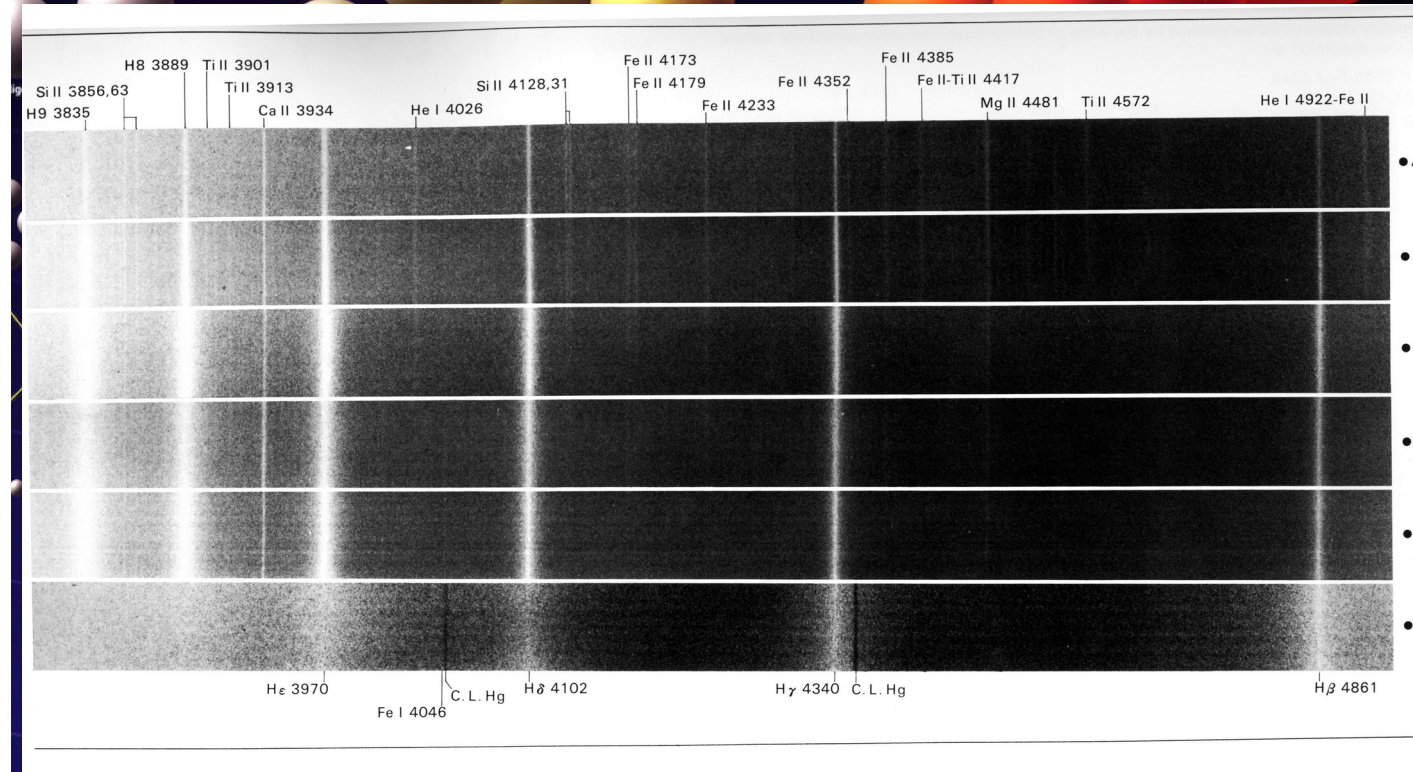
# Star brightness vs. temperature



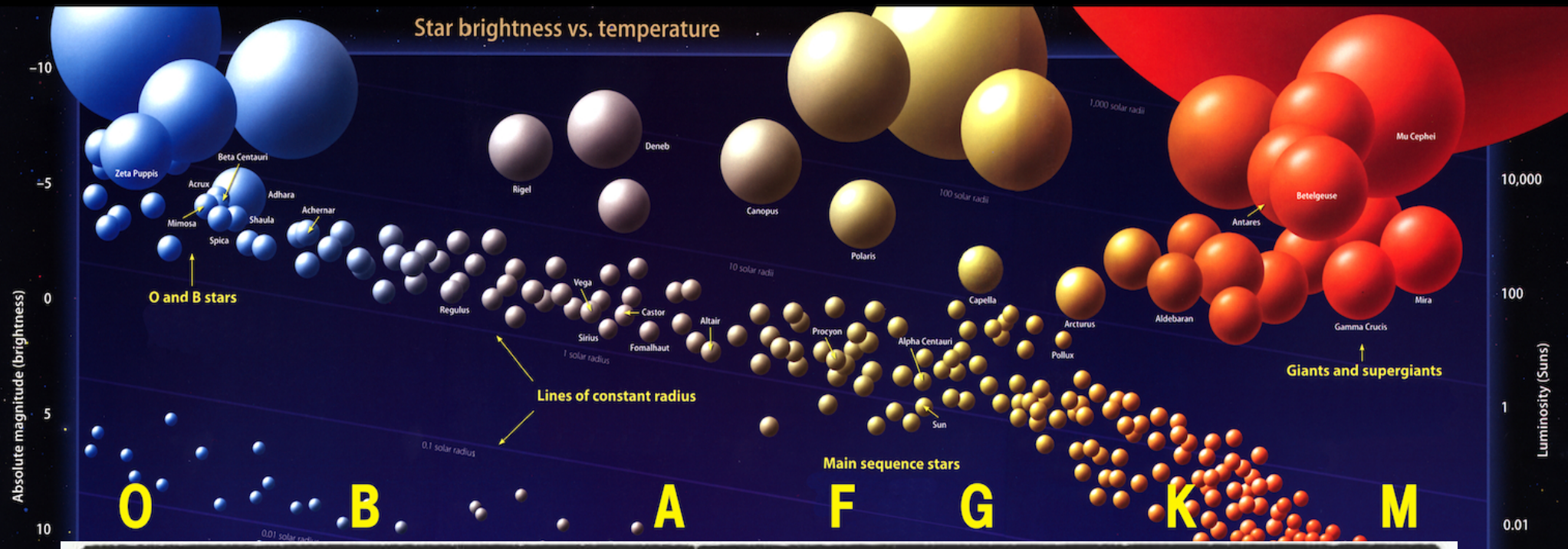




Mass vs. temperature



# Star brightness vs. temperature



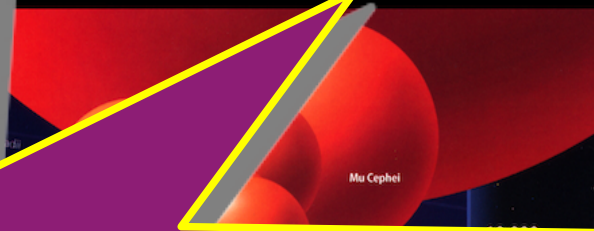
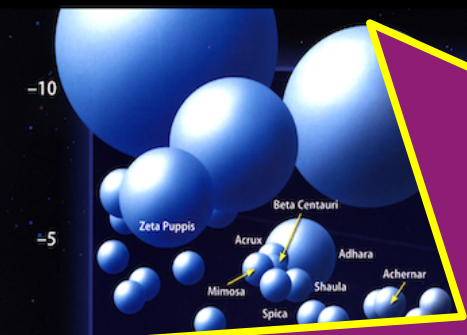
Star brightness vs. tempera

**Make sure to read more!**

Suggested article:  
"Women Astronomers  
at Harvard at the Turn of the Century"

<https://www.carleton.edu/goodsell/research/student-research/women/harvard/>

*...also: come to Torun Observatory ;) :D*



absolute magnitude (brightness)

Luminosity (Suns)

**M**

↑  
supergiants

-10

-5

0

5

15

20

100

1

0.01

0.0001

0.000001

# Planck law

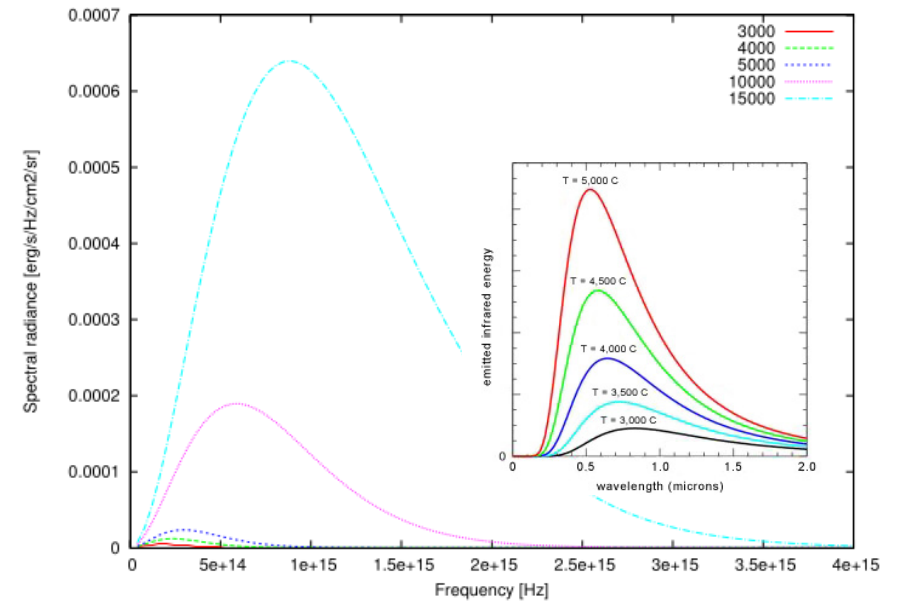
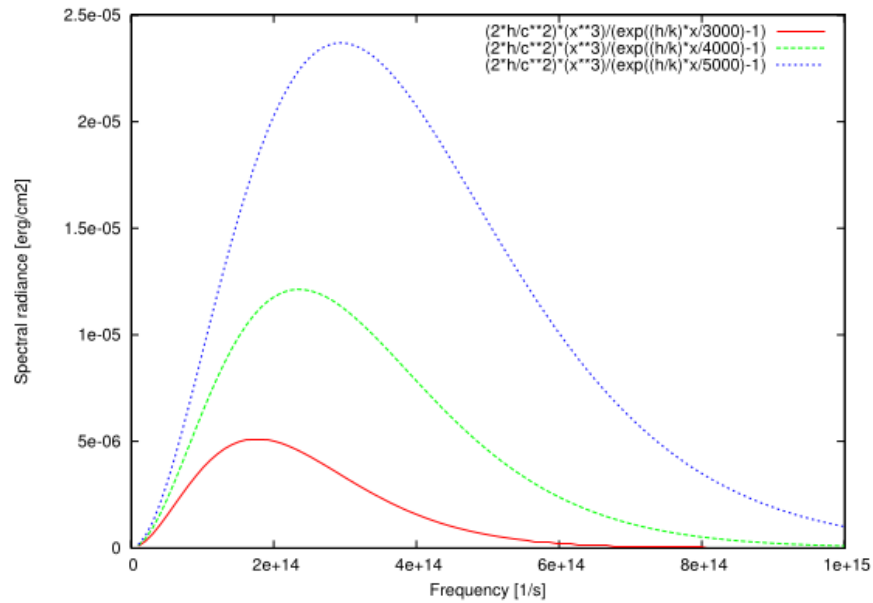
$$B(\nu, T_{eff}) = \frac{2h}{c^2} \frac{\nu^3}{e^{\frac{h\nu}{k_B T_{eff}}} - 1} \quad (3)$$

*here: as a function of frequency  
(works with wavelength as well)*

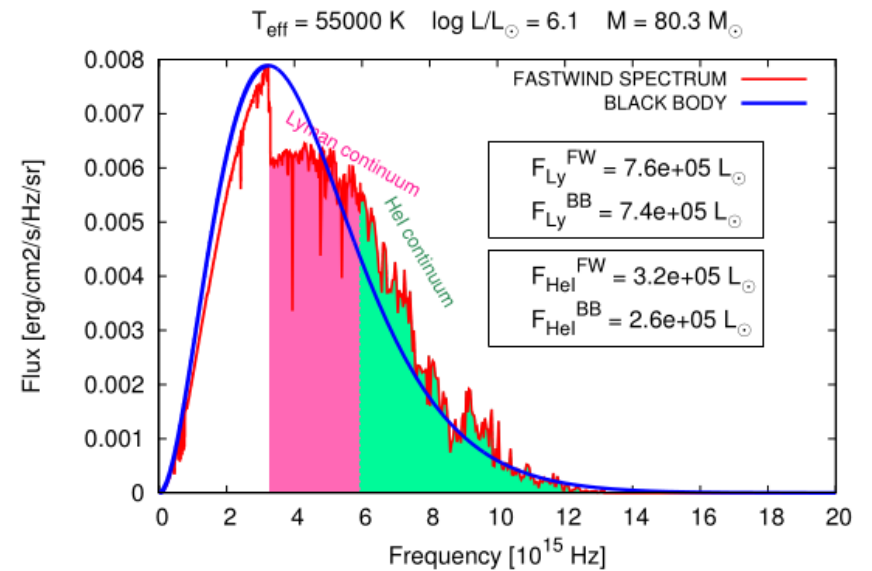
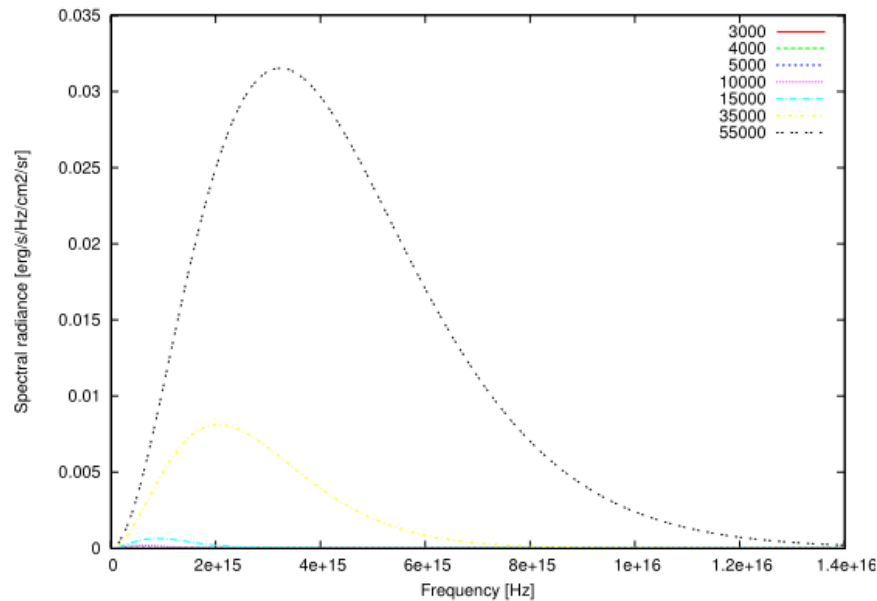
Note: there is a T value in it!



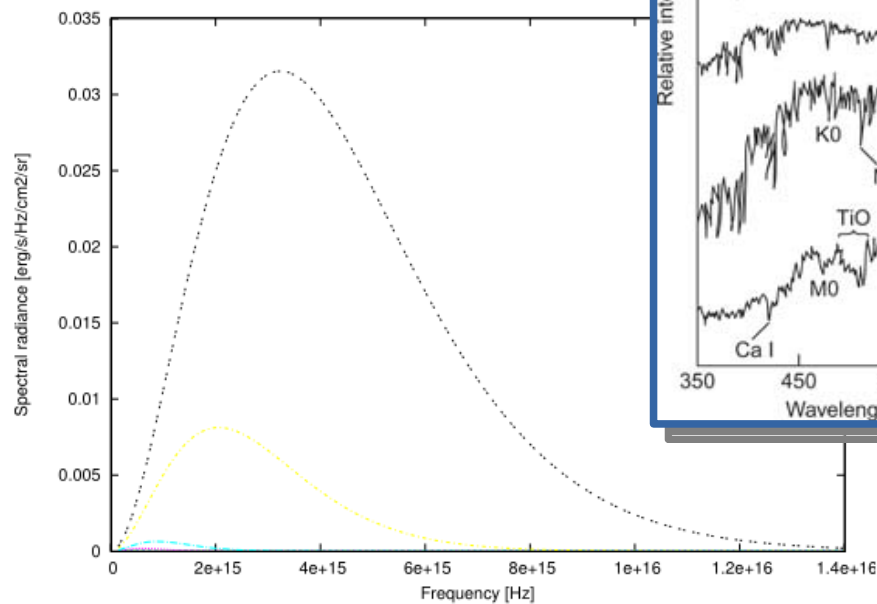
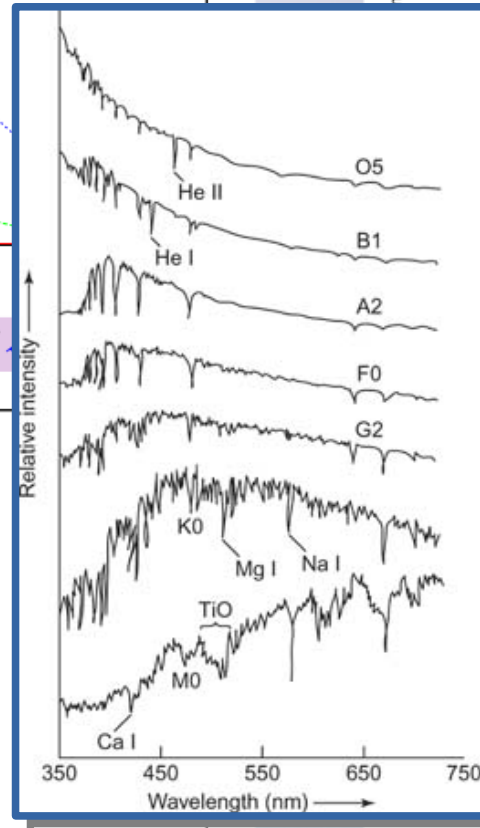
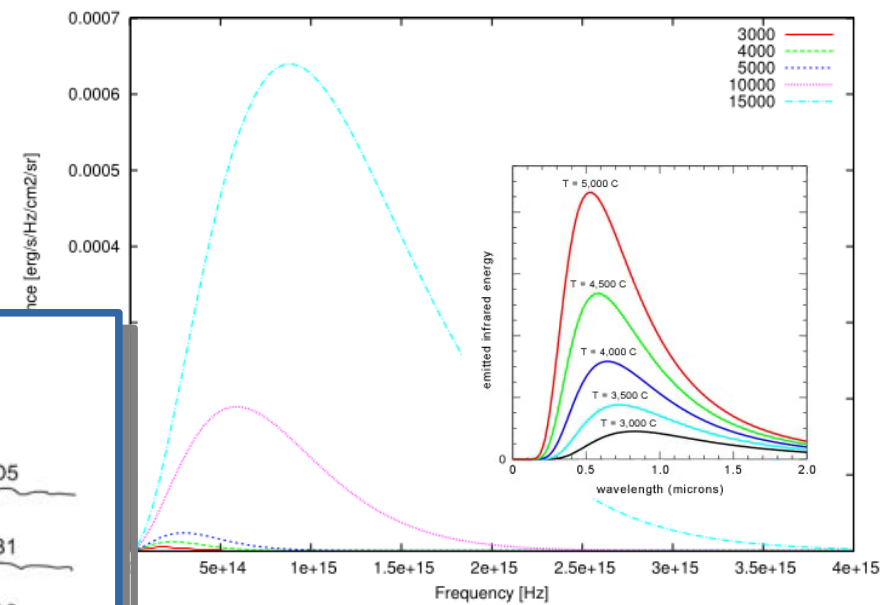
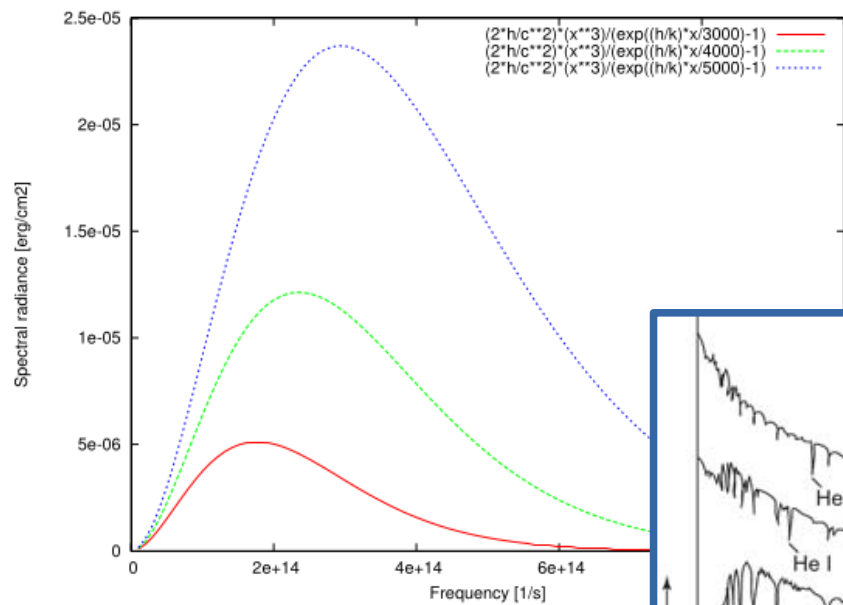
# Radiation field of stars with different $T_{eff}$



$$B(\nu, T_{eff}) = \frac{2h}{2} \frac{\nu^3}{e^{kT_{eff}} - 1} \quad (3)$$

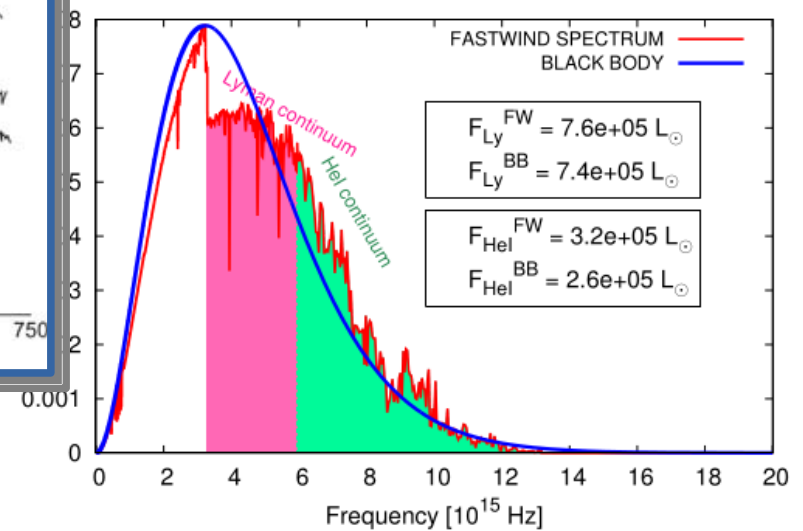


# Radiation field of stars with different $T_{eff}$



(3)

$T_{eff} = 55000 \text{ K}$     $\log L/L_{\odot} = 6.1$     $M = 80.3 M_{\odot}$

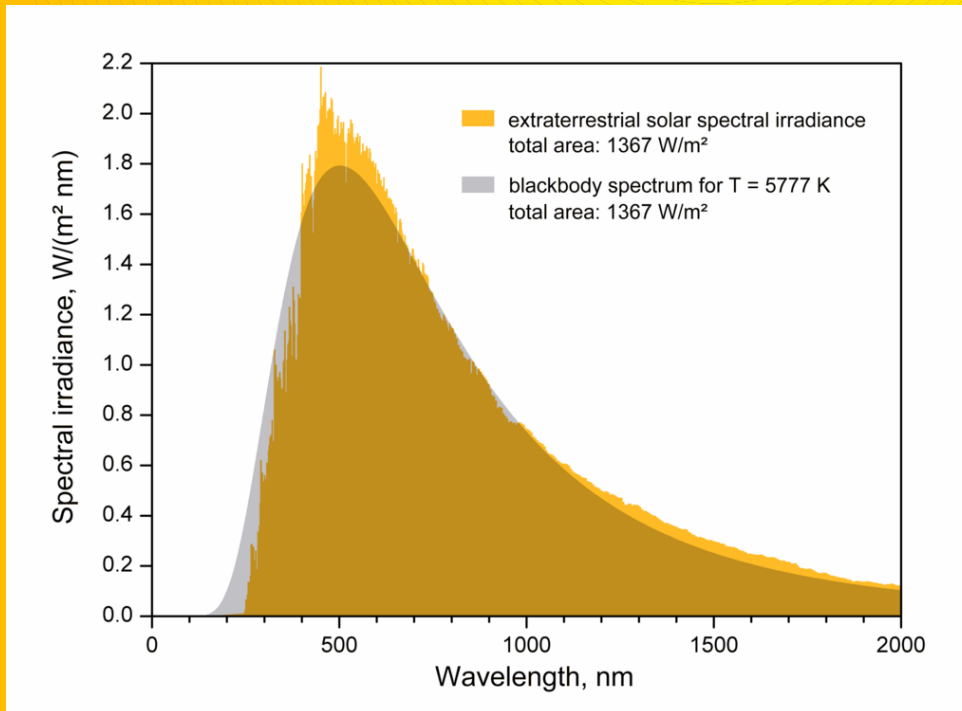


Moral of the story:

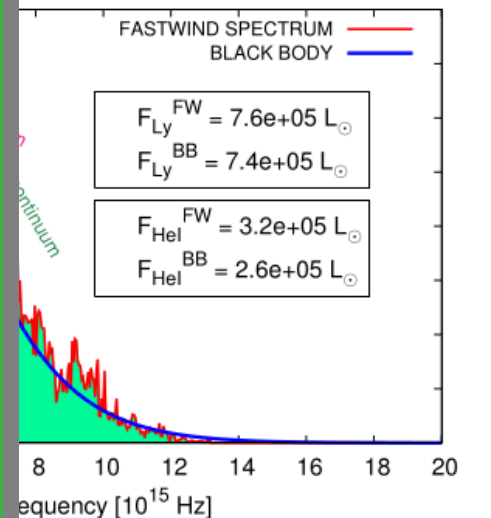
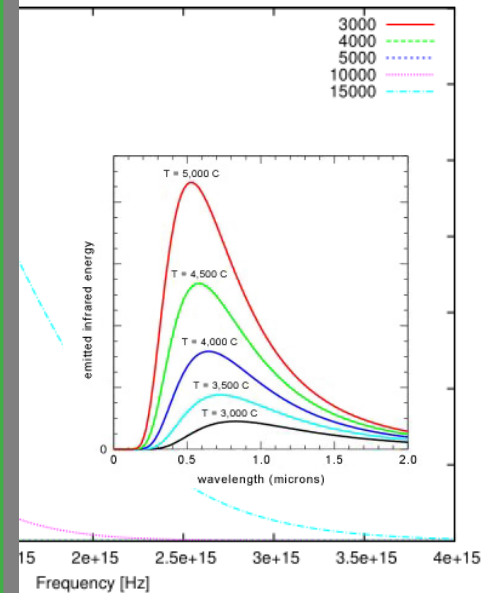
# Stars are perfect Black Bodies.

(Most of the time, more or less; but basically they are.)

**Their  $T_{\text{eff}}$  in the HRD is the  $T_{\text{eff}}$  from the Planck law.**

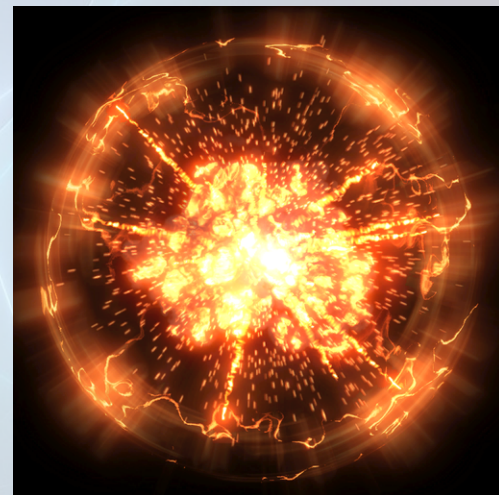


$T_{\text{eff}}$



*And now...*

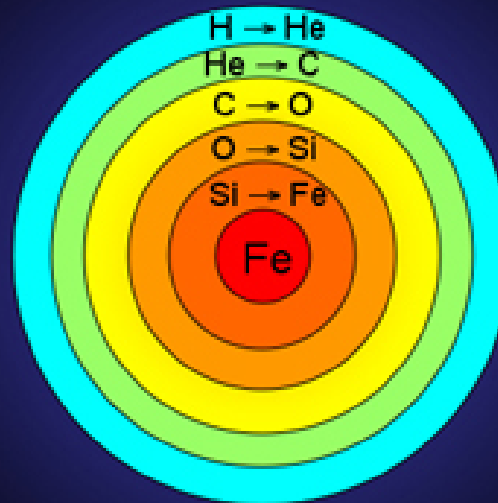
**EXPLOSIONS!!**



# Pre-supernova structure – iron core

- Includes:

- Temp ↓
- core-He-burning (& shell-H-burning)
  - core-C-burning (& shell-He & shell-H-burning)
  - core-O-burning (& shell-C, shell-He, shell-H...
  - core-Ne-burning
  - core-Si-burning
- onion-structure

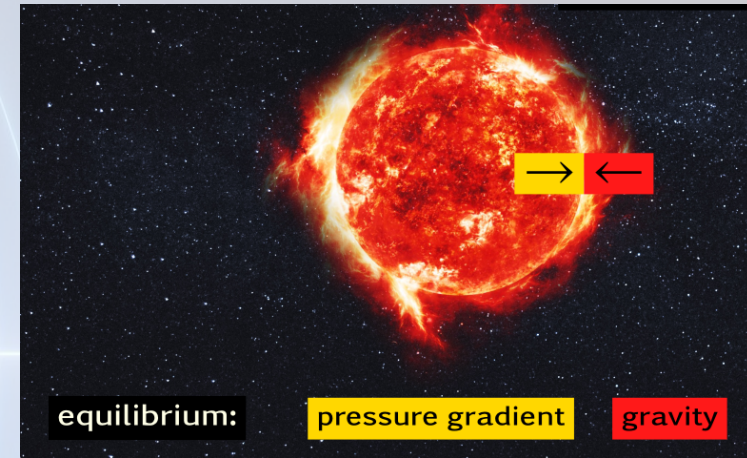


**For a 25 solar mass star:**

Stage	Duration
H → He	$7 \times 10^6$ years
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Core Collapse	1/4 second

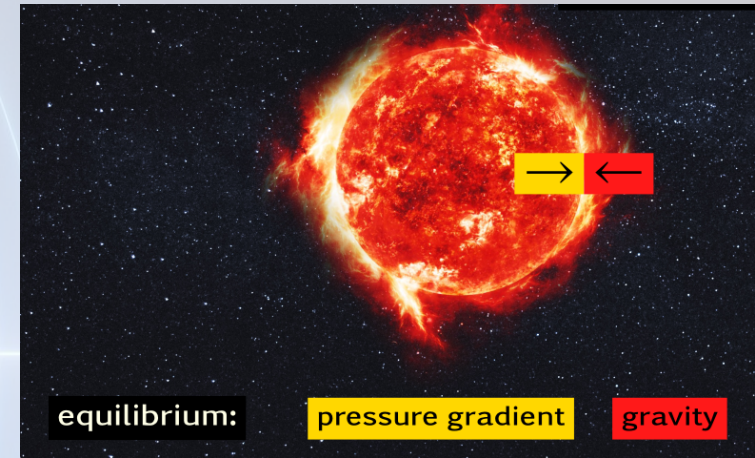
# Core collapse

- Gravity takes over
  - end of the long-term equilibrium
  - fall-in: on the free-fall timescale



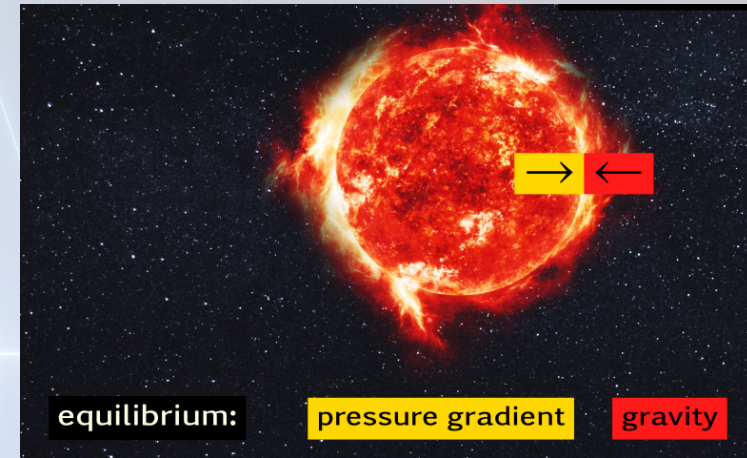
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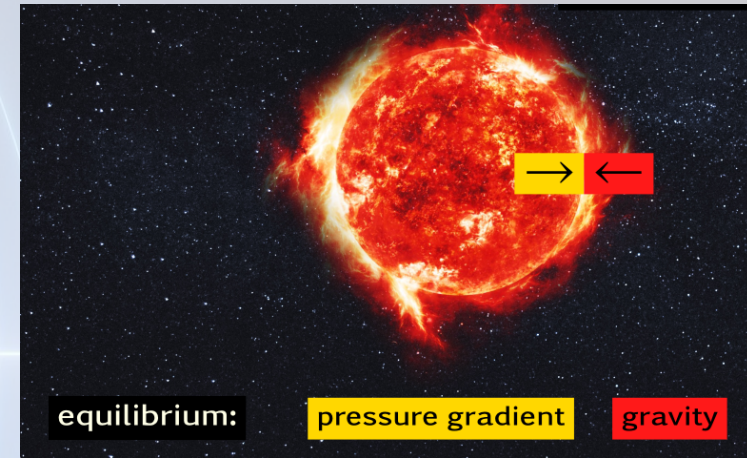
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  - Most of the time (“classical” case): a neutron star forms in the center (“proto-neutron-star”)





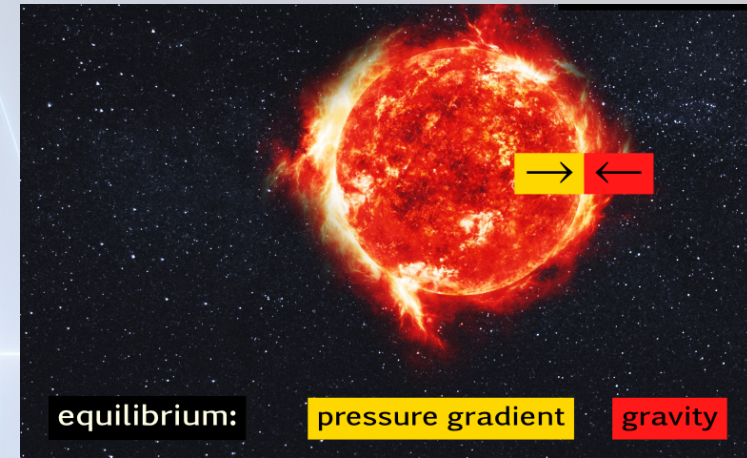
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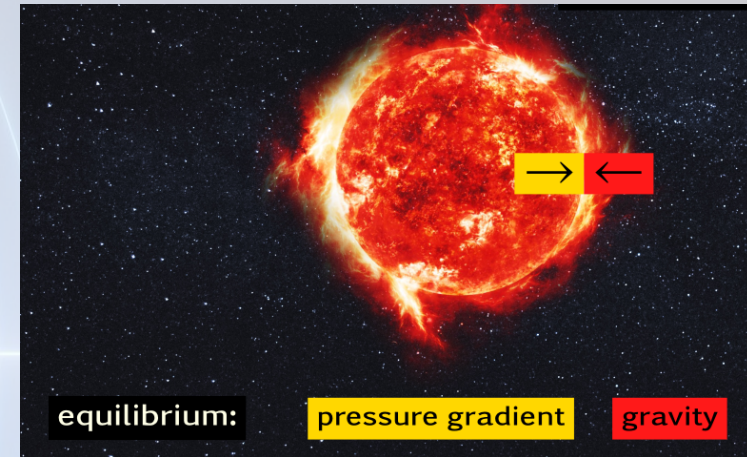
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    - bounce-back, shock waves, emission of neutrinos and light = **SUPERNOVA EXPLOSION**

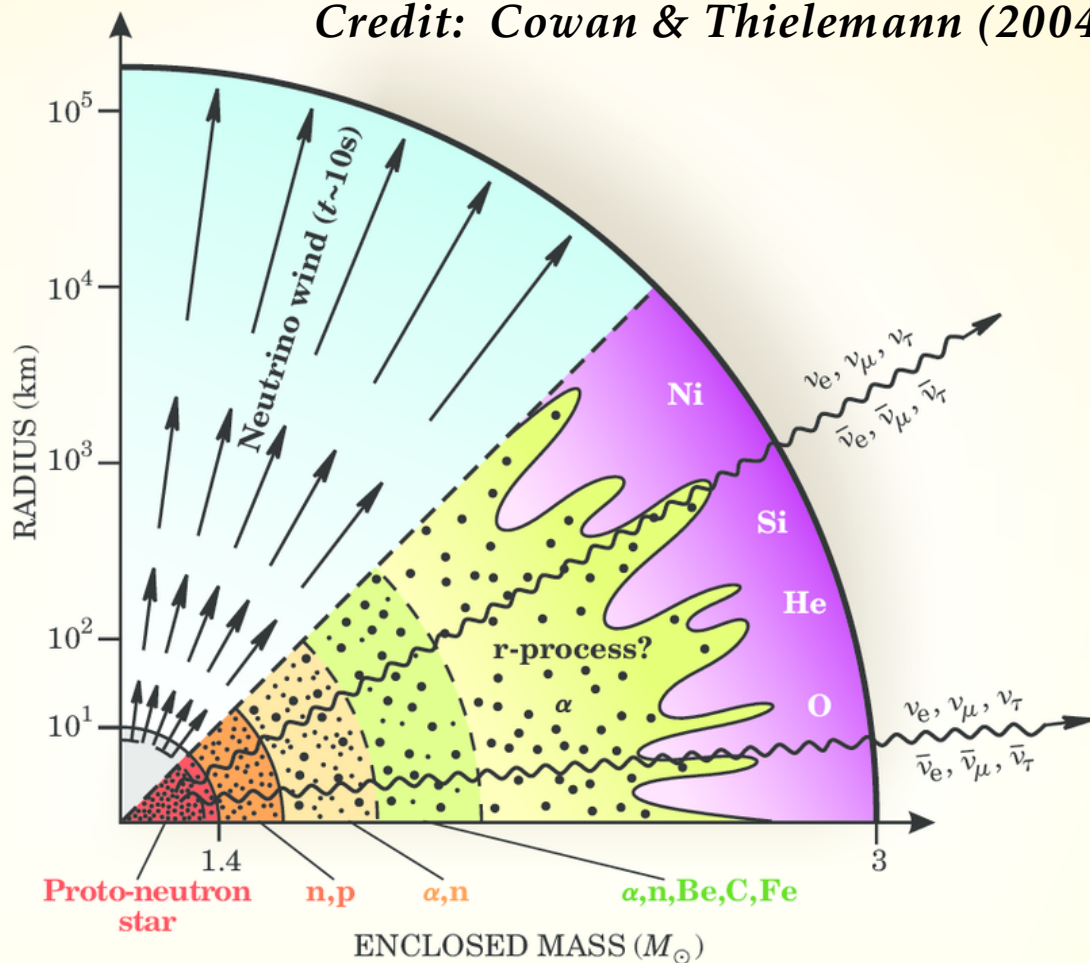


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  - technically: a core-collapse supernova (CCSN)

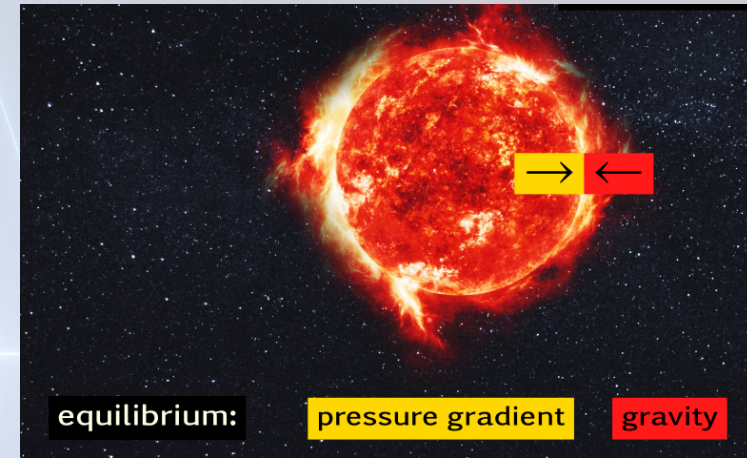


Credit: Cowan & Thielemann (2004)



collapse

um  
ale  
it?



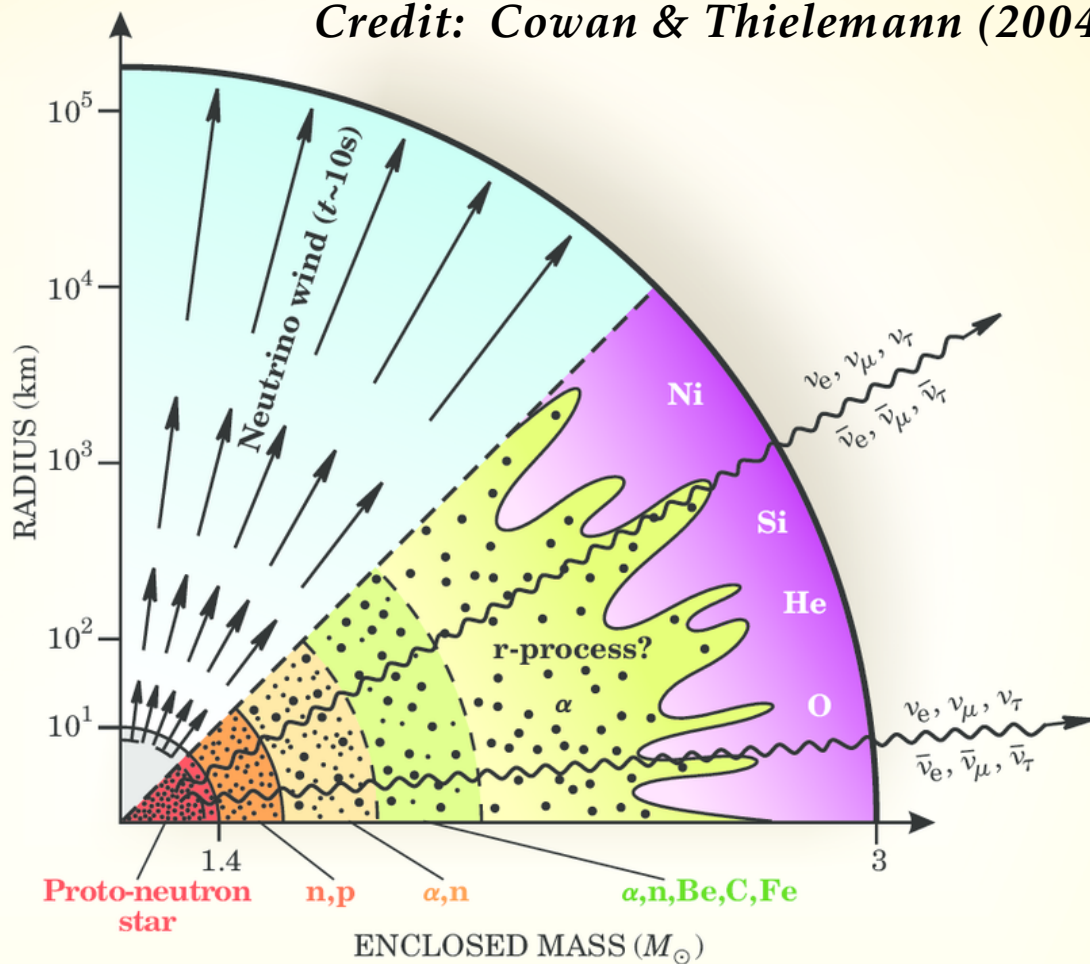
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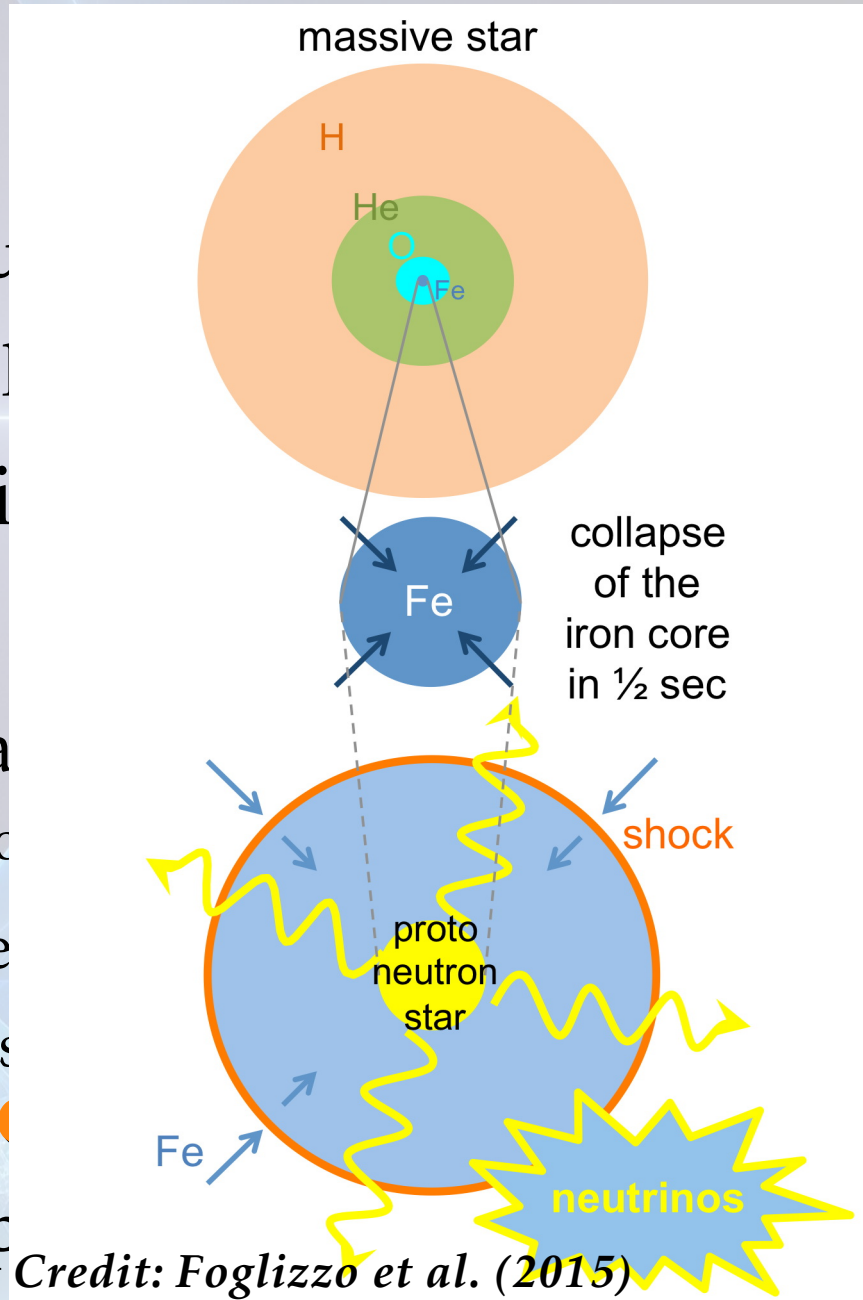
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Credit: Cowan & Thielemann (2004)



# apse

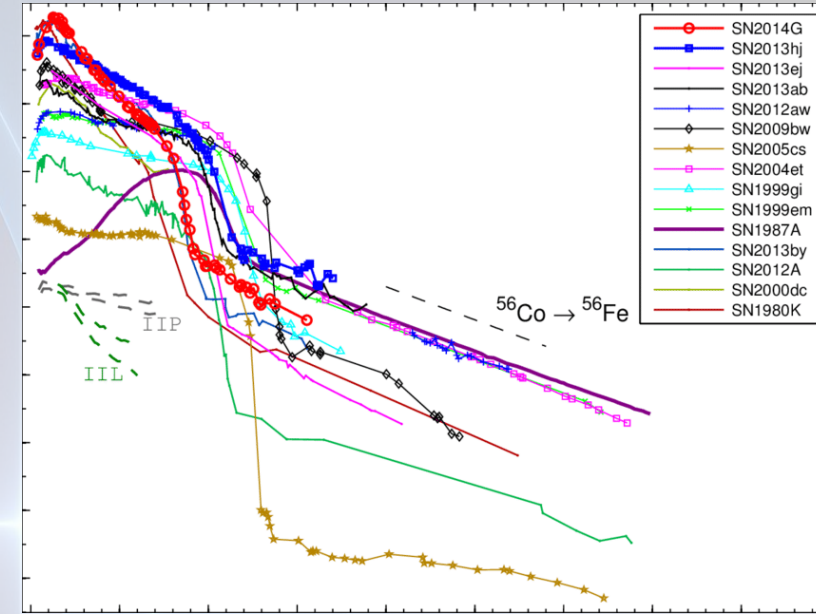
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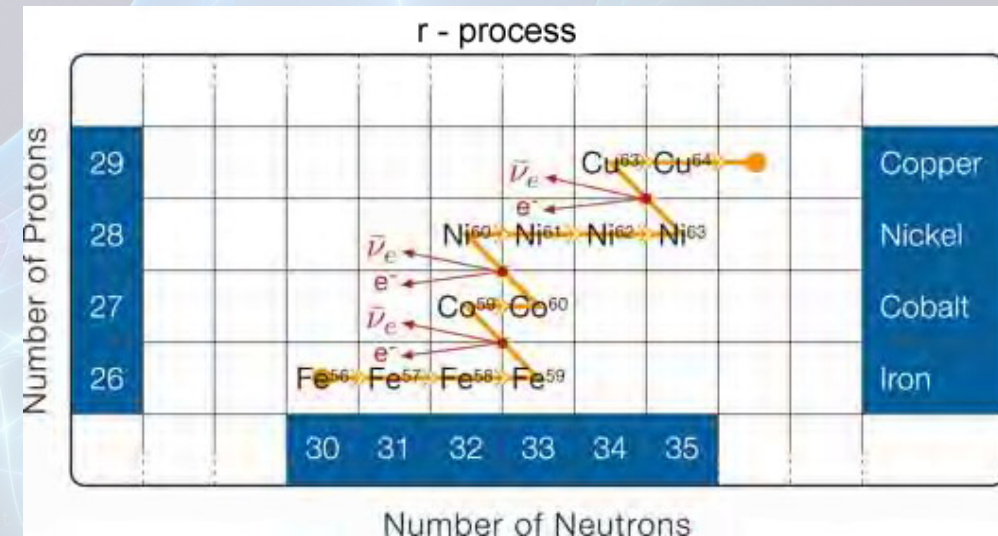
Credit: Foglizzo et al. (2015)

# Results of a CCSN

- supernova lightcurve
  - photons: emitted in the shock
  - observed at many wavelenths = *spectrum*
  - decay phase:  $^{56}\text{Co} \rightarrow ^{56}\text{Fe}$
- explosive nuclear burning: r-process (**rapid**)
  - lots of free neutrons: rapid neutron-capture
  - elements heavier than iron
- remnant: NS... or BH



credit: Bose, Kumar et al. (2015)



# Fate of the proto-NS

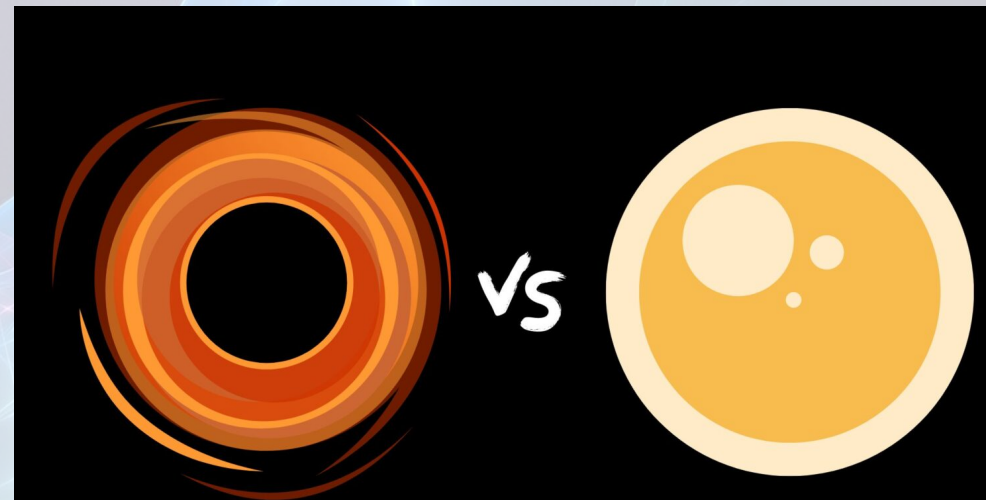
- depends on the mass of the object
  - $M_{\text{ini}} < \sim 20 M_{\odot}$ : NS
  - $> \sim 20 M_{\odot}$ : BH
  - but... explosion physics is complicated (as is stellar evolution...)



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*under active research*

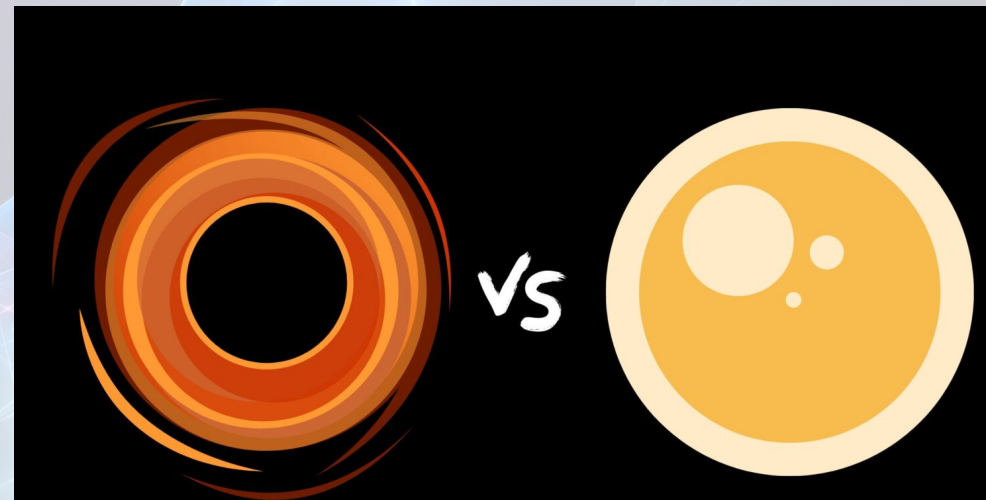




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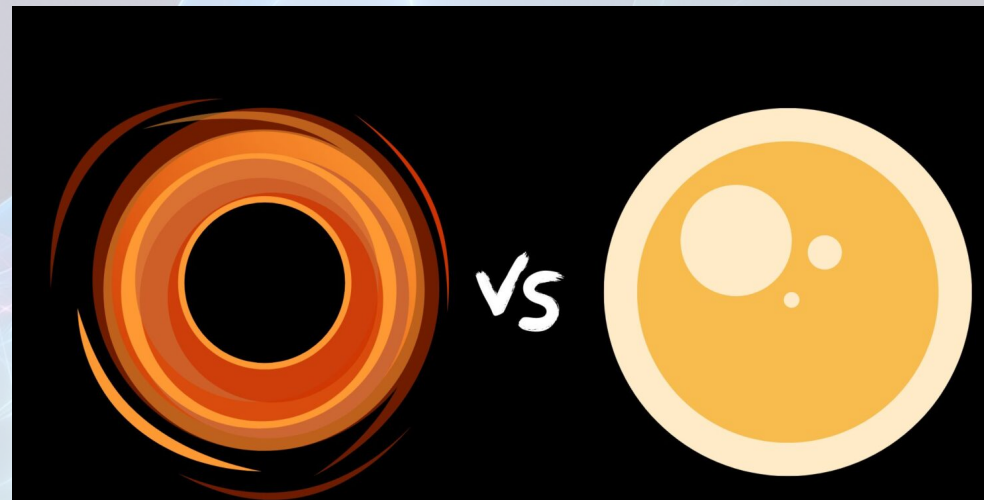
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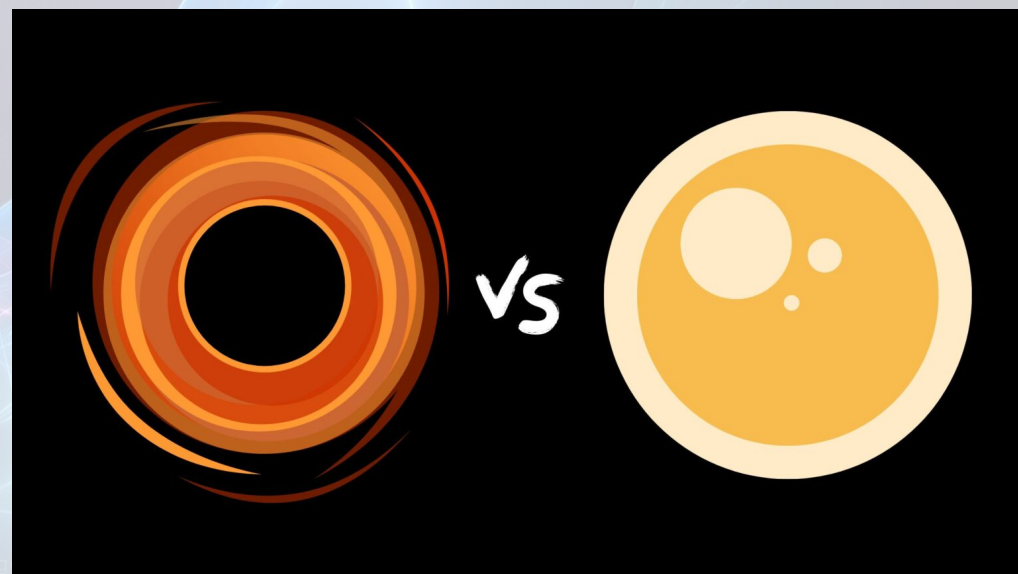


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*Not the Chandrasekhar limit!  $\sim 1.4 M_{\odot}$  (= limit between NSs and white dwarfs)*

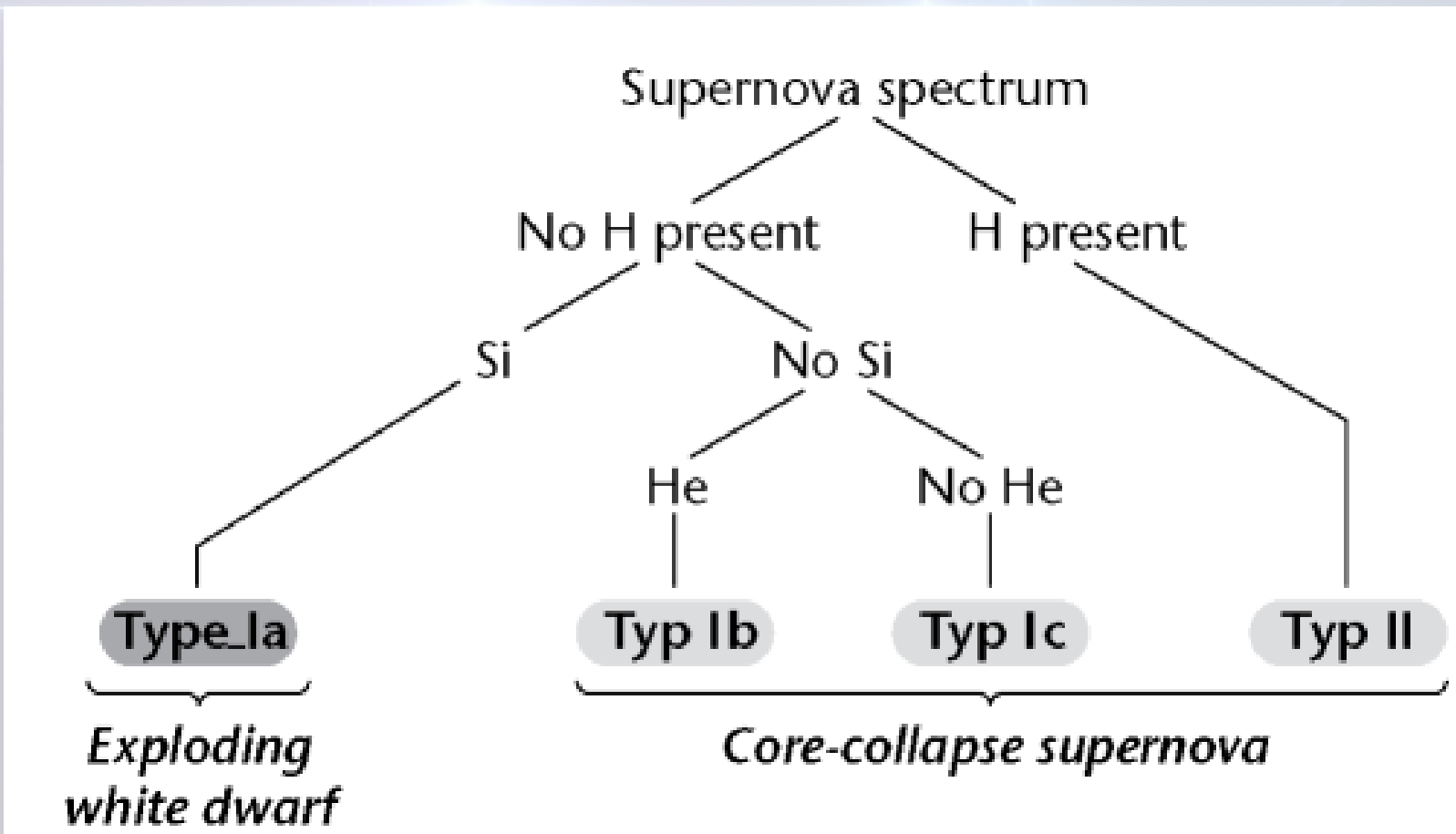


# So far: core-collapse SNe

- There are so many other types...

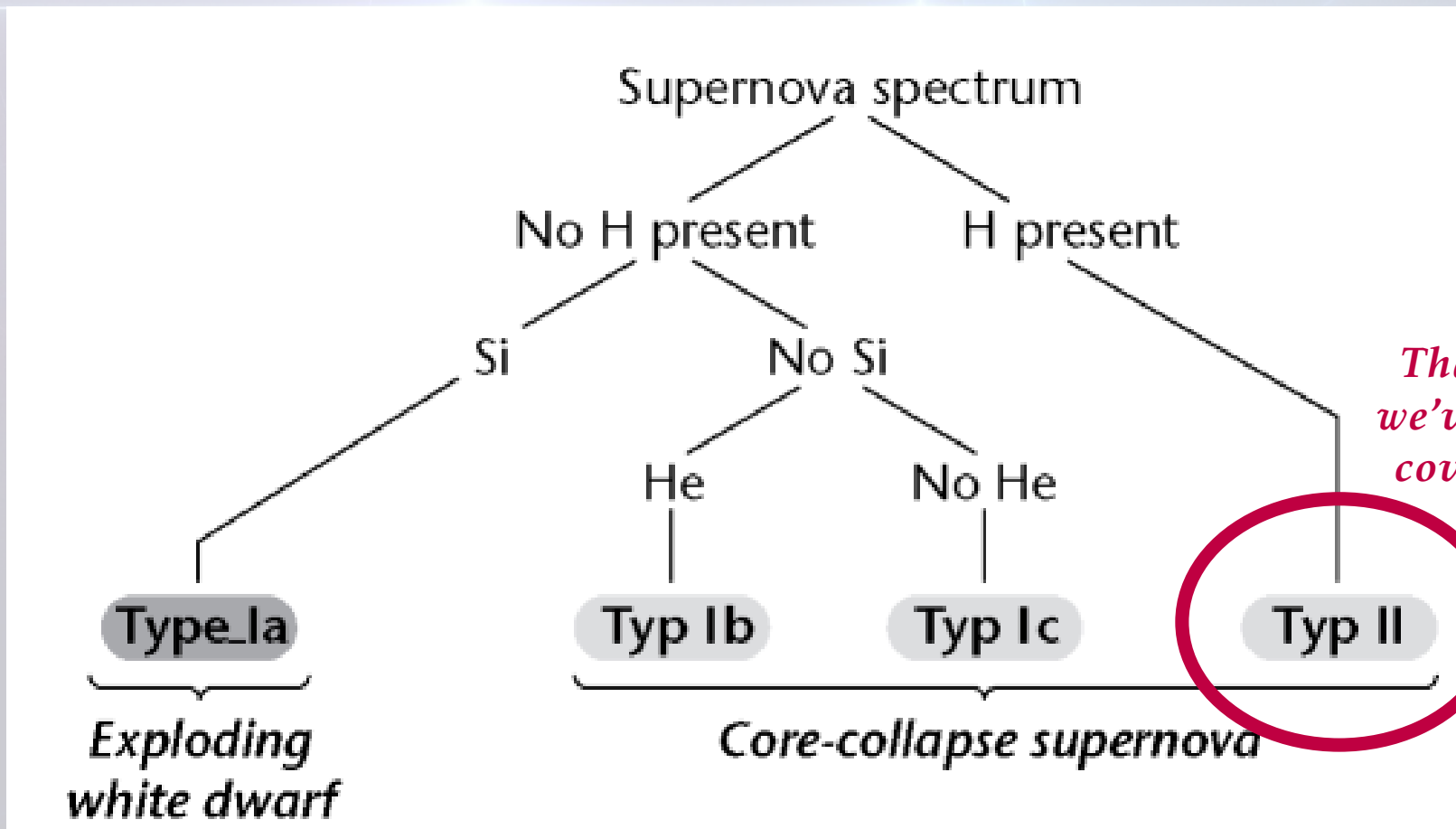
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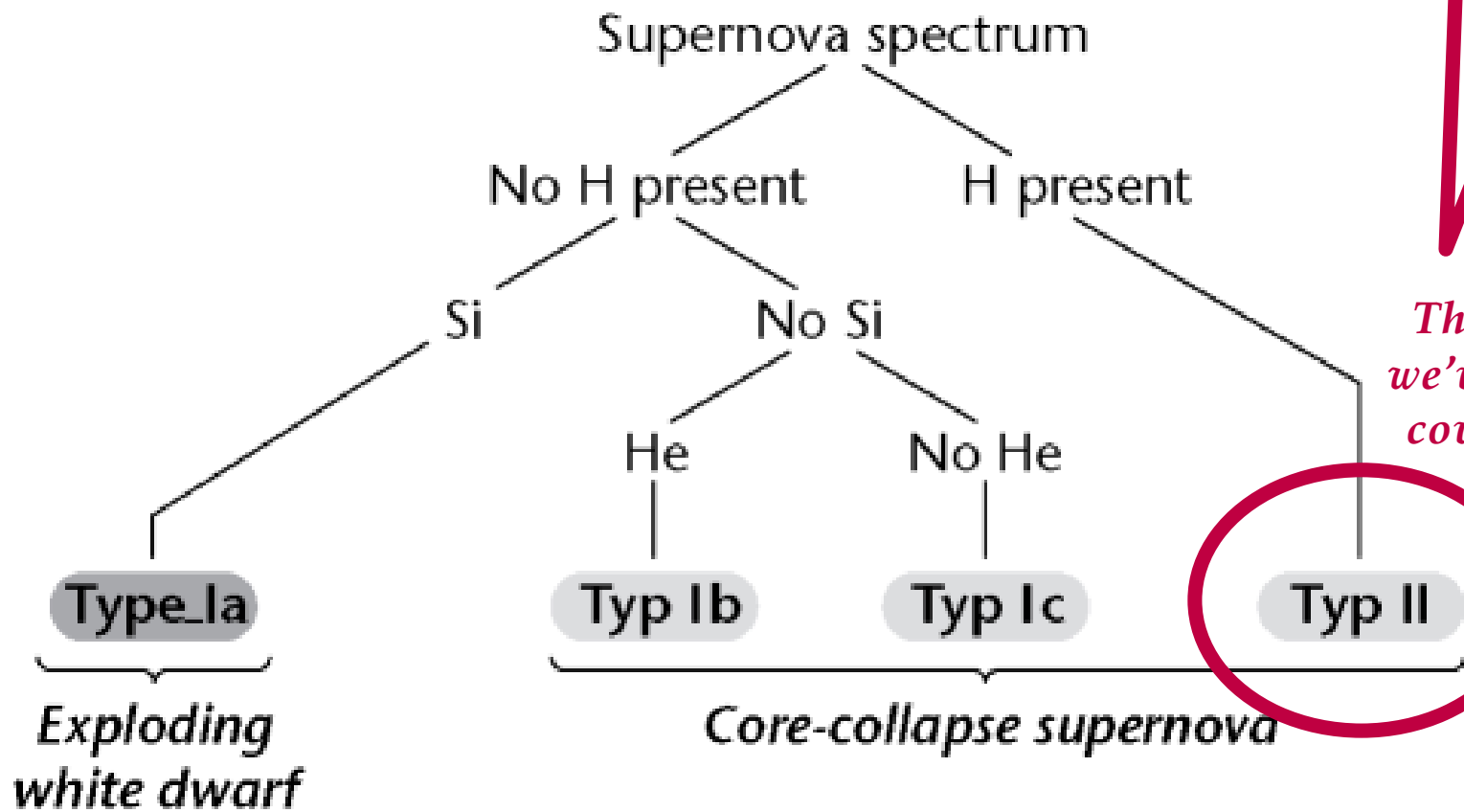
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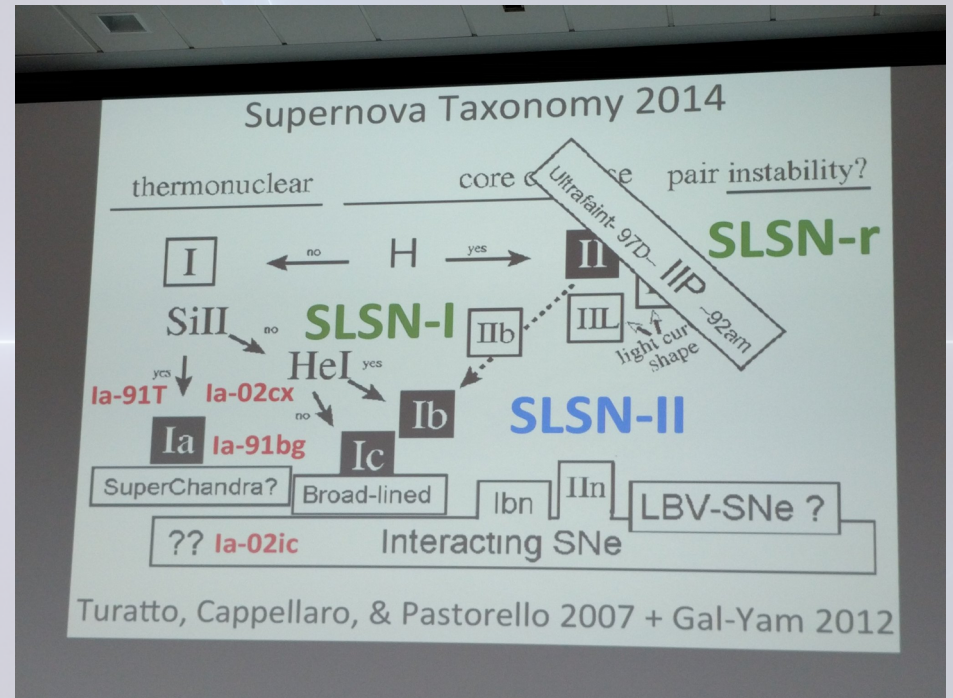
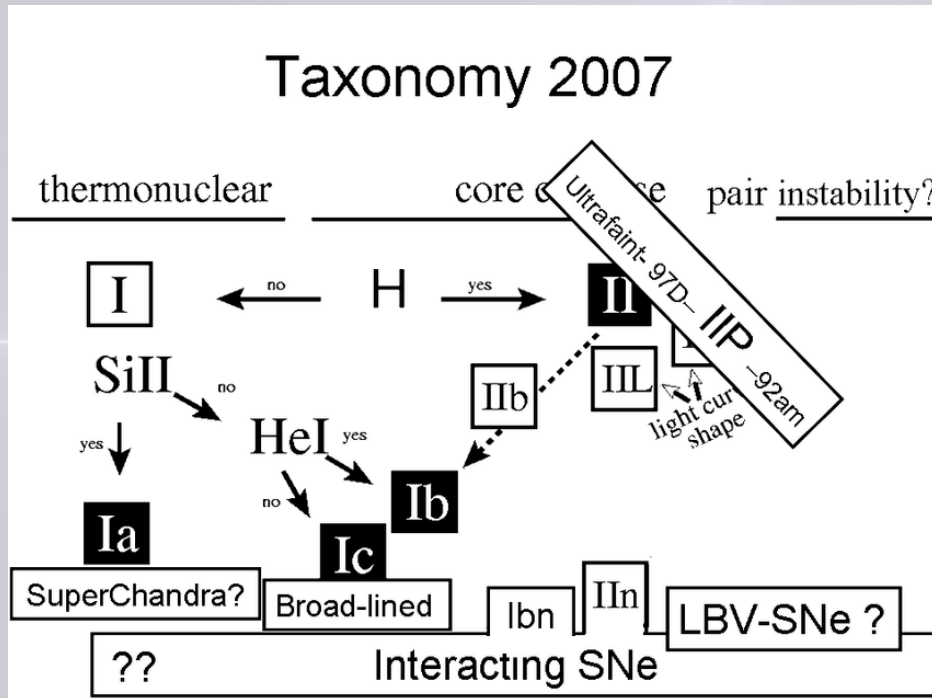
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*Progenitor:*  
a massive star with  
a H-rich envelope

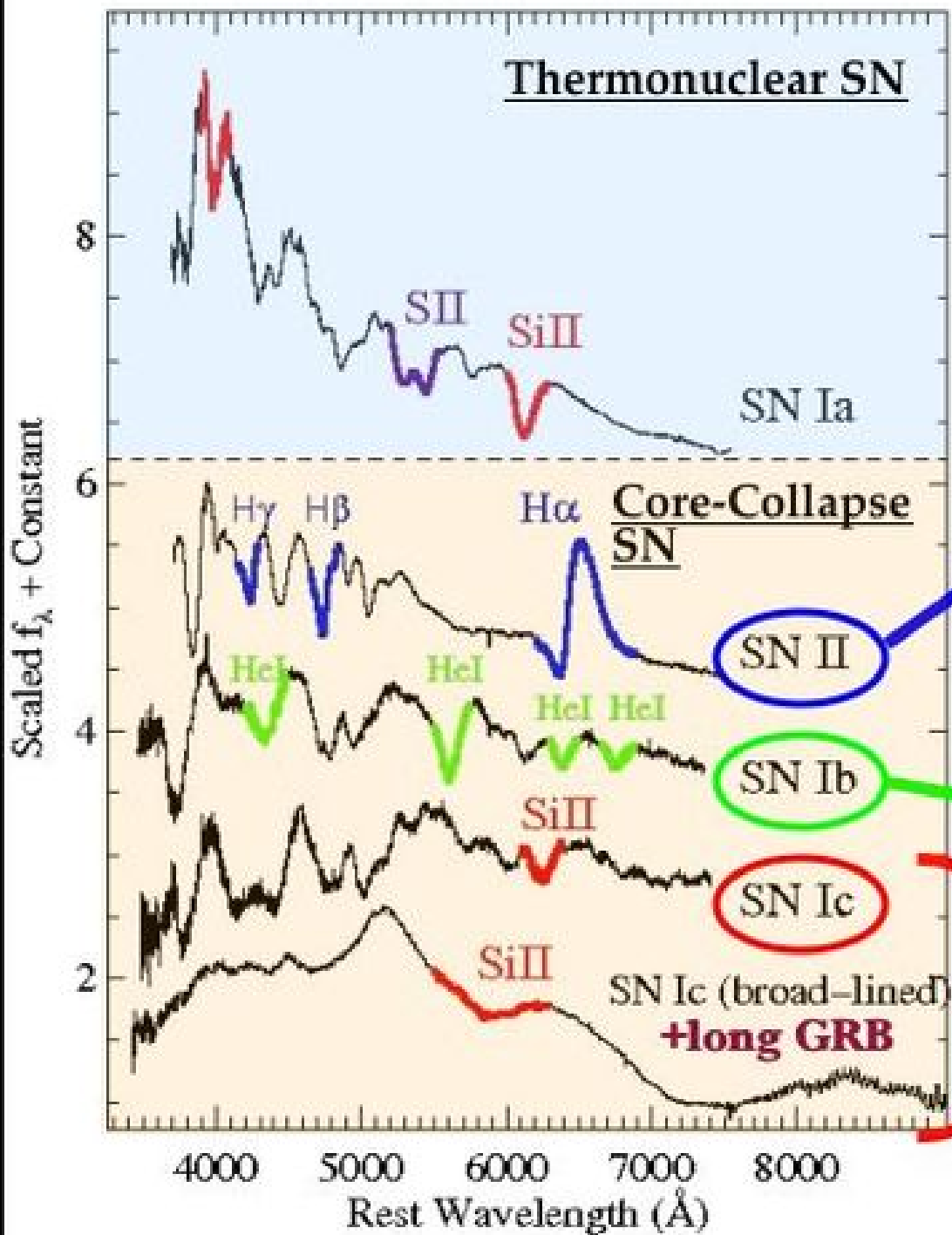


# Full supernova taxonomy *as of 2022?*

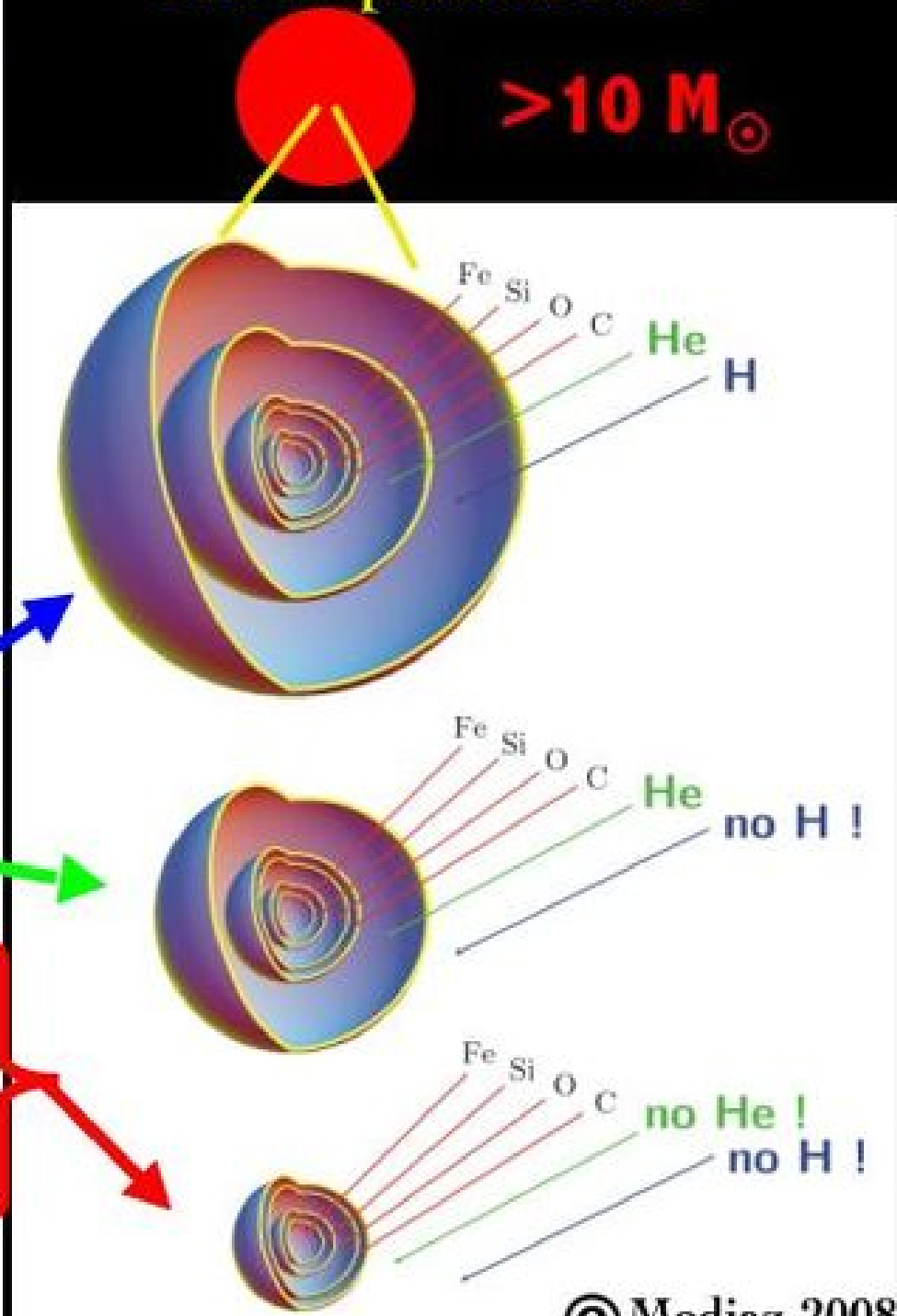




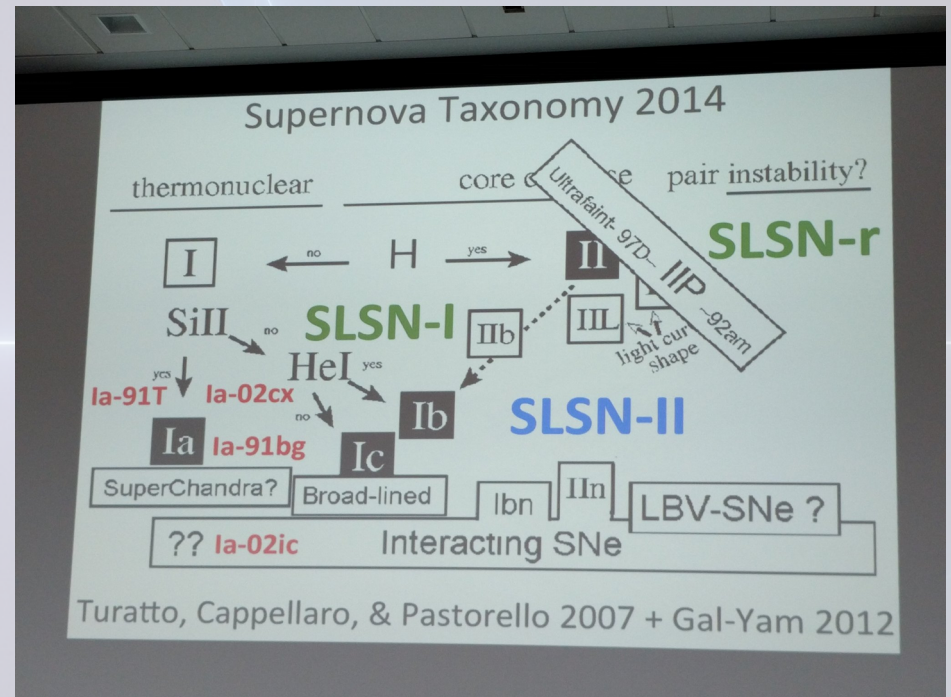
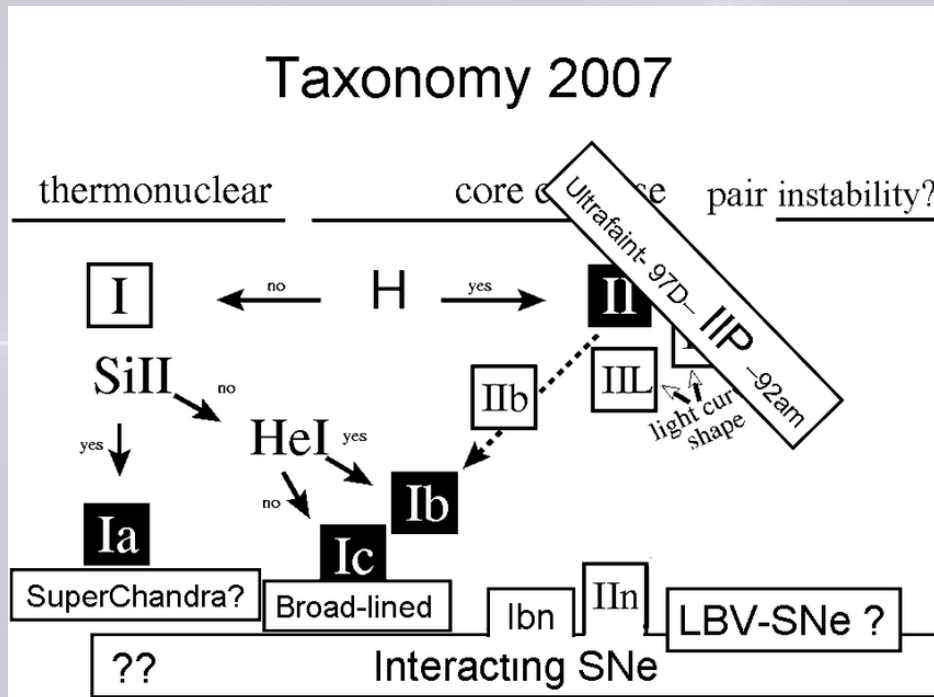
# SN Classification



# Pre-Explosion Star



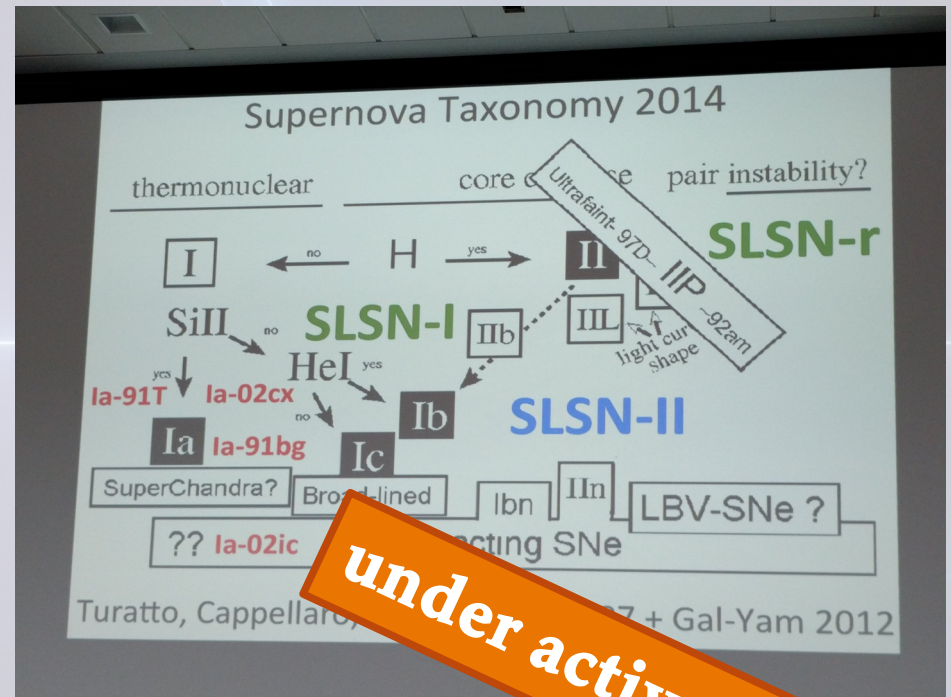
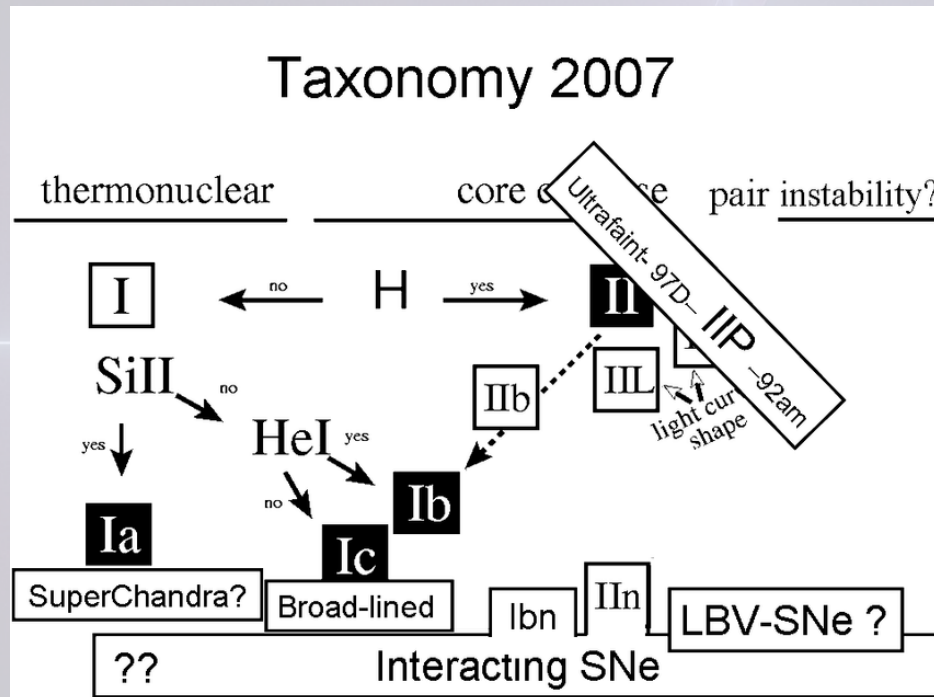
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*Need to consider additionally (at the very least):*

- rotation (leading to e.g. Gamma-ray bursts or Superluminous SNe)
- pair-creation mechanism (leading to Pair Instability Supernovae, PISNe)
- binarity (leading to, basically, anything we want but also to GWs)

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**under active research**

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