

# Gravitational-wave progenitors

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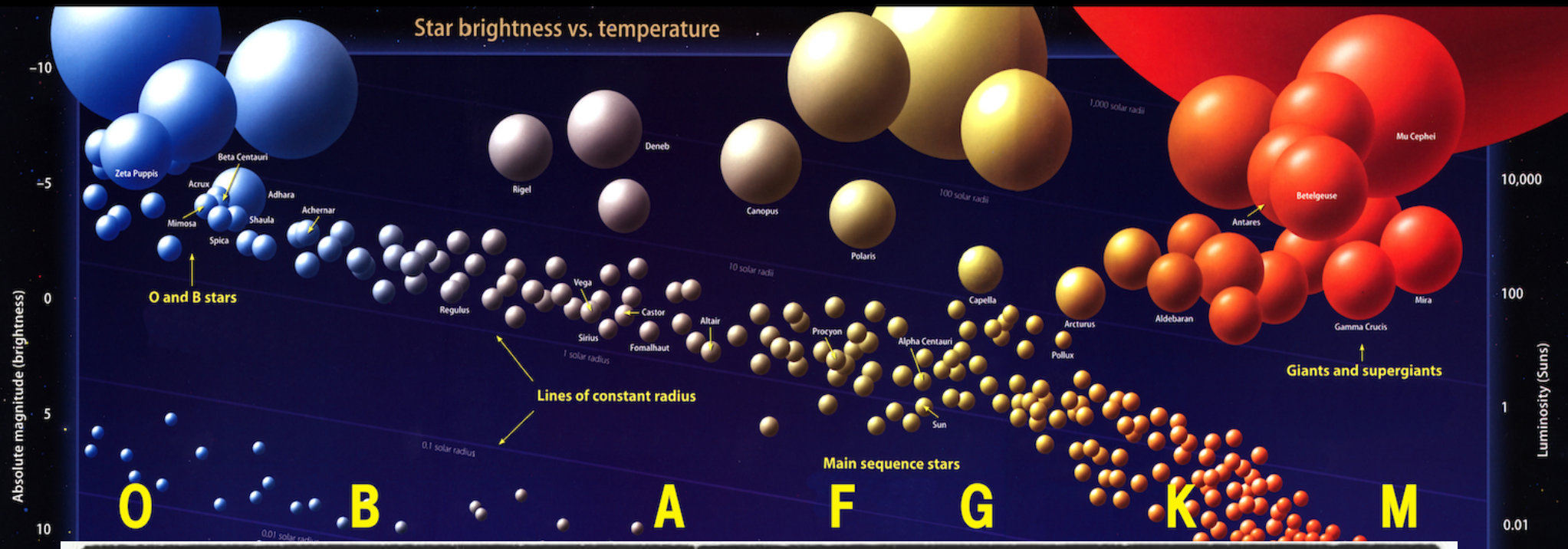
Lecture #6

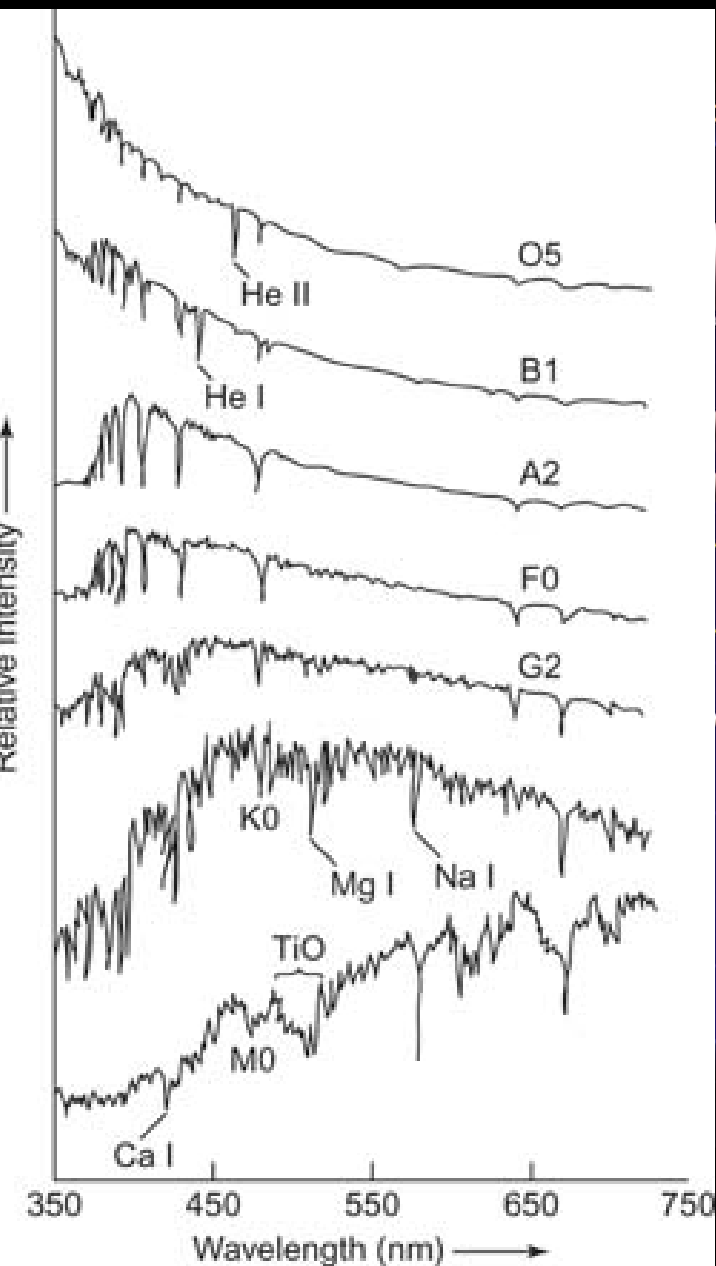
**NCU, Summer Semester 2022**



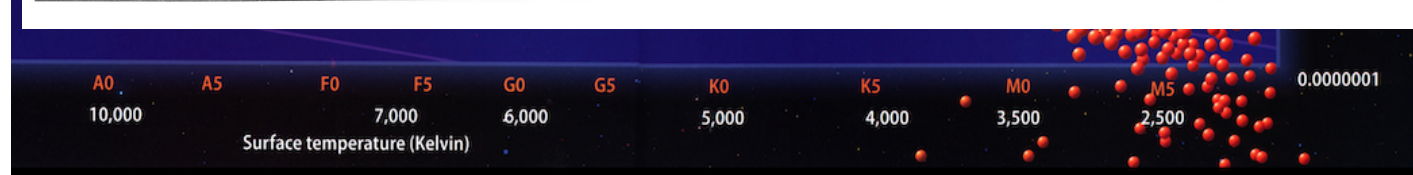
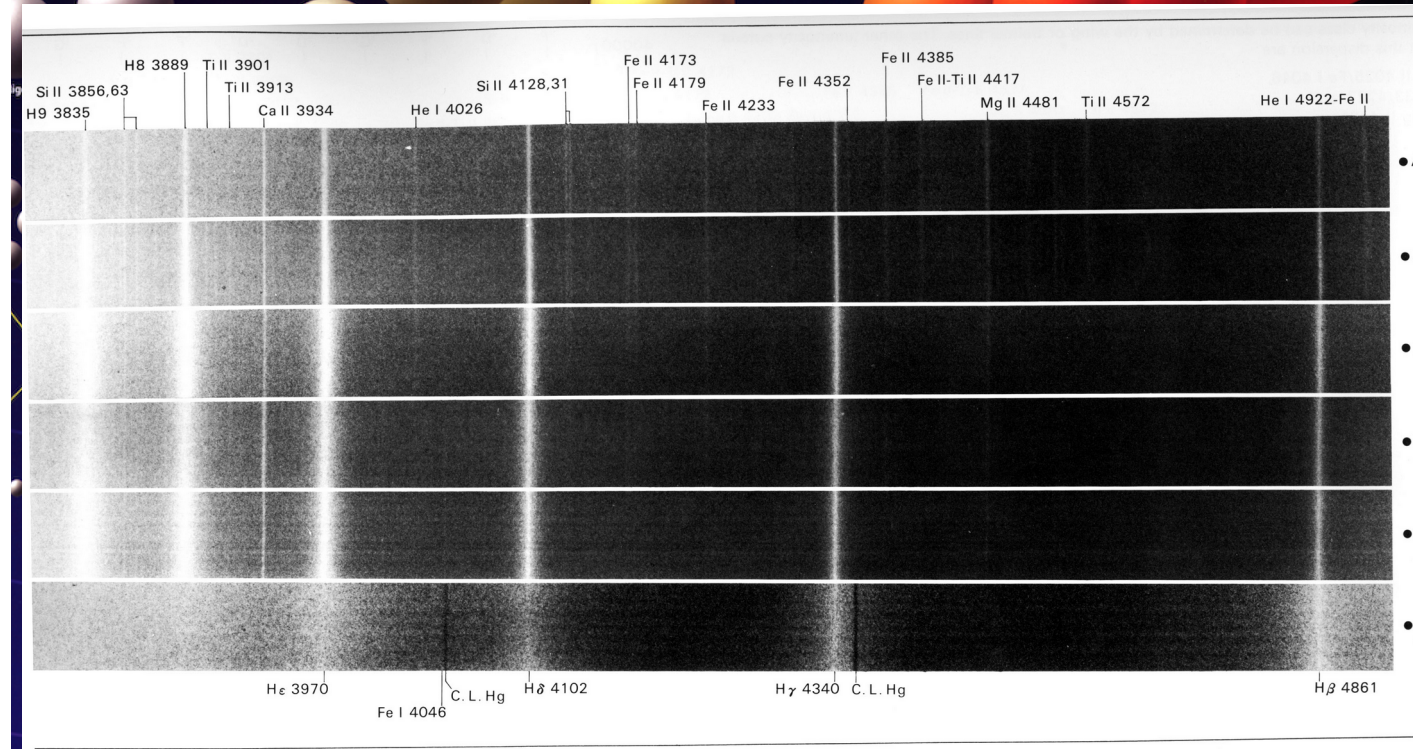
*Previously  
on GW-progenitors...*

# Star brightness vs. temperature





Mass vs. temperature



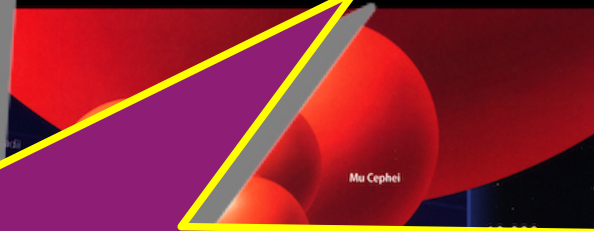
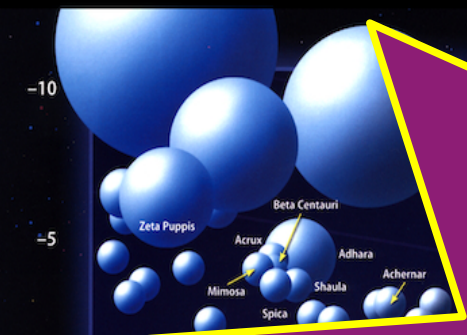
Star brightness vs. tempera

**Make sure to read more!**

Suggested article:  
"Women Astronomers  
at Harvard at the Turn of the Century"

<https://www.carleton.edu/goodsell/research/student-research/women/harvard/>

*...also: come to Torun Observatory ;) :D*



absolute magnitude (brightness)

Luminosity (Suns)

M

↑  
supergiants

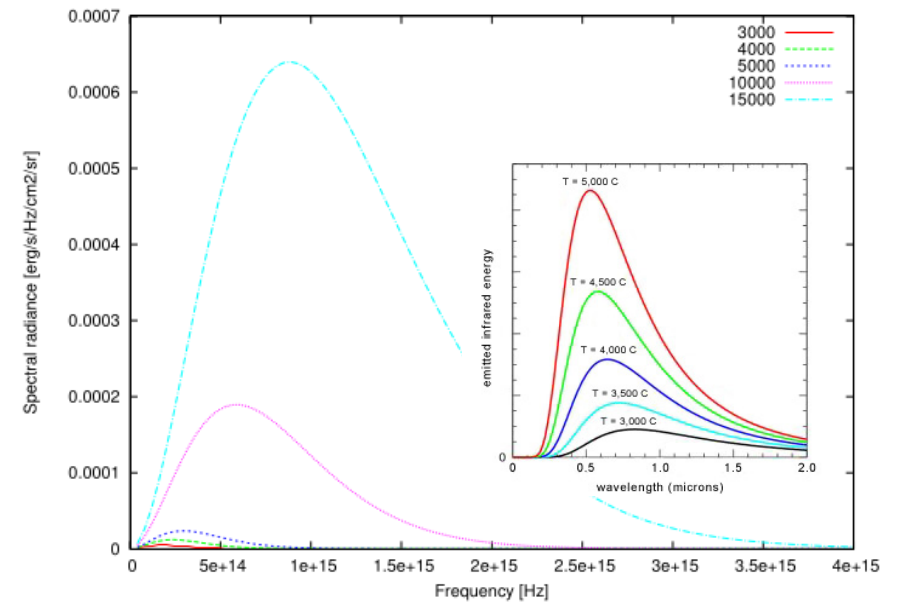
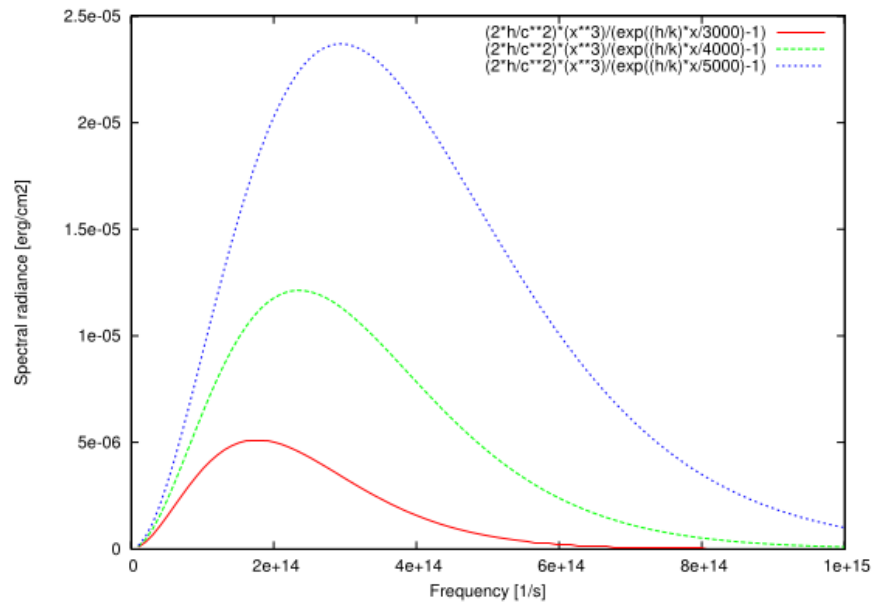
# Planck law

$$B(\nu, T_{eff}) = \frac{2h}{c^2} \frac{\nu^3}{e^{\frac{h\nu}{k_B T_{eff}}} - 1} \quad (3)$$

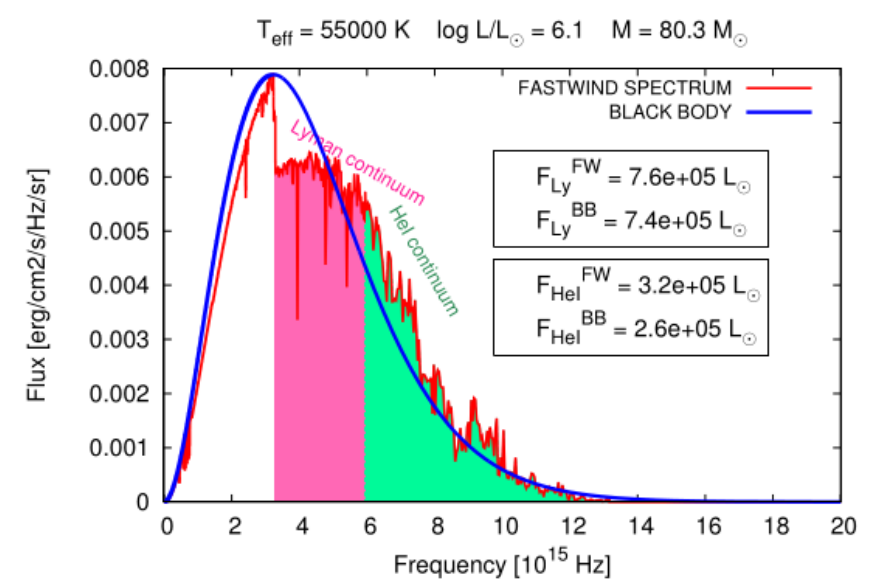
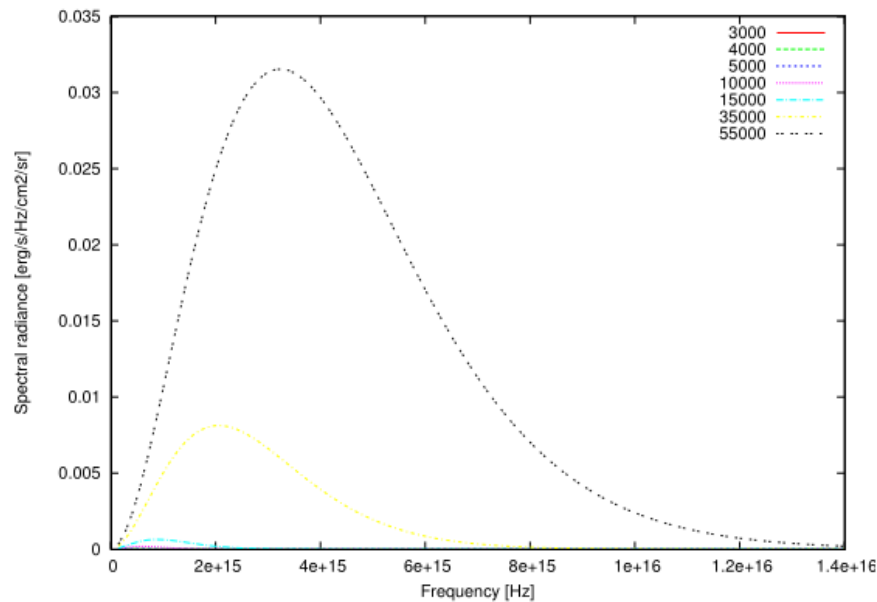
*here: as a function of frequency  
(works with wavelength as well)*

Note: there is a T value in it!

# Radiation field of stars with different $T_{eff}$

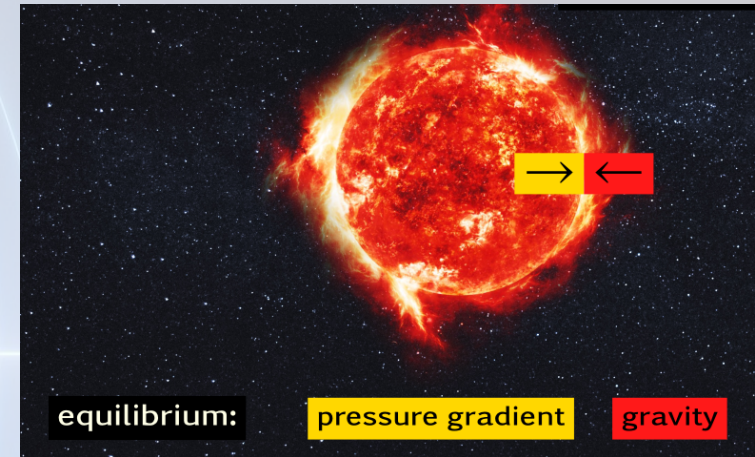


$$B(\nu, T_{eff}) = \frac{2h}{2} \frac{\nu^3}{e^{kT_{eff}} - 1} \quad (3)$$



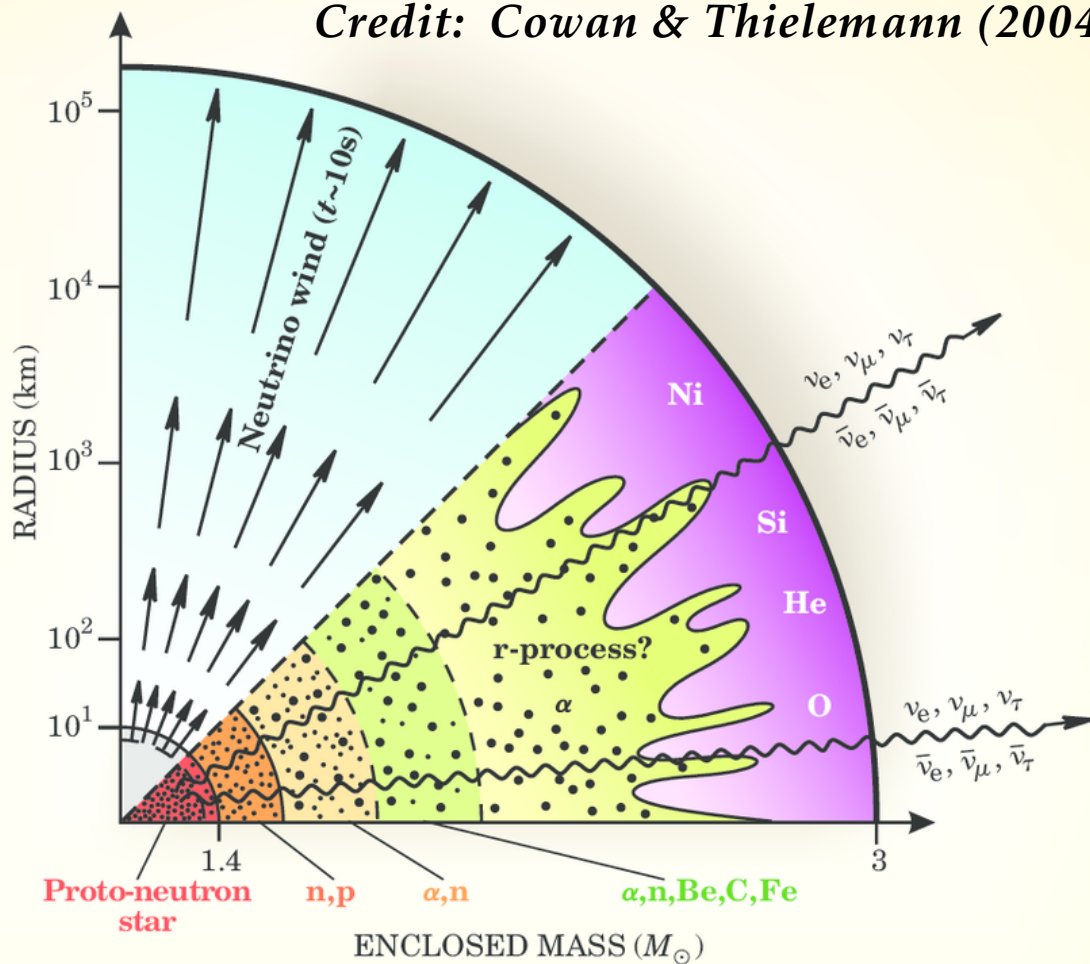
# Core collapse

- Gravity takes over
  - end of the long-term equilibrium
  - fall-in: on the free-fall timescale
- ...is there something to stop it?
  - Well... it depends.
  - Most of the time (“classical” case): a neutron star forms in the center (“proto-neutron-star”)
    - a neutron star is: one giant nucleus. dense. stable.
    - bounce-back, shock waves, emission of neutrinos and light = **SUPERNOVA EXPLOSION**



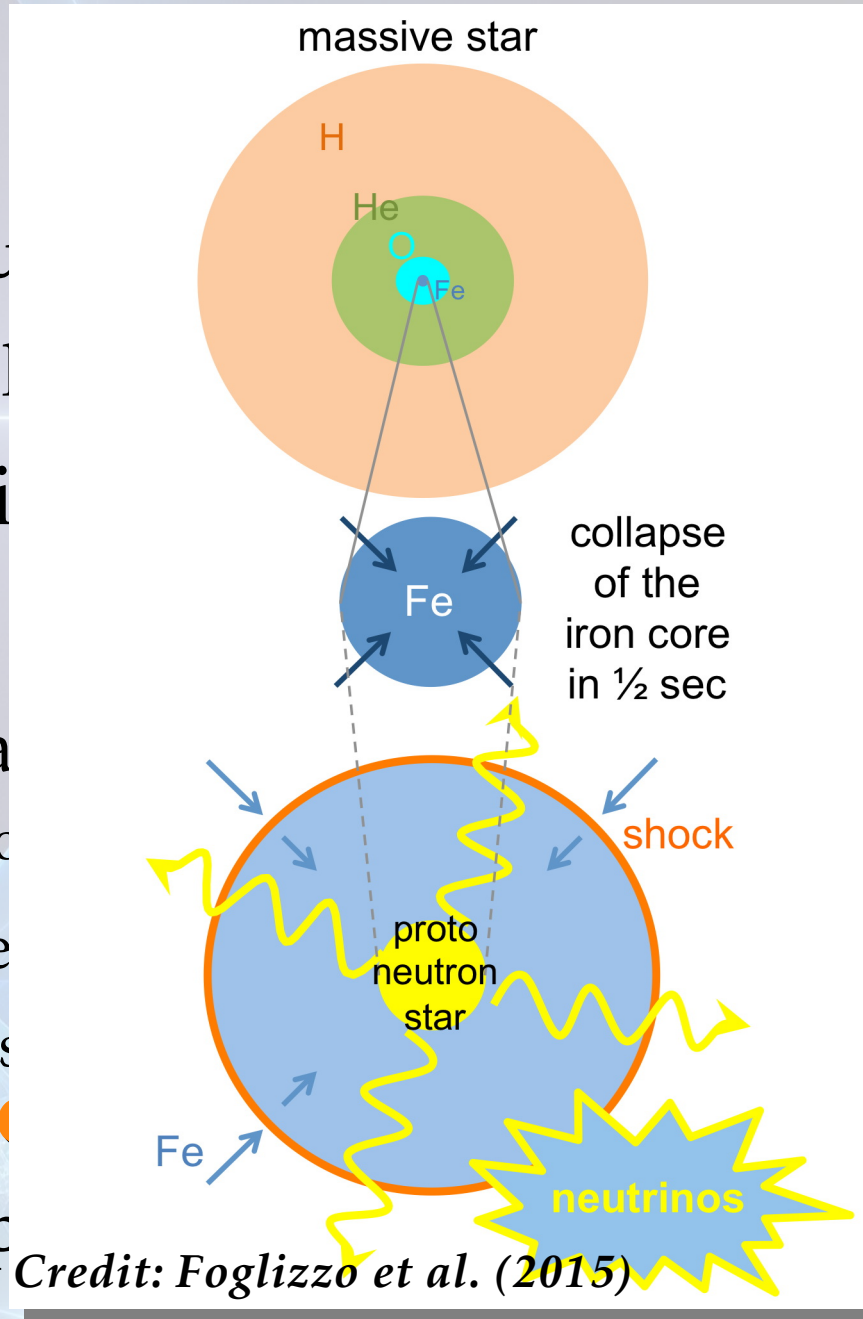


Credit: Cowan & Thielemann (2004)



# apse

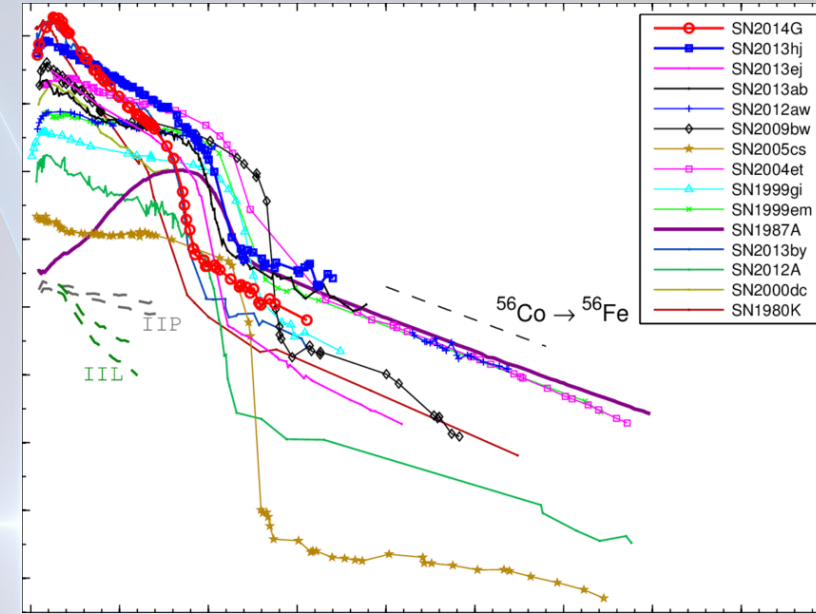
- forms in the center (“proto-neutron star”)
- a neutron star is: one giant nucle
  - bounce-back, shock waves, emiss
  - light = **SUPERNOVA EXPLOSION**
- technically: a core-collapse supernova



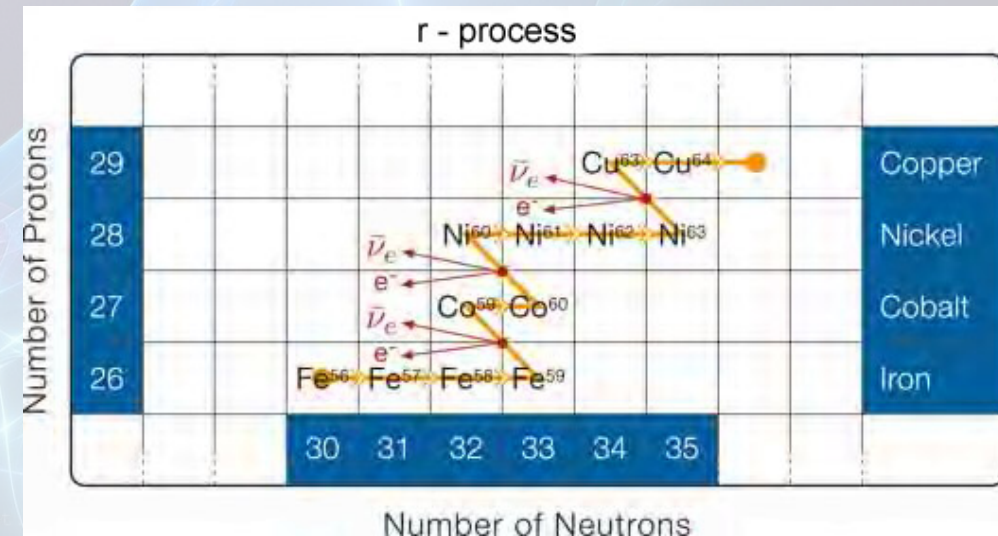
Credit: Foglizzo et al. (2015)

# Results of a CCSN

- supernova lightcurve
  - photons: emitted in the shock
  - observed at many wavelenths = *spectrum*
  - decay phase:  $^{56}\text{Co} \rightarrow ^{56}\text{Fe}$
- explosive nuclear burning: r-process (**rapid**)
  - lots of free neutrons: rapid neutron-capture
  - elements heavier than iron
- remnant: NS... or BH



credit: Bose, Kumar et al. (2015)

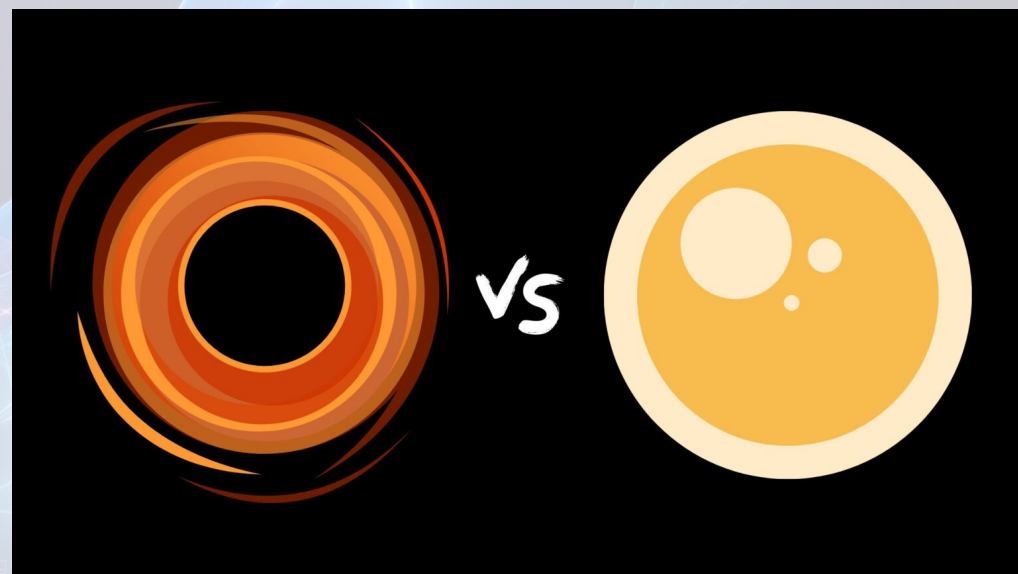


# Fate of the proto-NS

- depends on the mass of the object
  - $M_{\text{ini}} < \sim 20 M_{\odot}$ : NS
  - $> \sim 20 M_{\odot}$ : BH
  - but... explosion physics is complicated (as is stellar evolution...)
- Tolman–Oppenheimer–Volkoff limit:  **$2.16 M_{\odot}$** 
  - maximum observed mass of a neutron star is  $2.14 M_{\odot}$   
for PSR J0740+6620 discovered in 2019

*under active research*

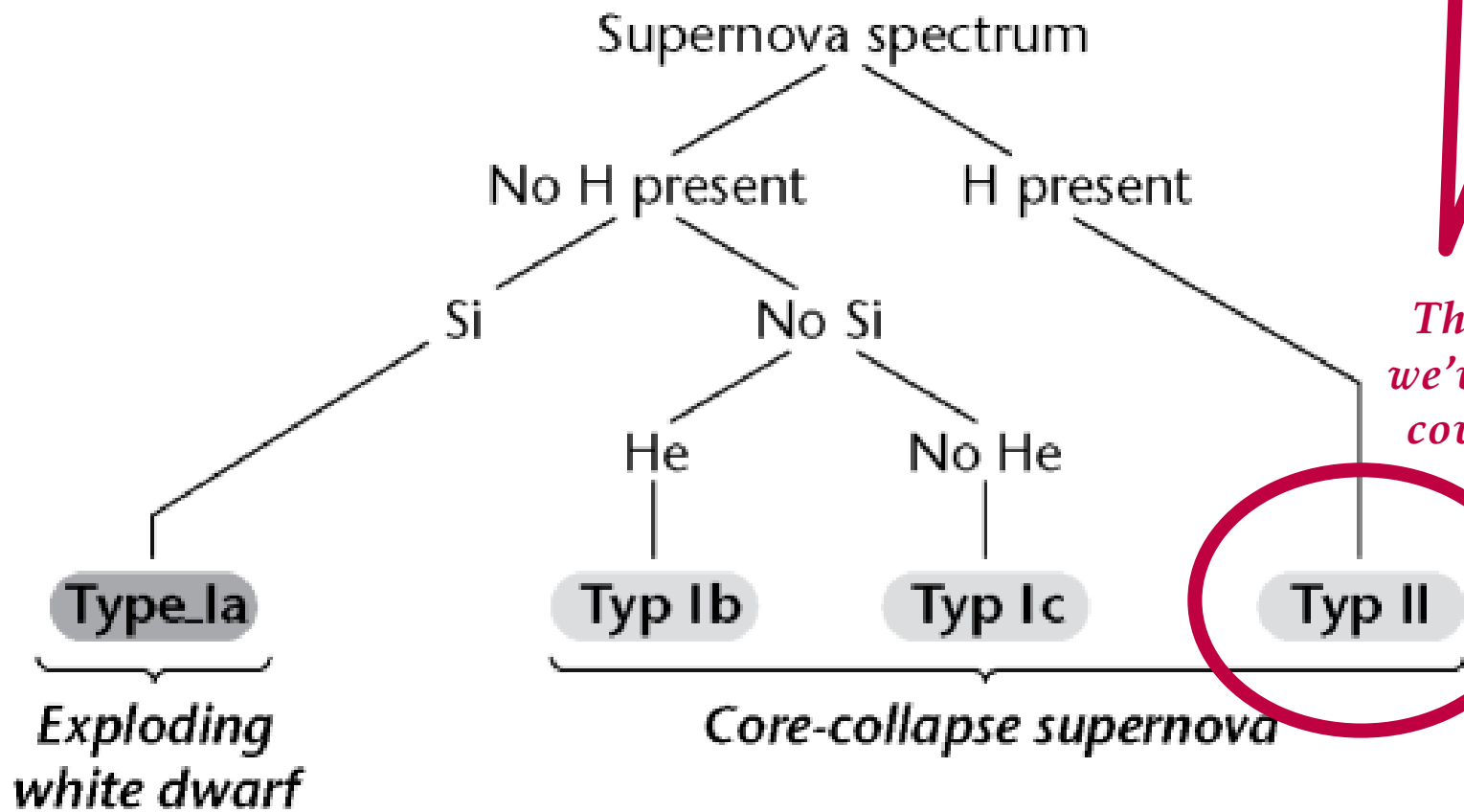
*Not the Chandrasekhar limit!  $\sim 1.4 M_{\odot}$   
(= limit between NSs and white dwarfs)*



# So far: core-collapse SNe

- There are so many other types...
- Classified by observers (simple picture):

*Progenitor:*  
a massive star with  
a H-rich envelope

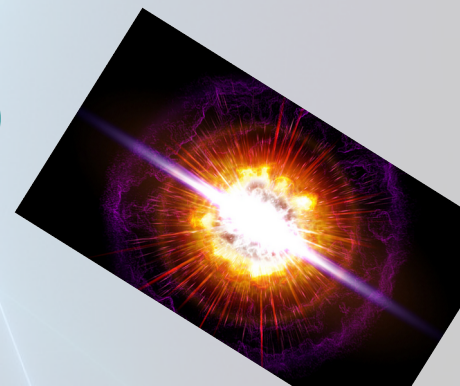




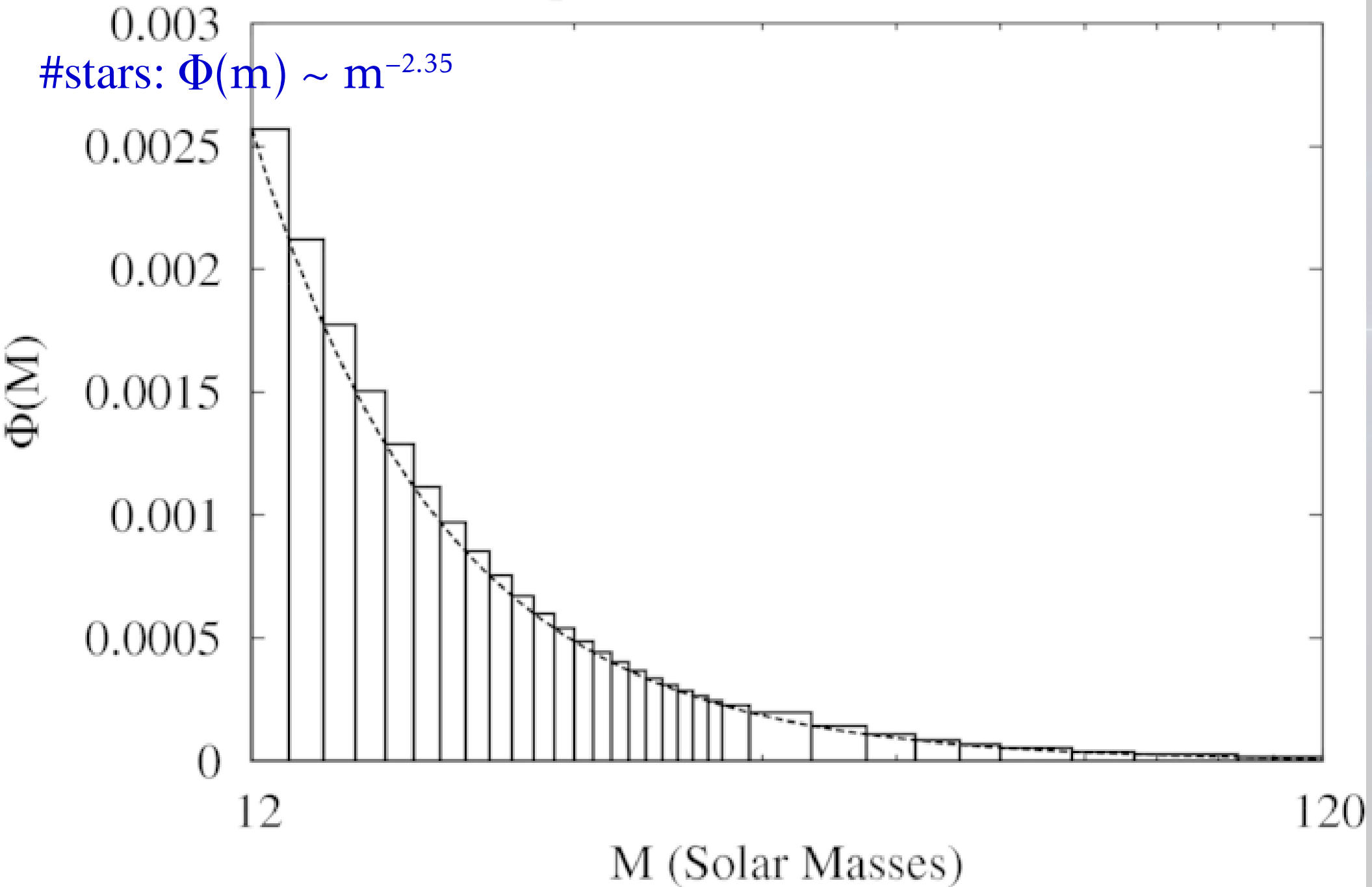
*Today...*

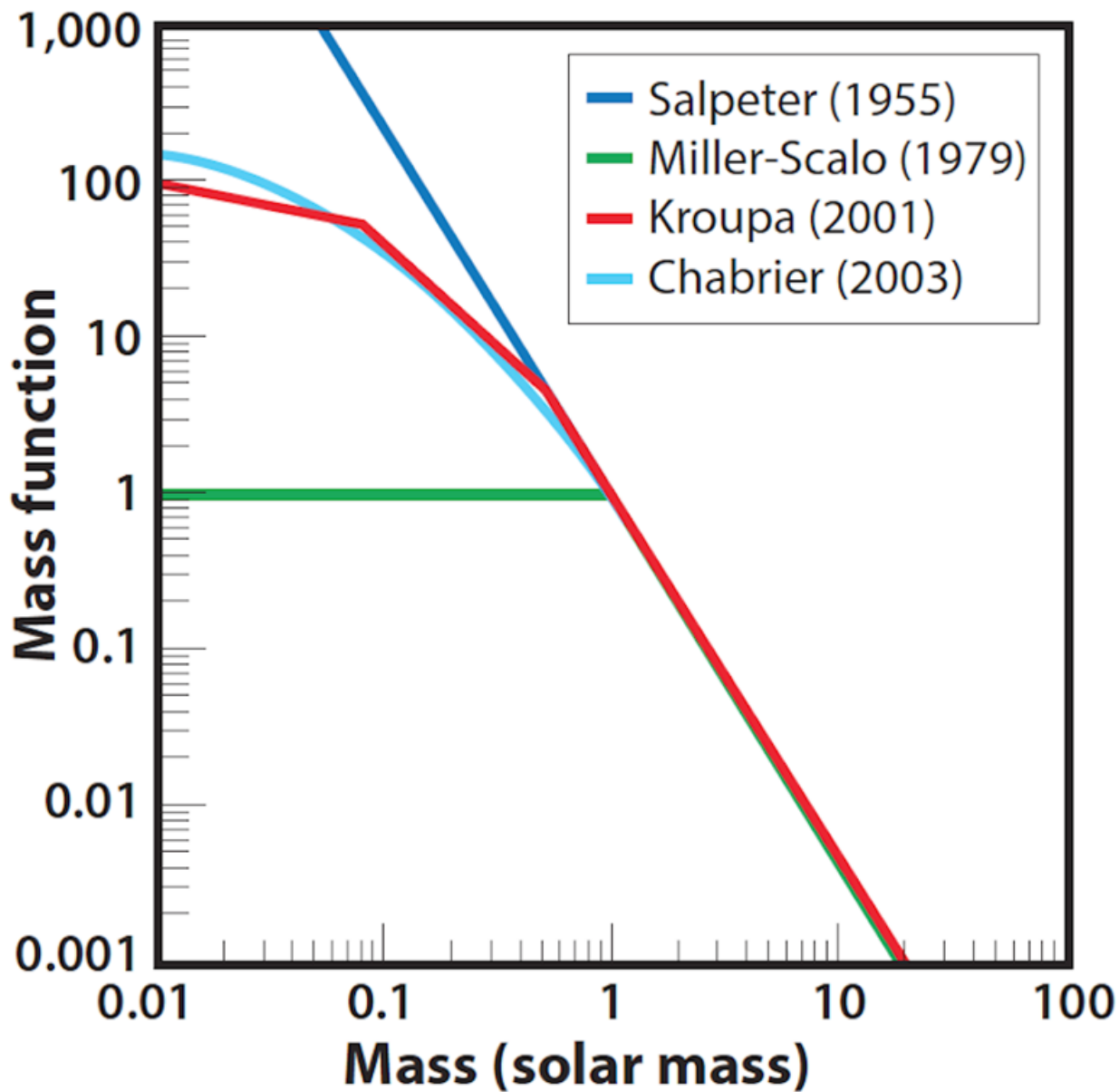
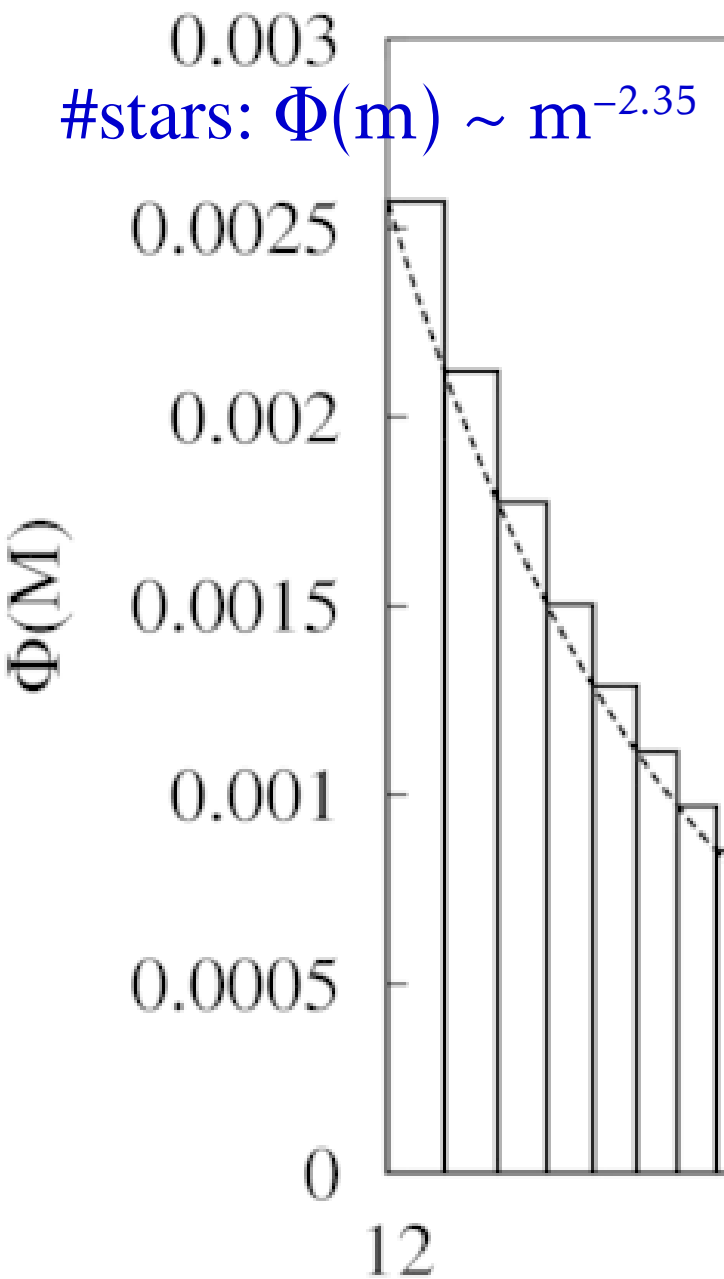
**CORPSES.**

And also: some more explosions ;)



# Salpeter Initial Mass Function



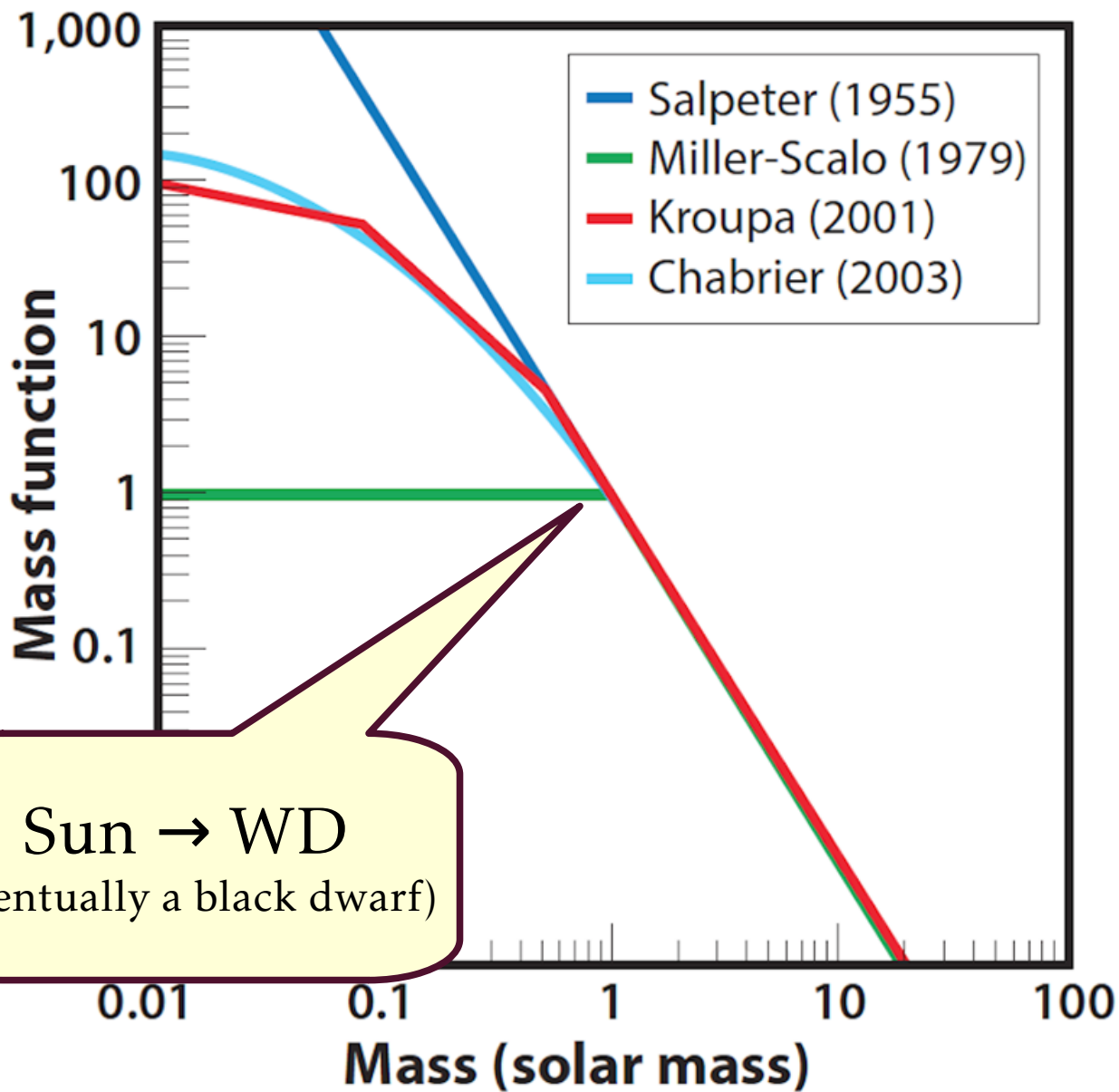
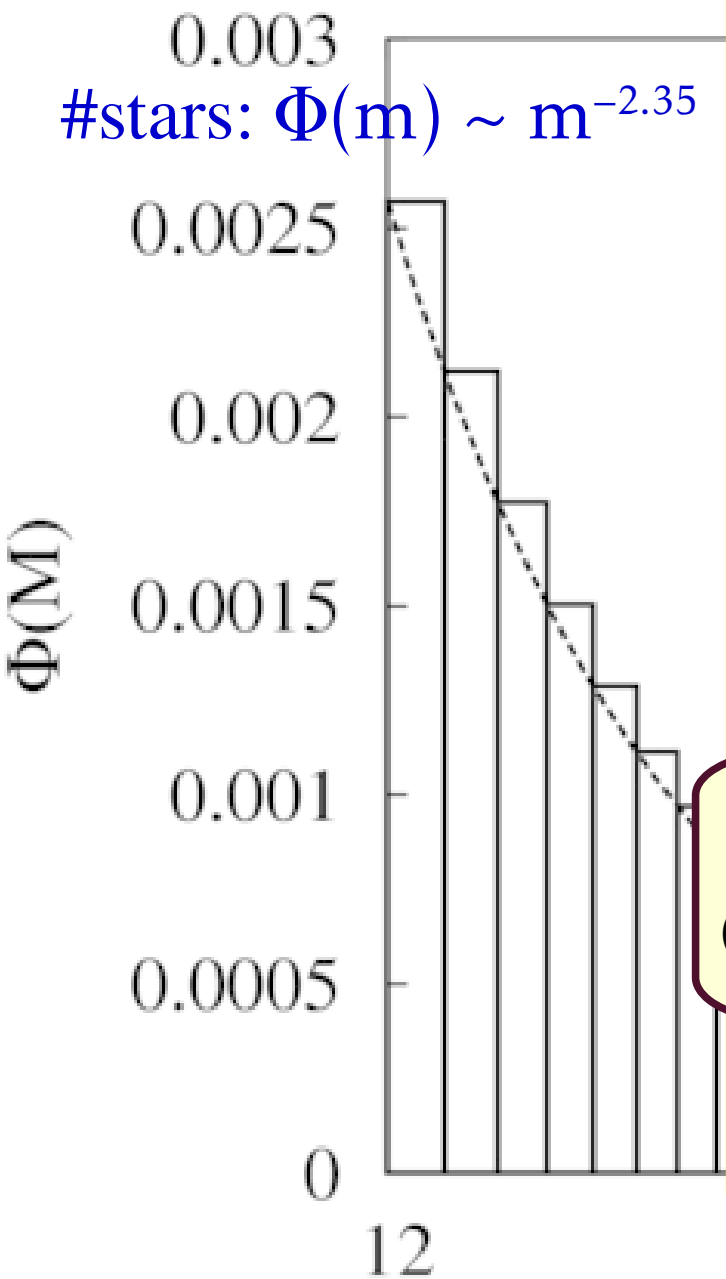


*Credit: Roen Kelly*

M (Solar Masses)

120



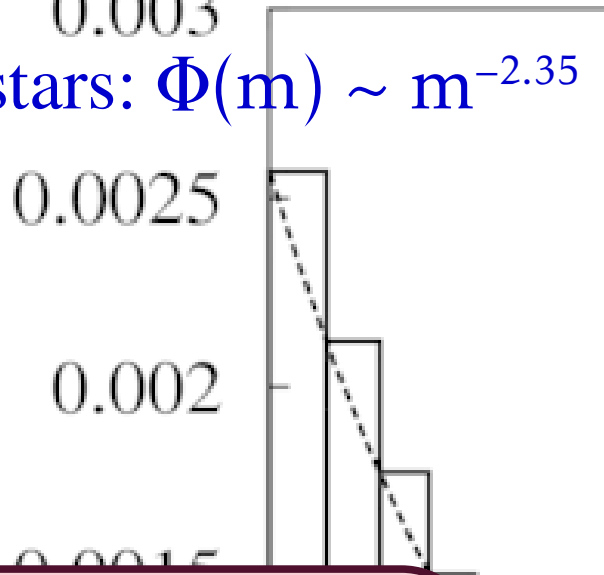


Sun  $\rightarrow$  WD  
(eventually a black dwarf)

*Credit: Roen Kelly*

M (Solar Masses)

#stars:  $\Phi(m) \sim m^{-2.35}$



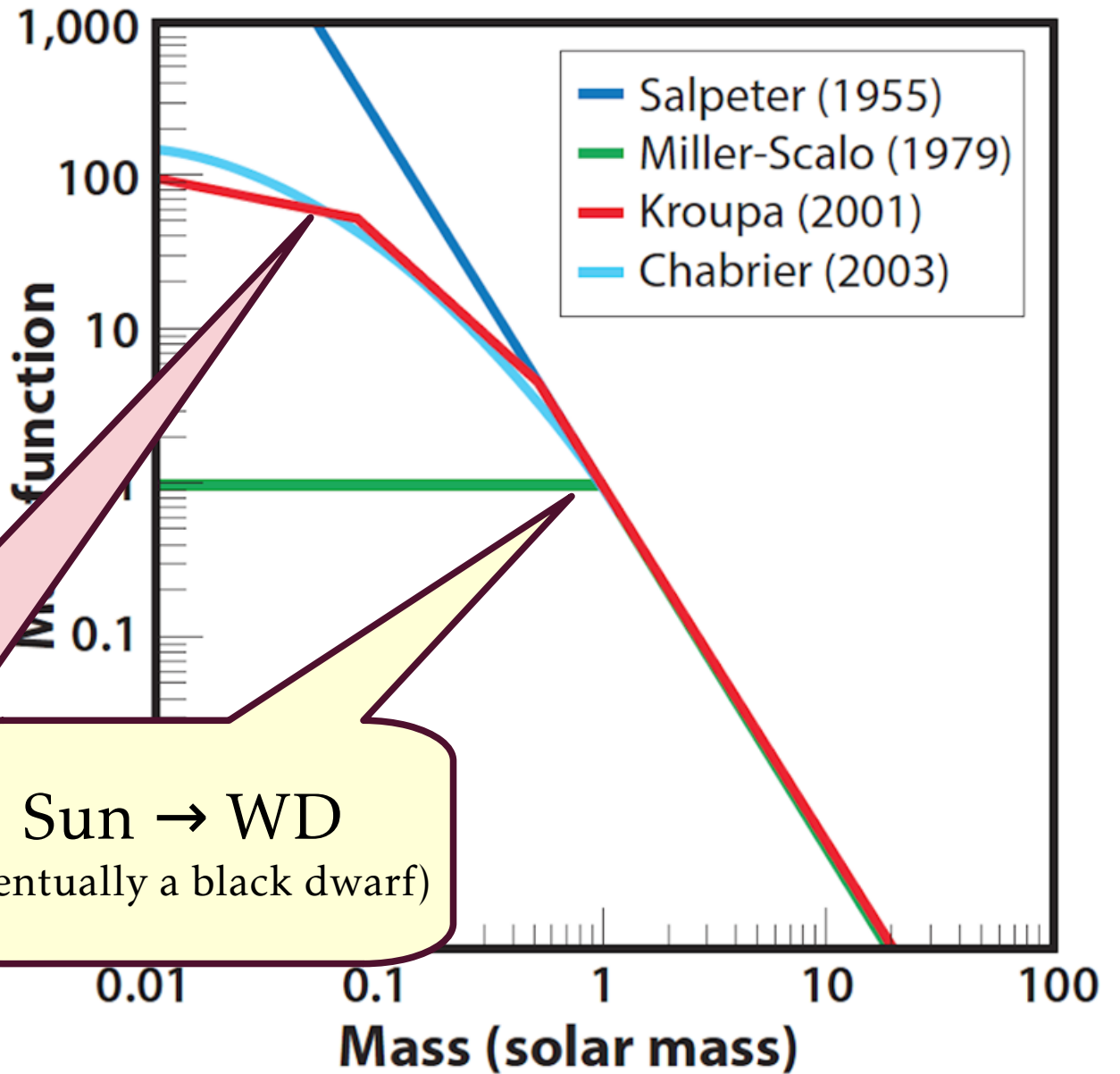
sub-Solar masses:

– also white dwarfs  
(=compact object,  
stellar remnant)

– *however:*

brown dwarf stars  
may live longer than  
the Universe...

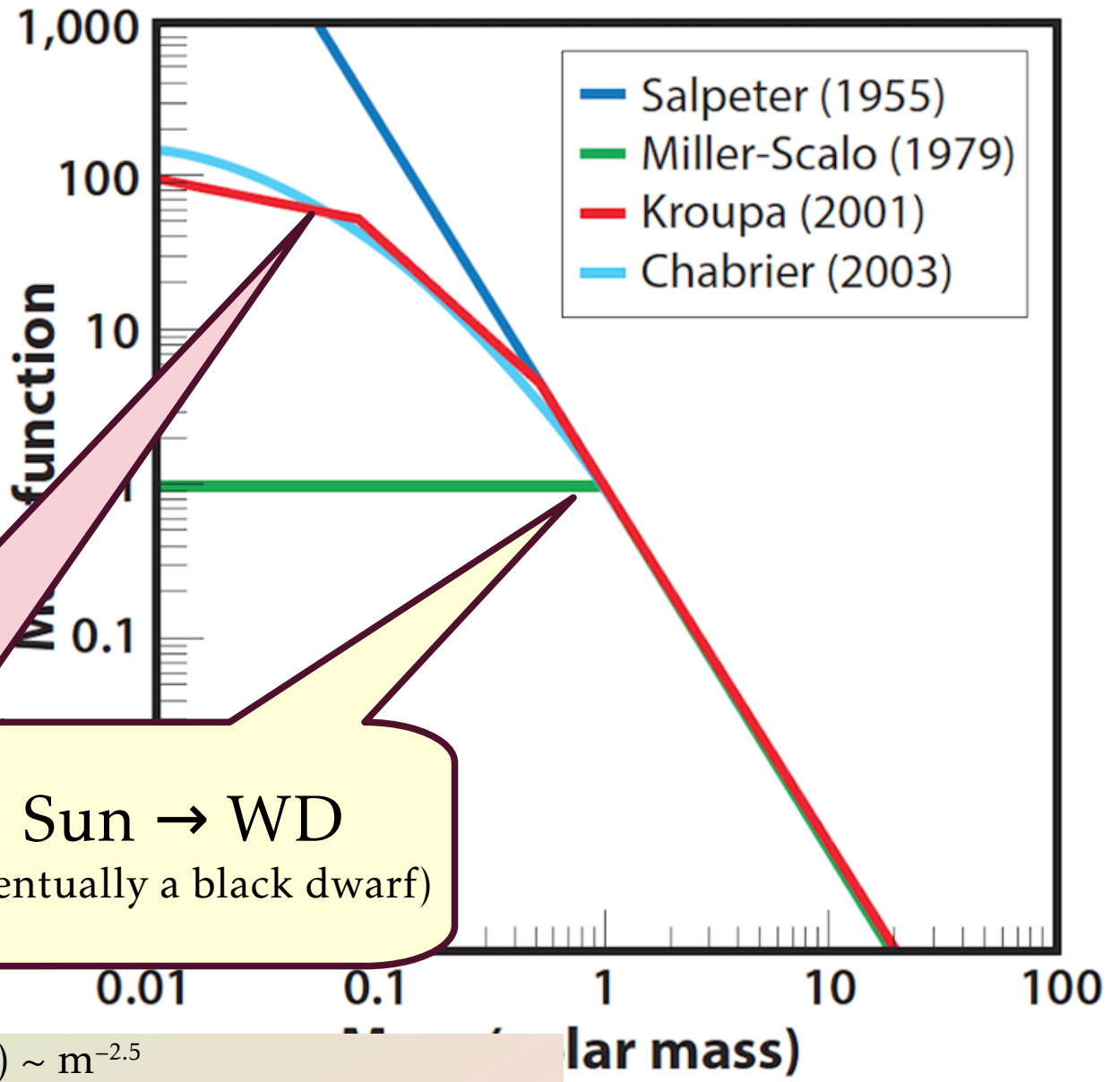
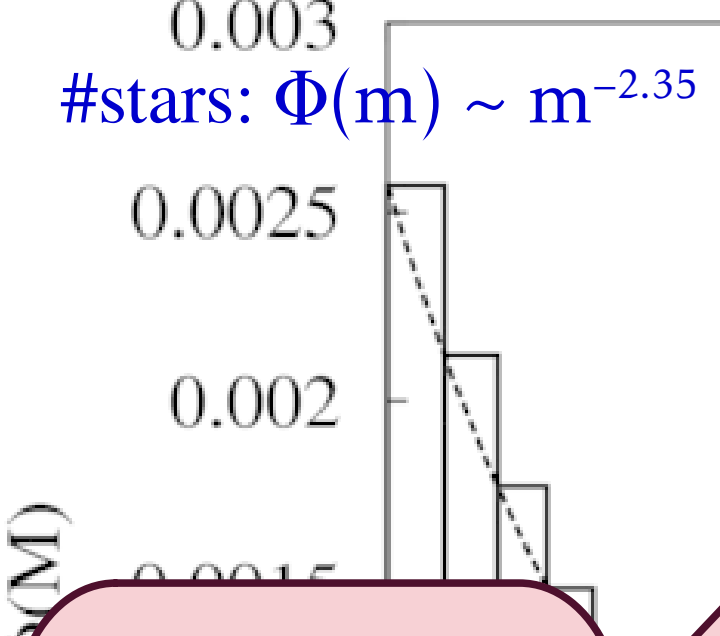
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- $\tau(m) \sim m^{-2.5}$ 
  - a 100  $M_{\odot}$  star's lifetime:  $\sim 2 \times 10^6$  yrs
  - an 8  $M_{\odot}$  star's lifetime:  $\sim 5 \times 10^7$  yrs
  - Sun's lifetime:  $\sim 10 \times 10^9$  yrs
  - sub-Solar: may exceed  $10 \times 10^{13}$  yrs

*Credit: Roen Kelly*

# What are compact objects? <sup>stellar 'corpses'</sup> = **remnants**

- three main types:

- white dwarf
- neutron star
- black hole

**degenerate  
stars**

other (speculative) degenerate stars:

- quark star
- preon star
- boson star
- ... (see e.g. Wikipedia)

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- nuclei (He/O/C/Ne/Mg) are **not** in degenerate state

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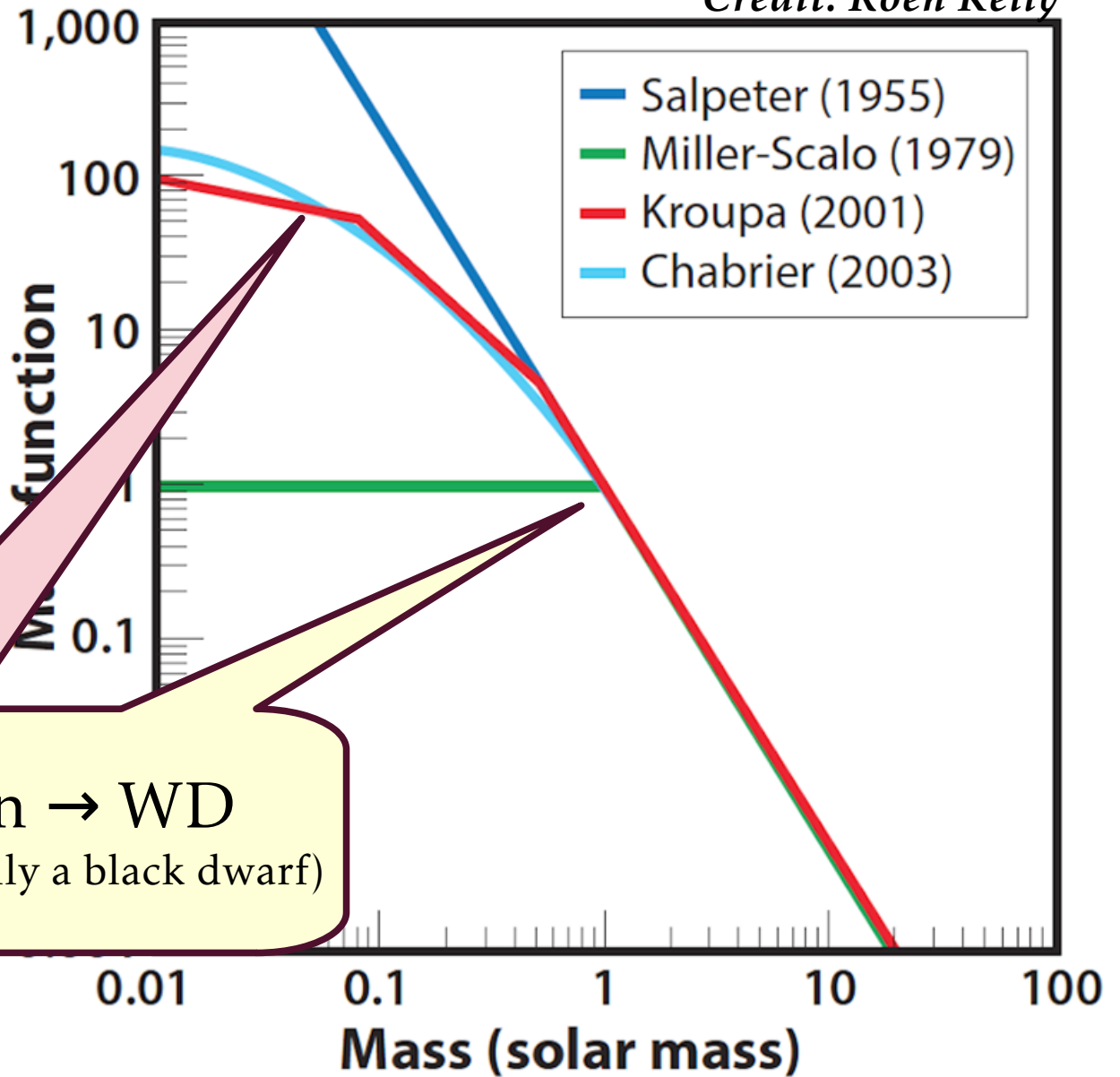
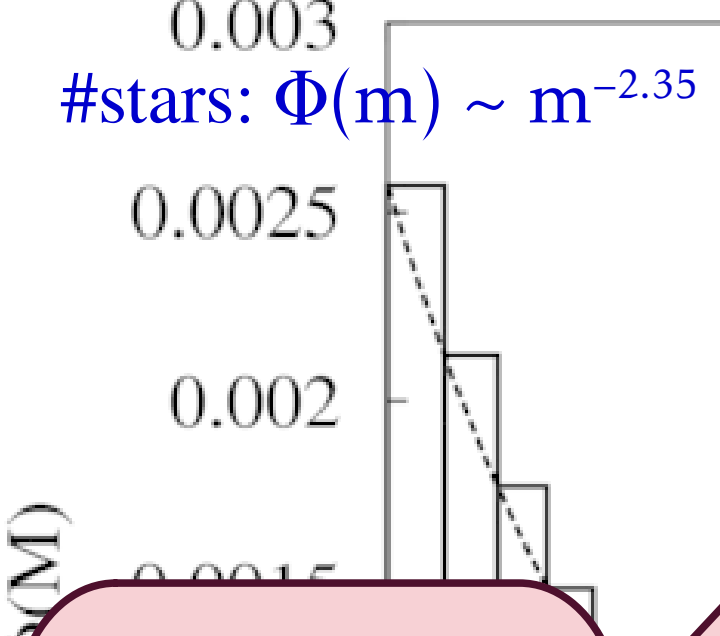
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degeneracy pressure → **stability** against  
(self-)gravity

composition depends on mass  
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sub-Solar masses:

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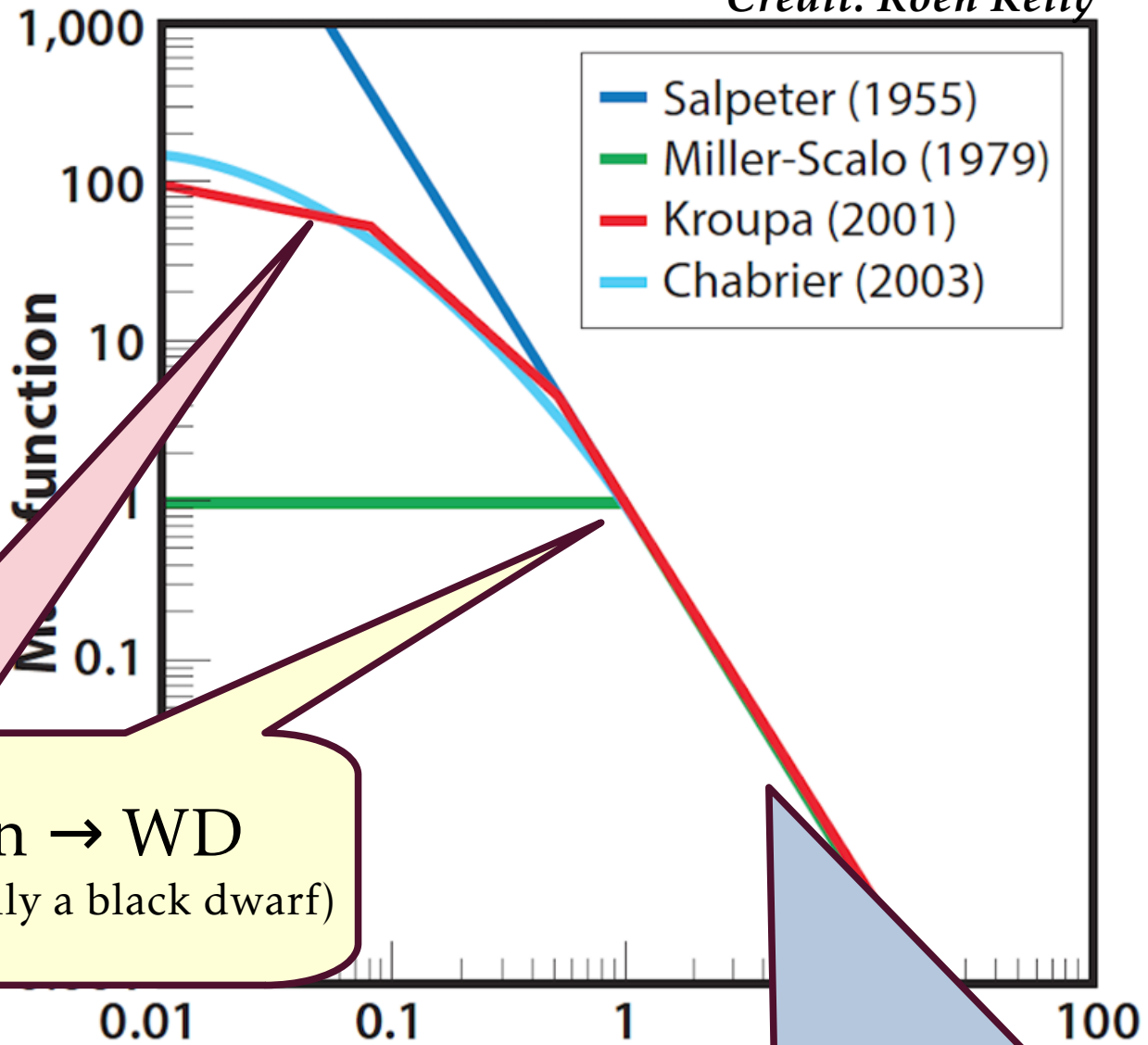
Sun → WD  
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M (Solar Masses)



Credit: Roen Kelly

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$\Phi(M)$

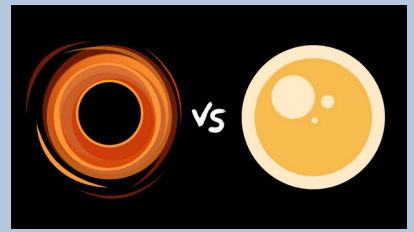
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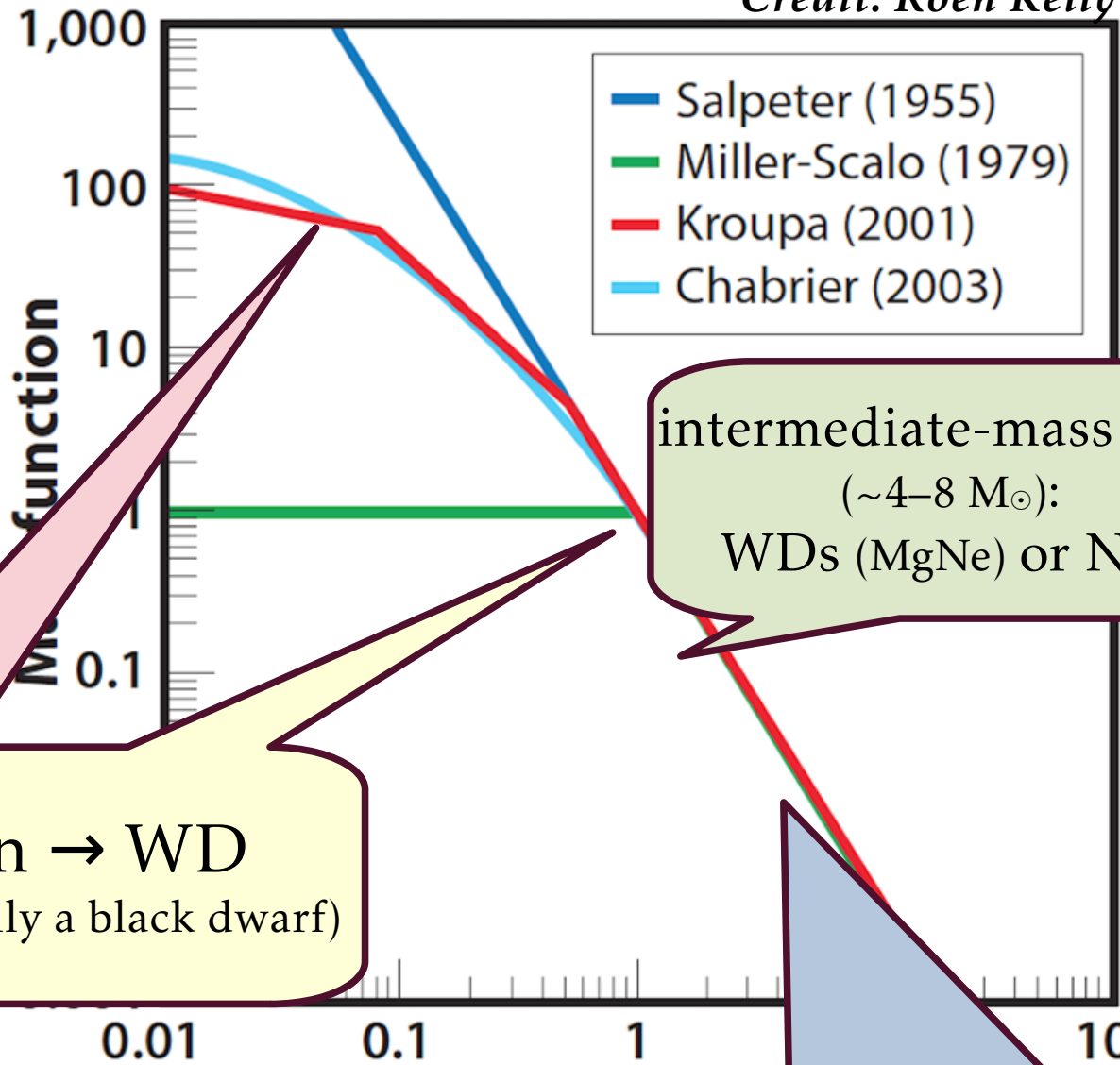
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Massive stars:  
NSs or BHs\*



Credit: Roen Kelly

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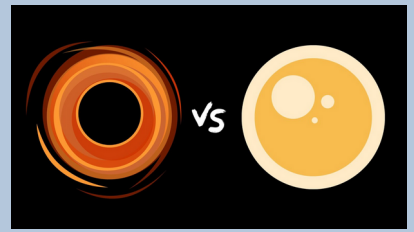
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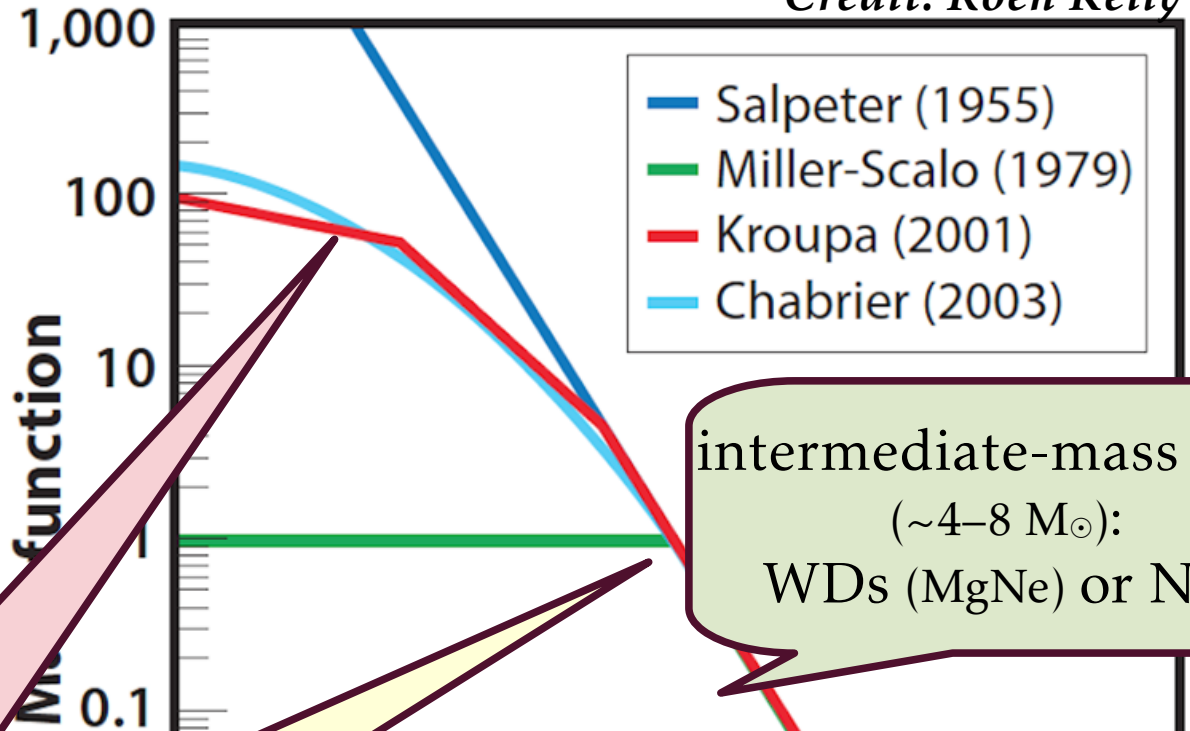
intermediate-mass stars  
(~4–8  $M_{\odot}$ ):  
WDs (MgNe) or NSs

Massive stars:  
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$\Phi(M)$

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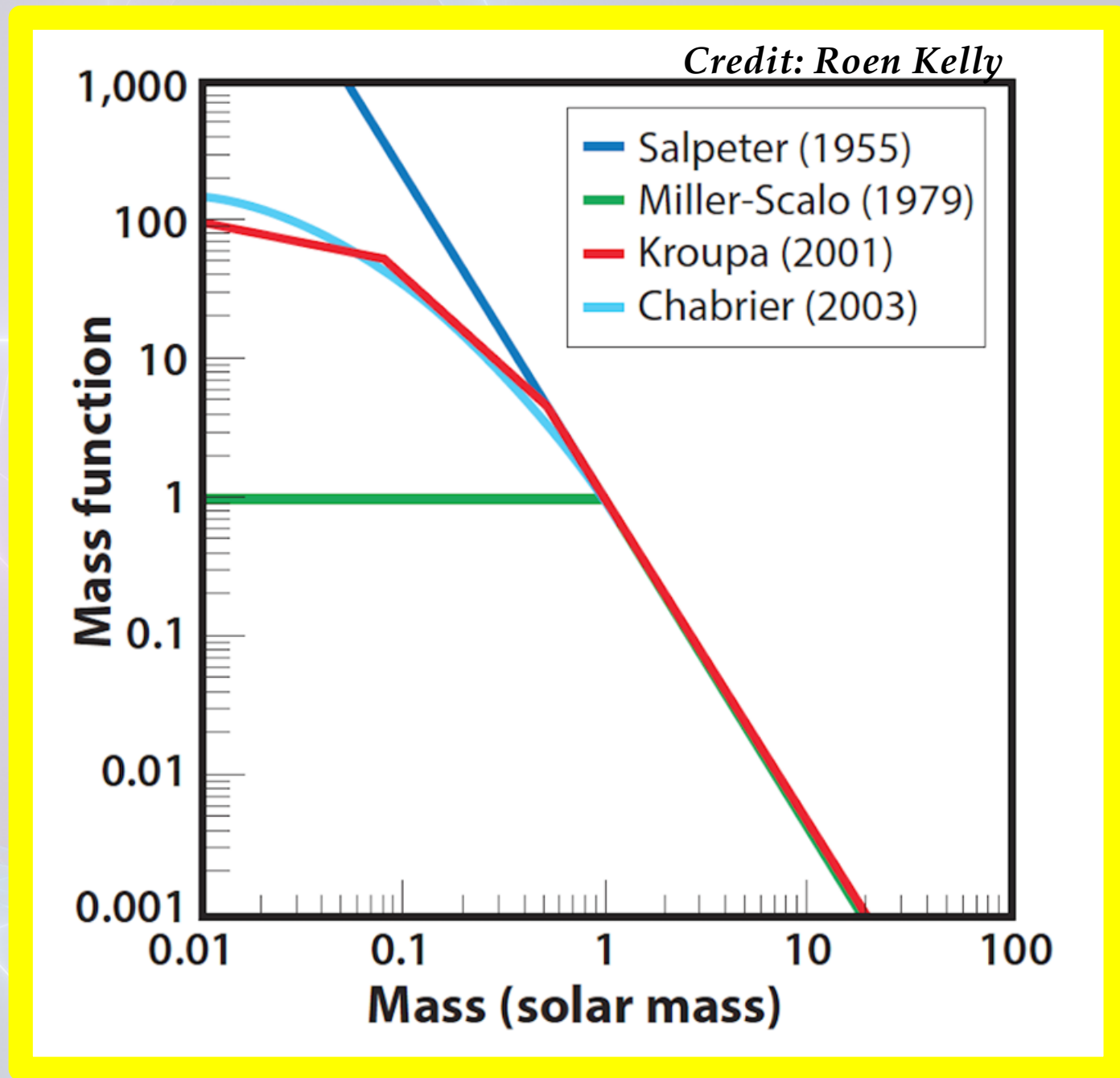
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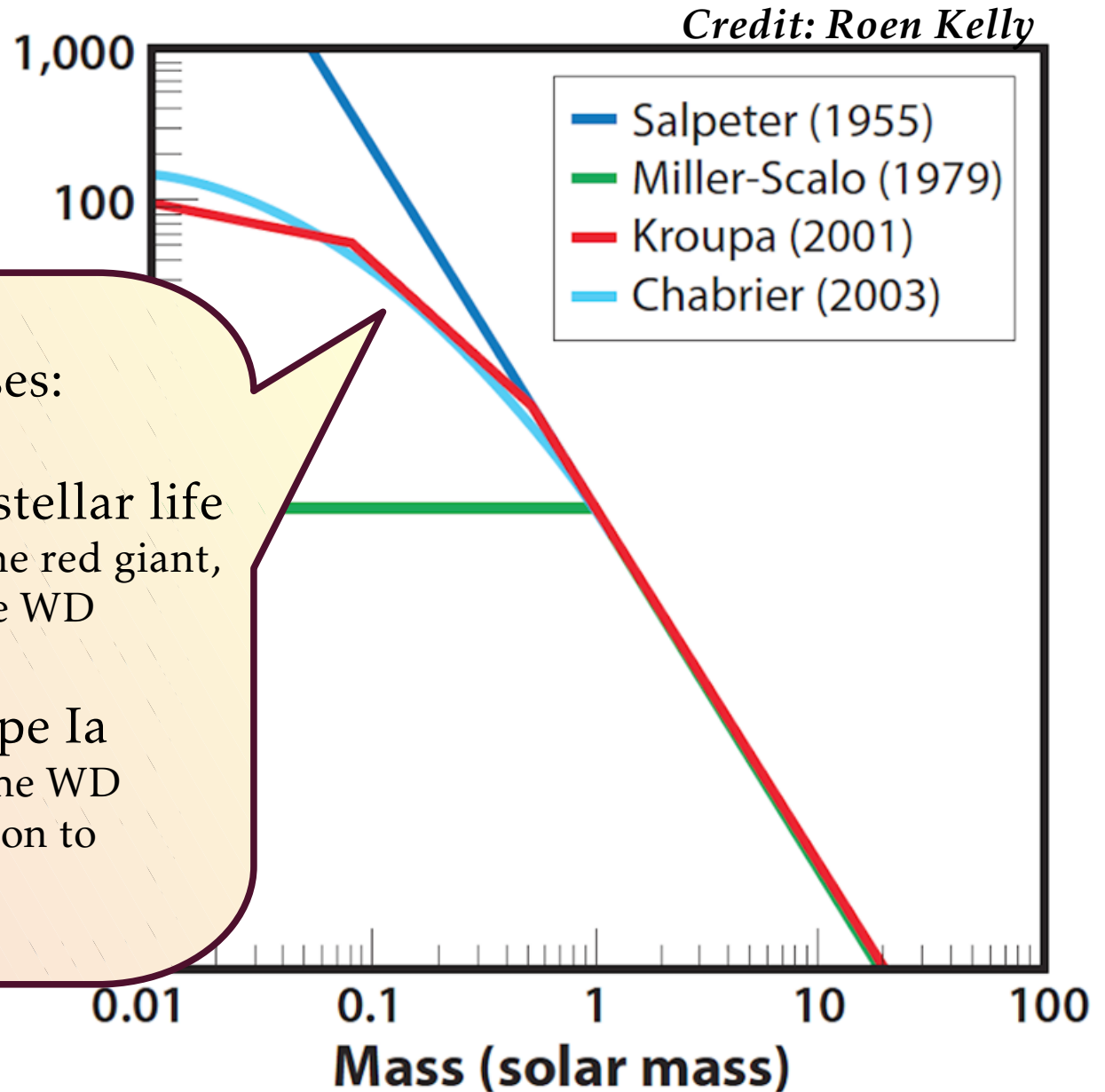
Massive stars:  
NSs or BHs\*

\*Maximum size of  
BHs at Solar Z  
is around  $40 M_{\odot}$   
due to strong  
mass loss of the massive  
star progenitor

# Explosion types?



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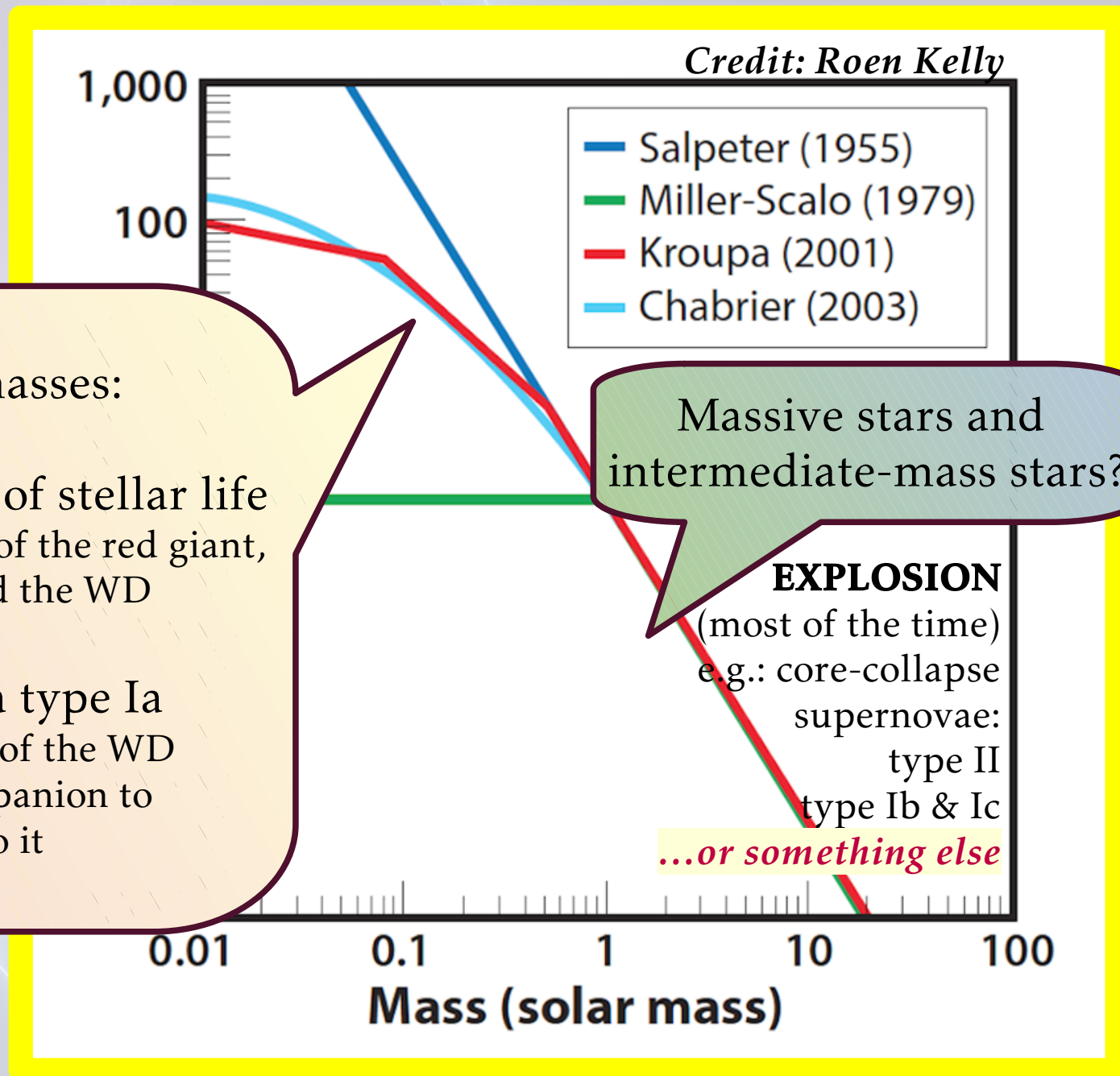
Sun & sub-Solar masses:

– no explosion at the end of stellar life  
i.e. ejection of the outer layers of the red giant,  
planetary nebula around the WD

– **LATER:** supernova type Ia  
thermonuclear explosion of the WD  
***IF*** there is a binary companion to  
transfer mass onto it

Side-note: type Ia SNe  
are standard candles  
in cosmology

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Massive stars and  
intermediate-mass stars?

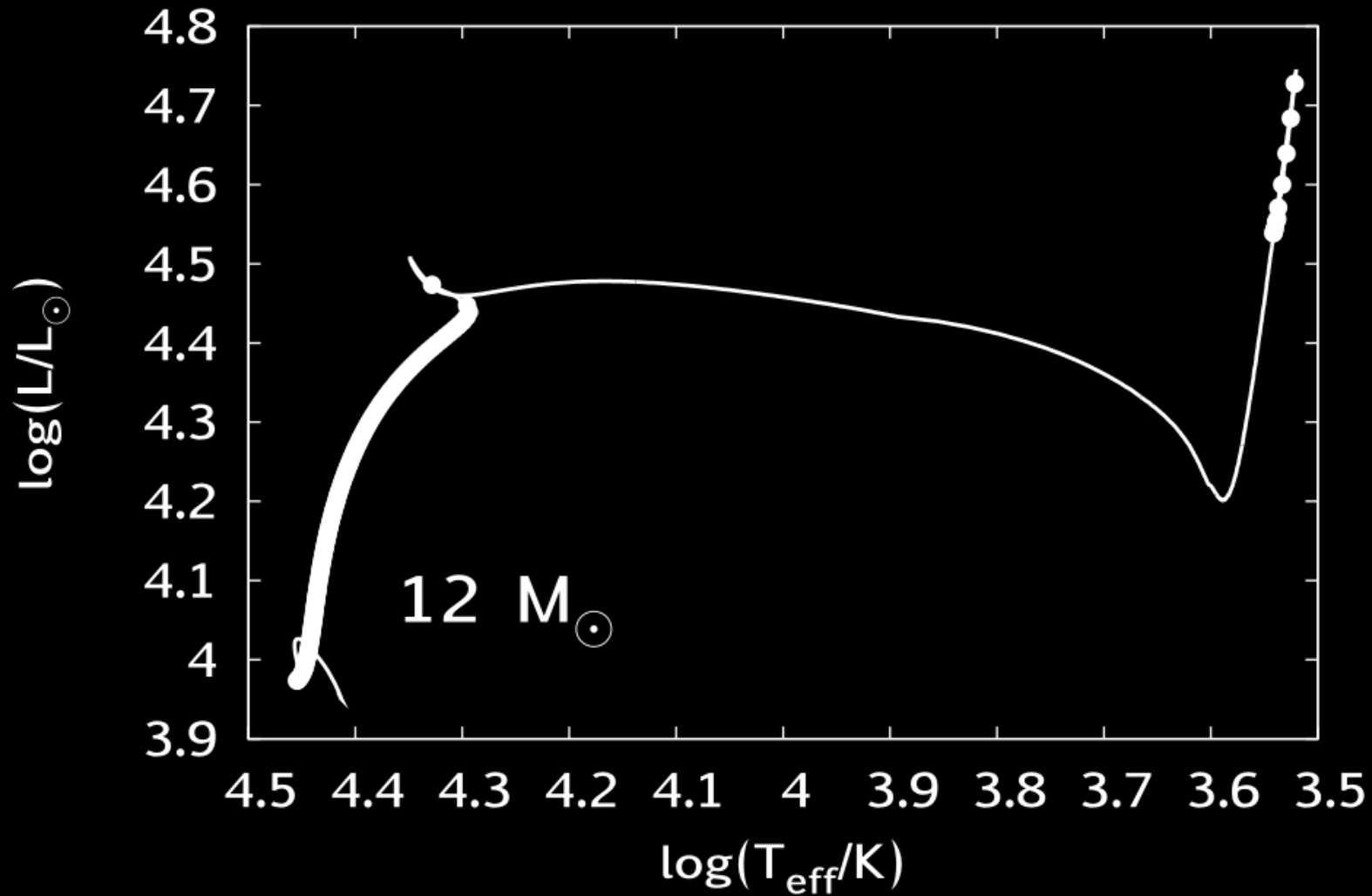
**EXPLOSION**

(most of the time)  
e.g.: core-collapse  
supernovae:  
type II  
type Ib & Ic

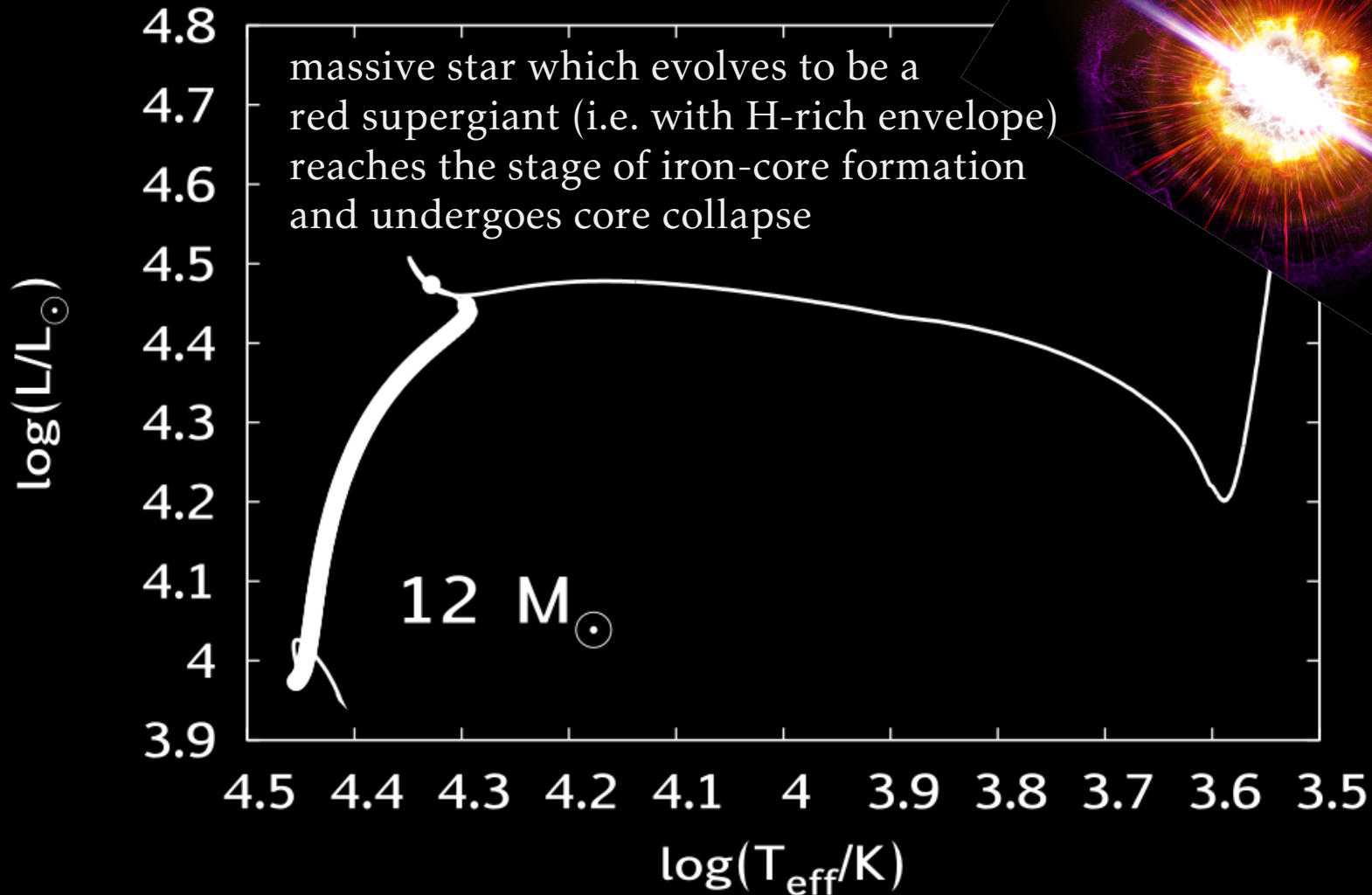
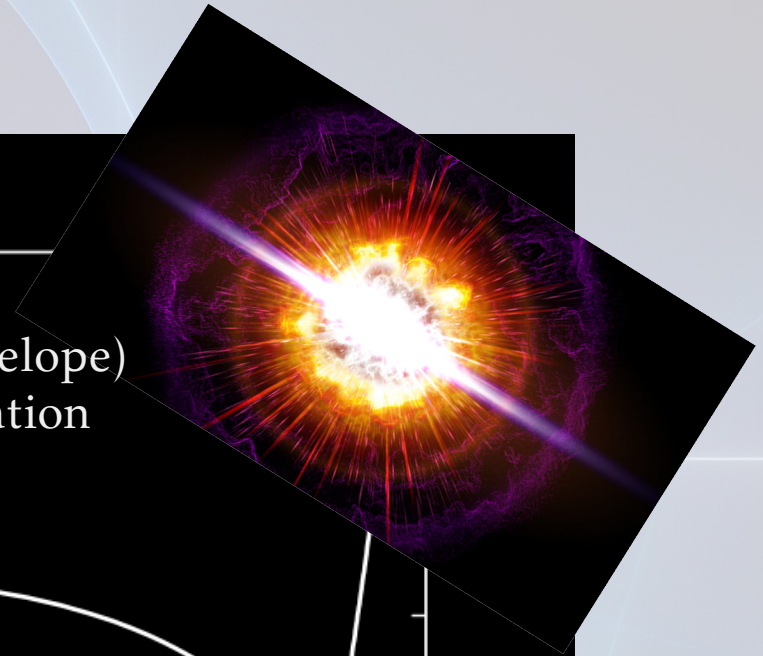
*...or something else*

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Way towards a type II supernova:

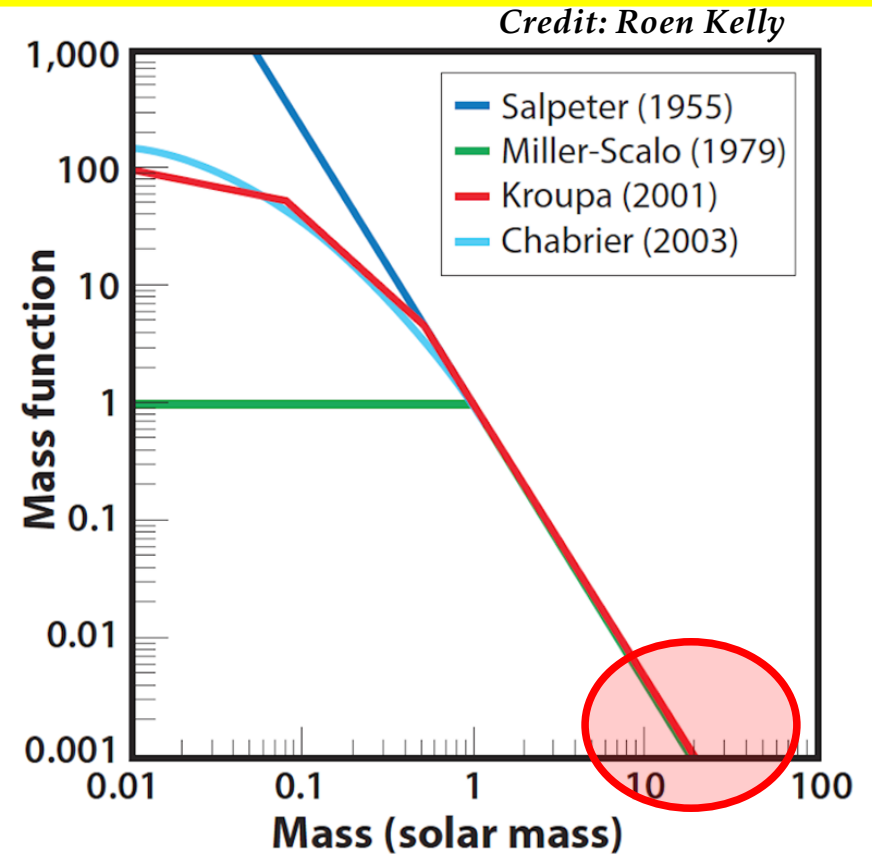
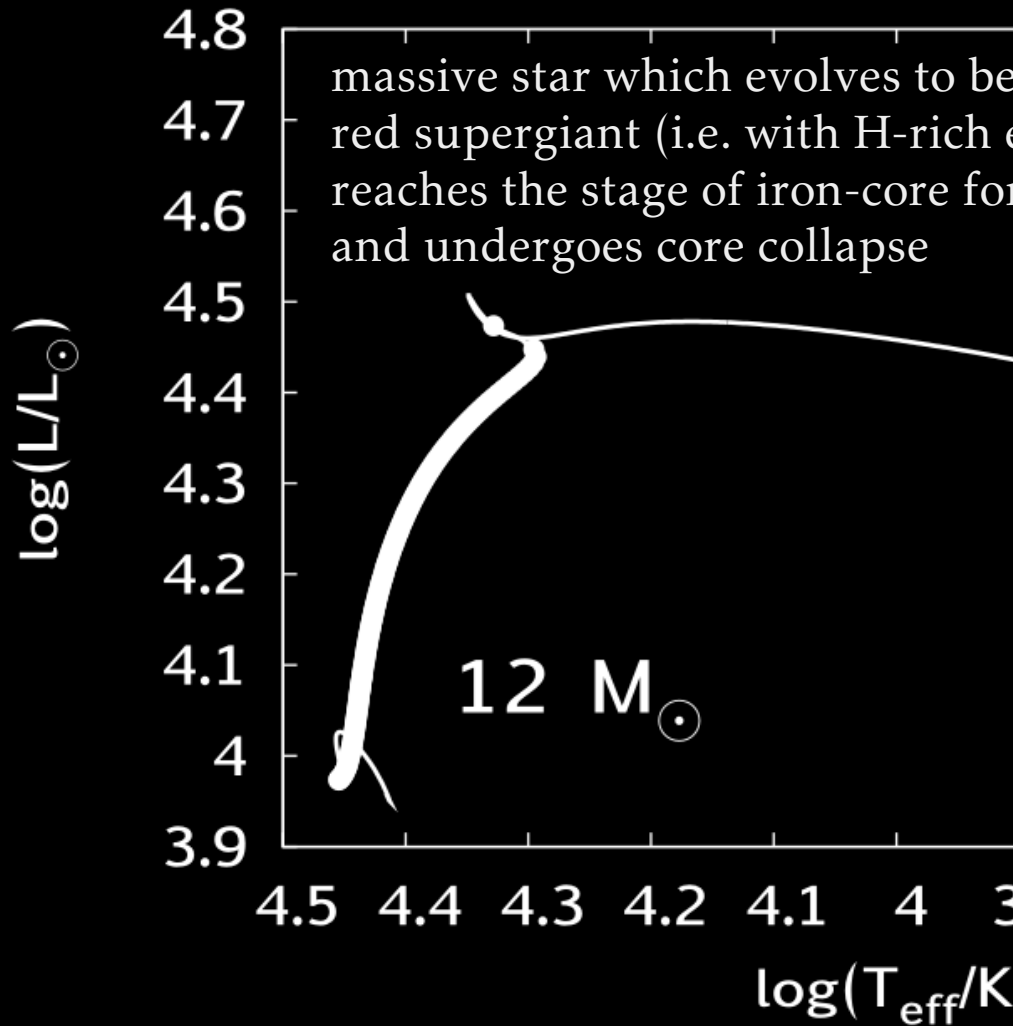
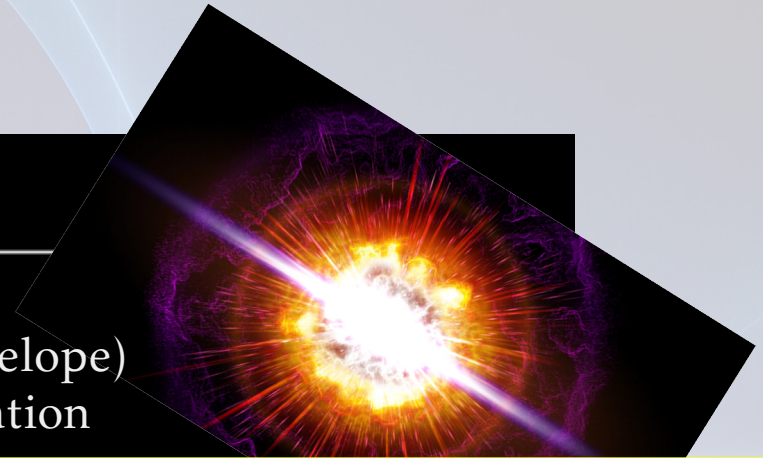


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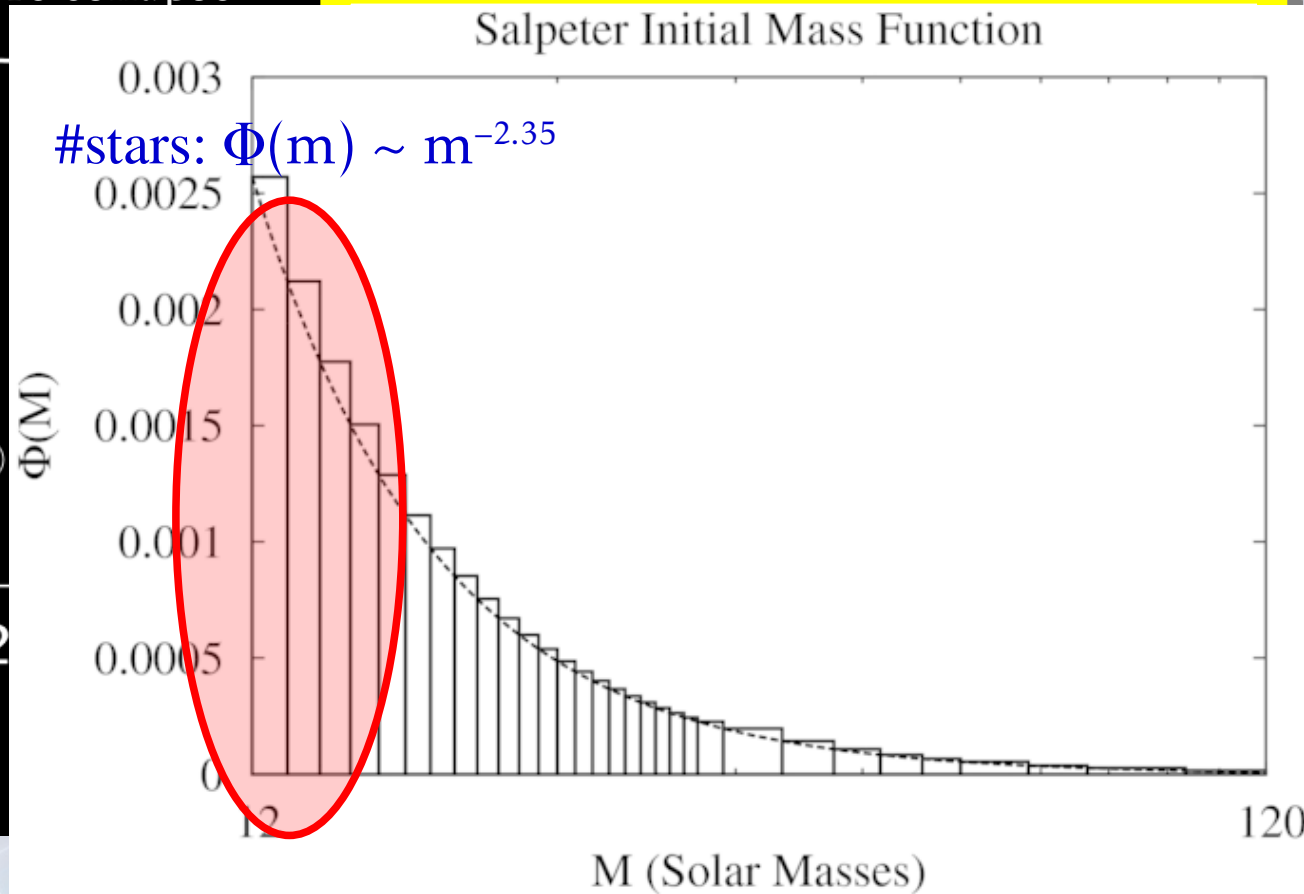
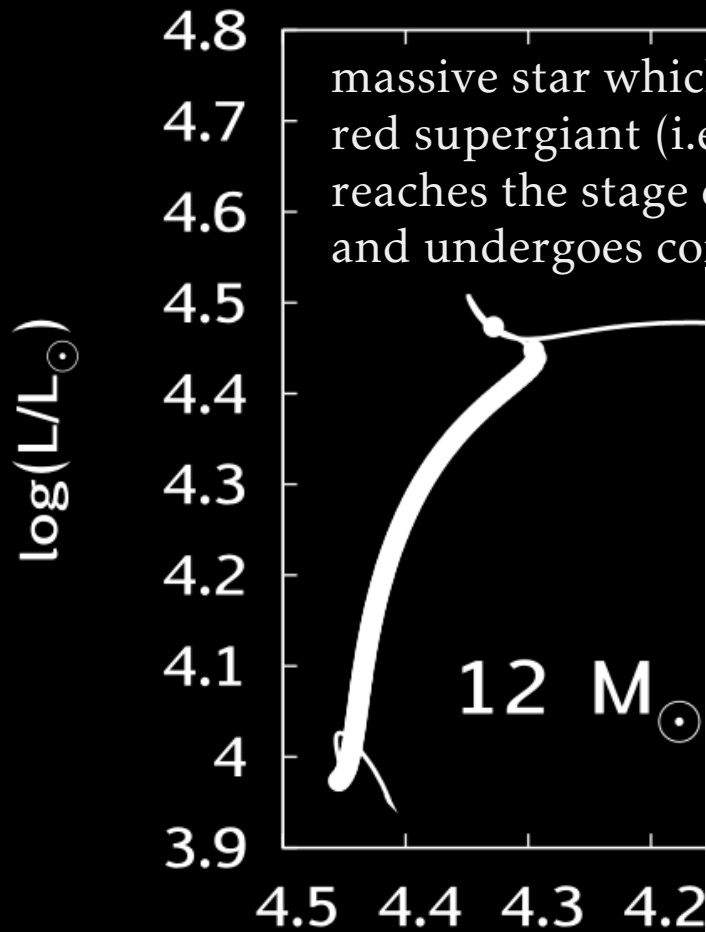
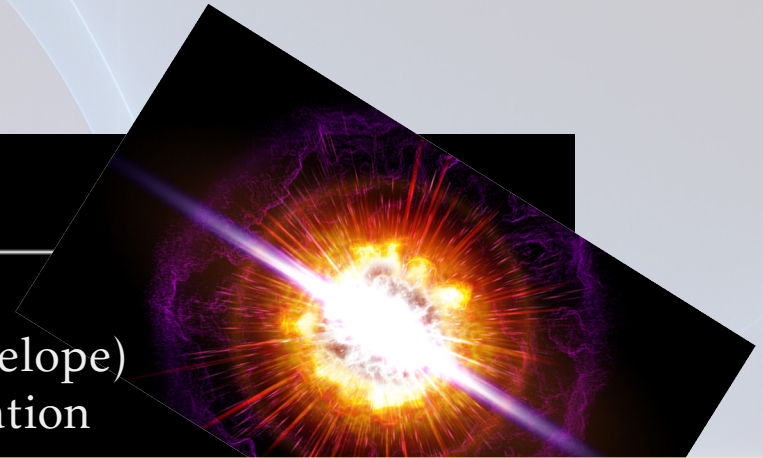


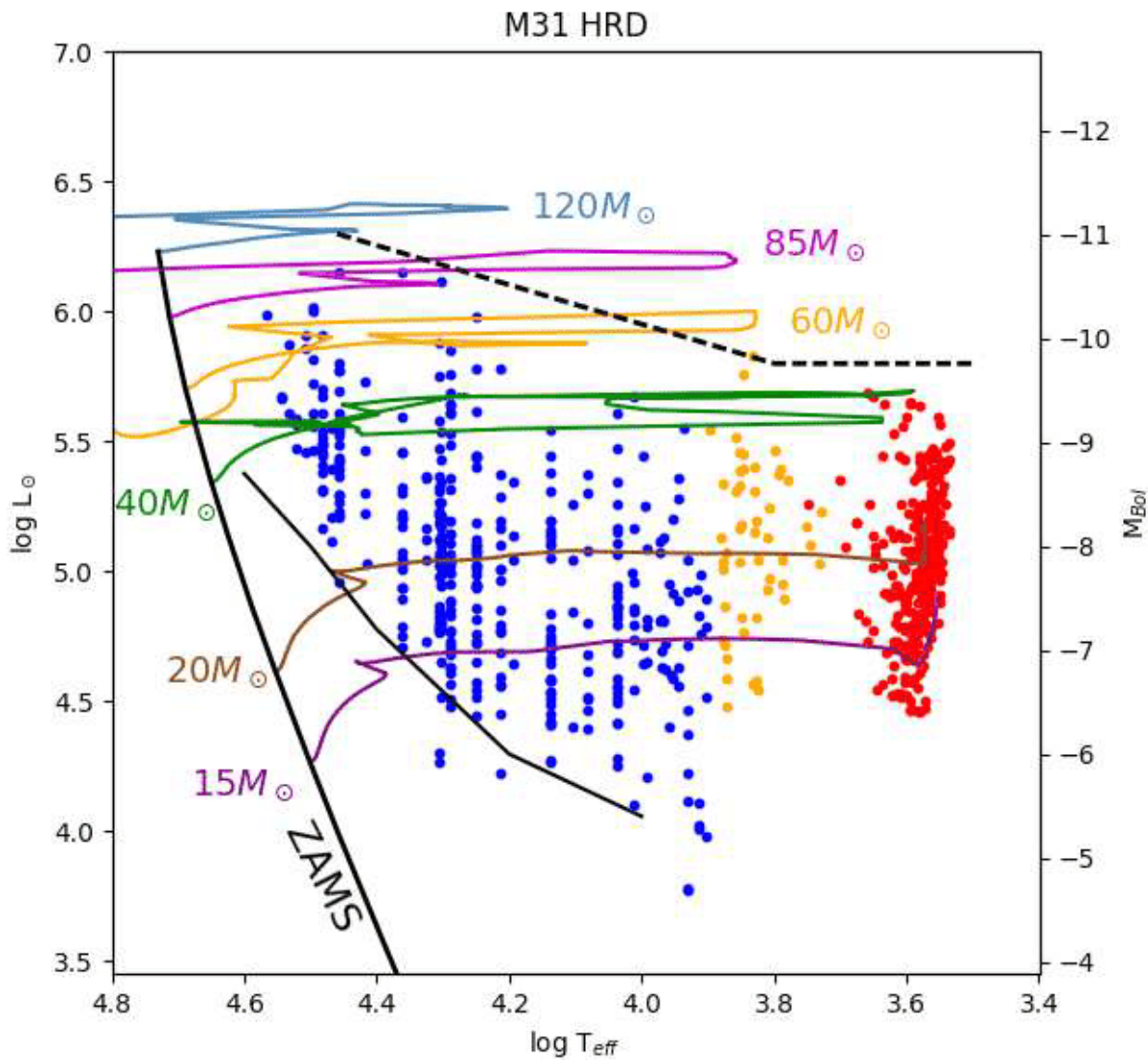


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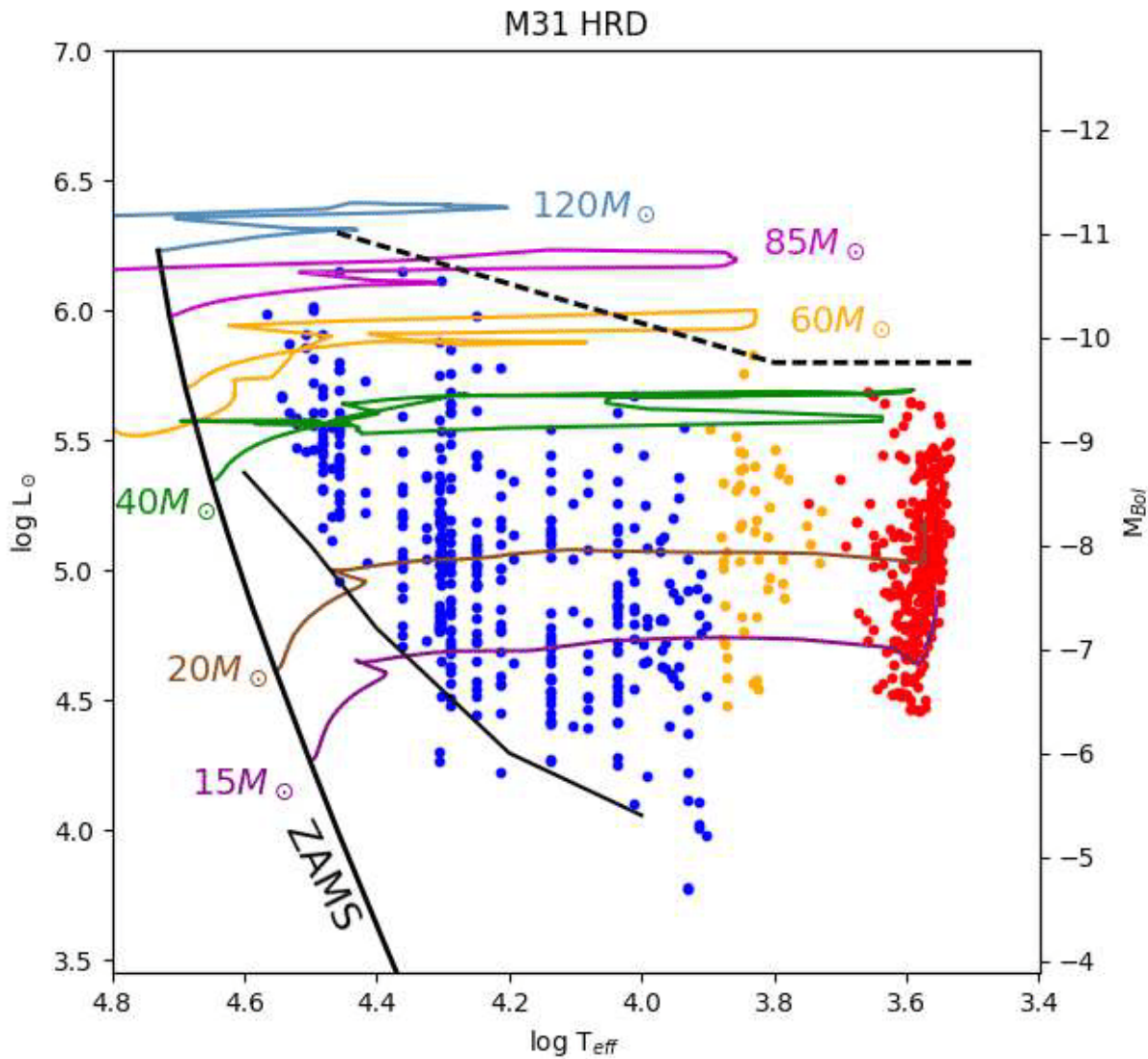


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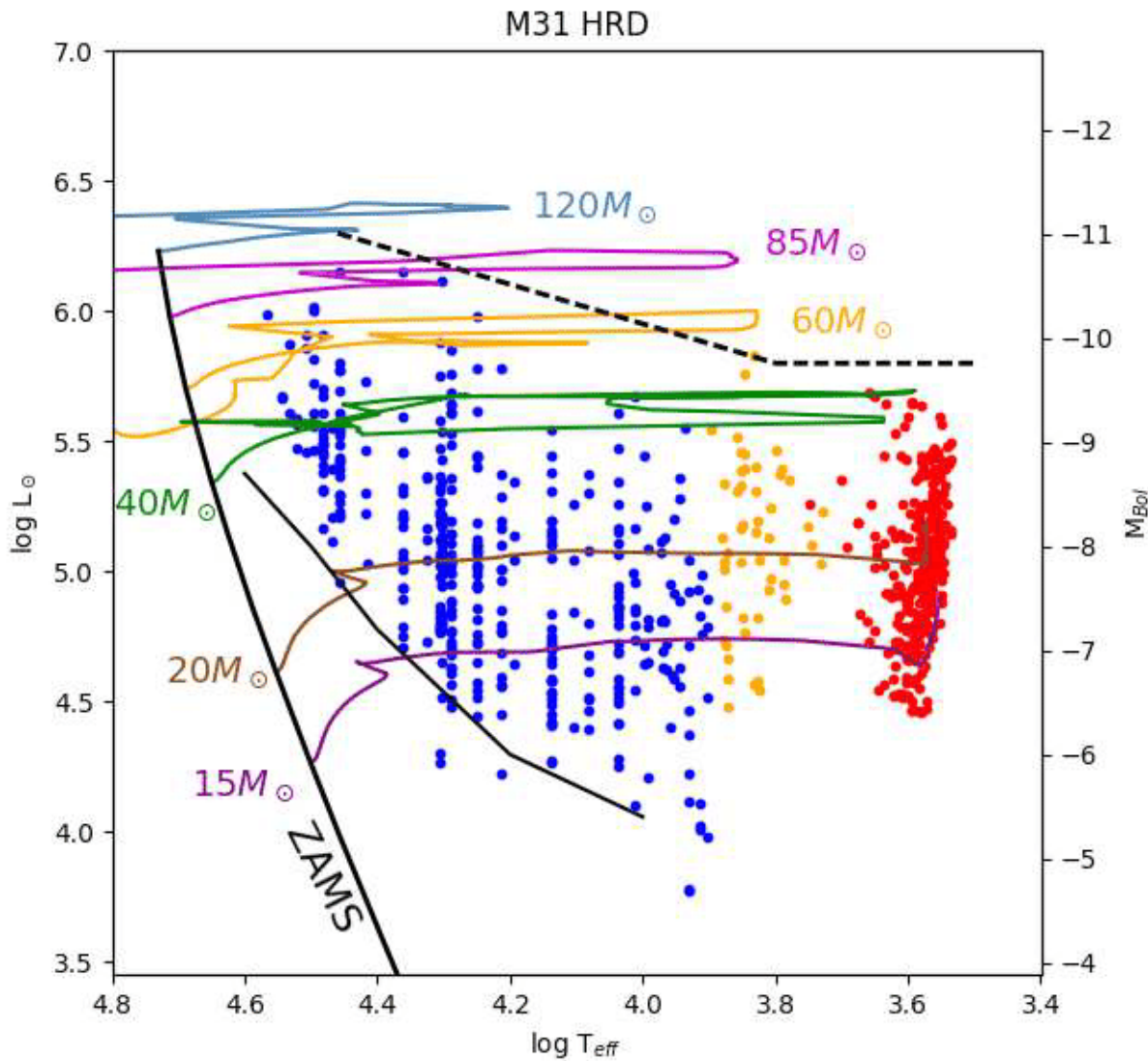


red-supergiant progenitor  
→ **type II**



Credit: Roberta Humphreys & al. (2017, ApJ. 844.)

\*stripping = loss of H-rich top layers  
In the context of *single* stars:  
'stripping' is due to losing mass in the strong wind  
In the context of *binary* stars:  
mass transfer



'stripped' progenitor\*  
(e.g. a Wolf-Rayet star)  
→ **type Ib or Ic**

red-supergiant progenitor  
→ **type II**

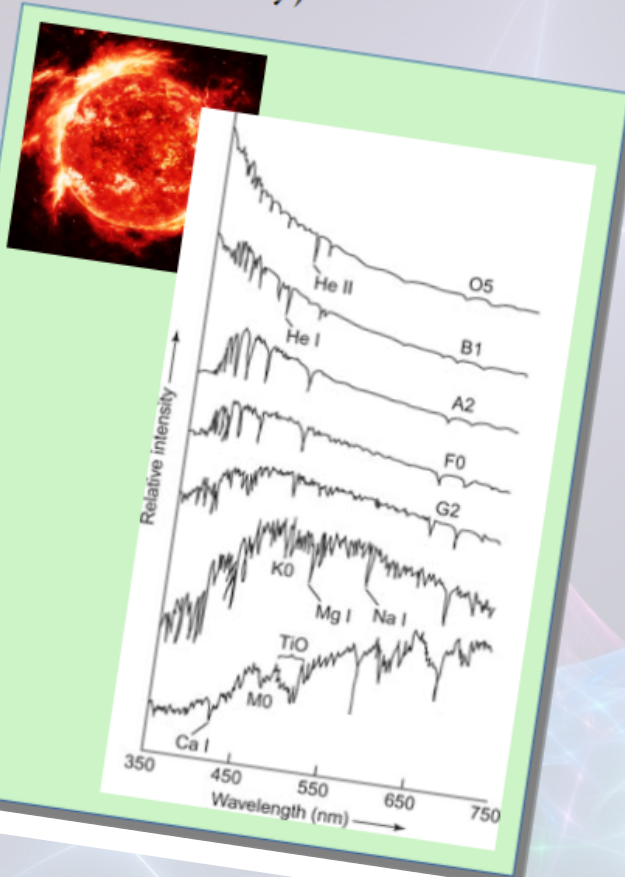
# Side-notes on Wolf-Rayet stars

- Observationally:
  - broad emission lines in the spectrum
  - meaning there is a nebula around the star
  - composition: (usually) H-free
- Theoretically:

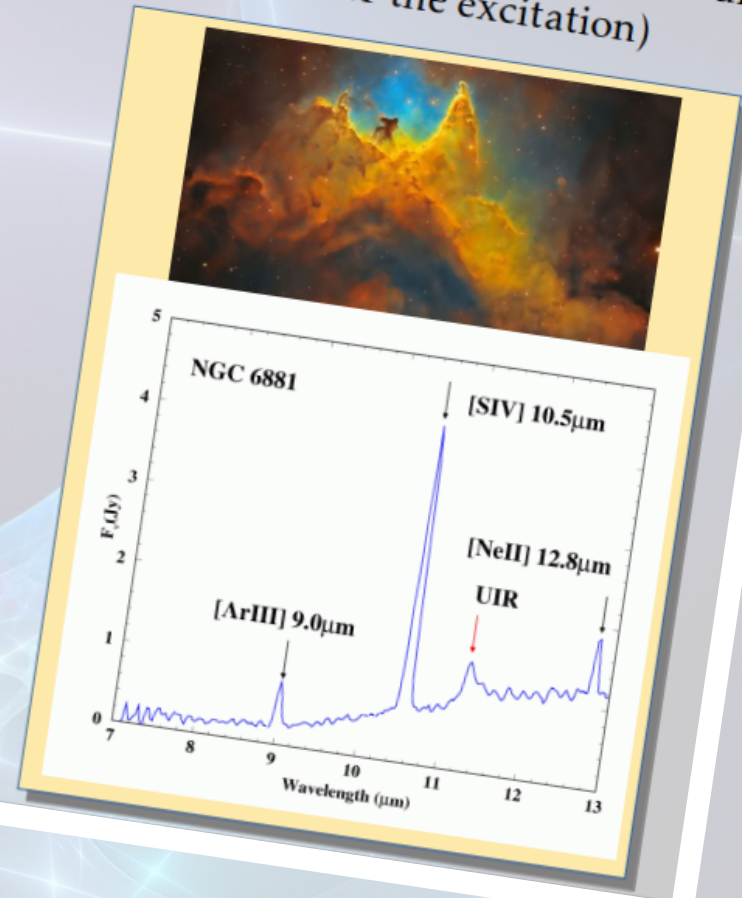
# Side-notes on Wolf-Rayet stars

- Observations
  - broad emission lines
  - meanings
  - components
- Theoretical

- Stellar spectra
  - absorption lines (mostly)

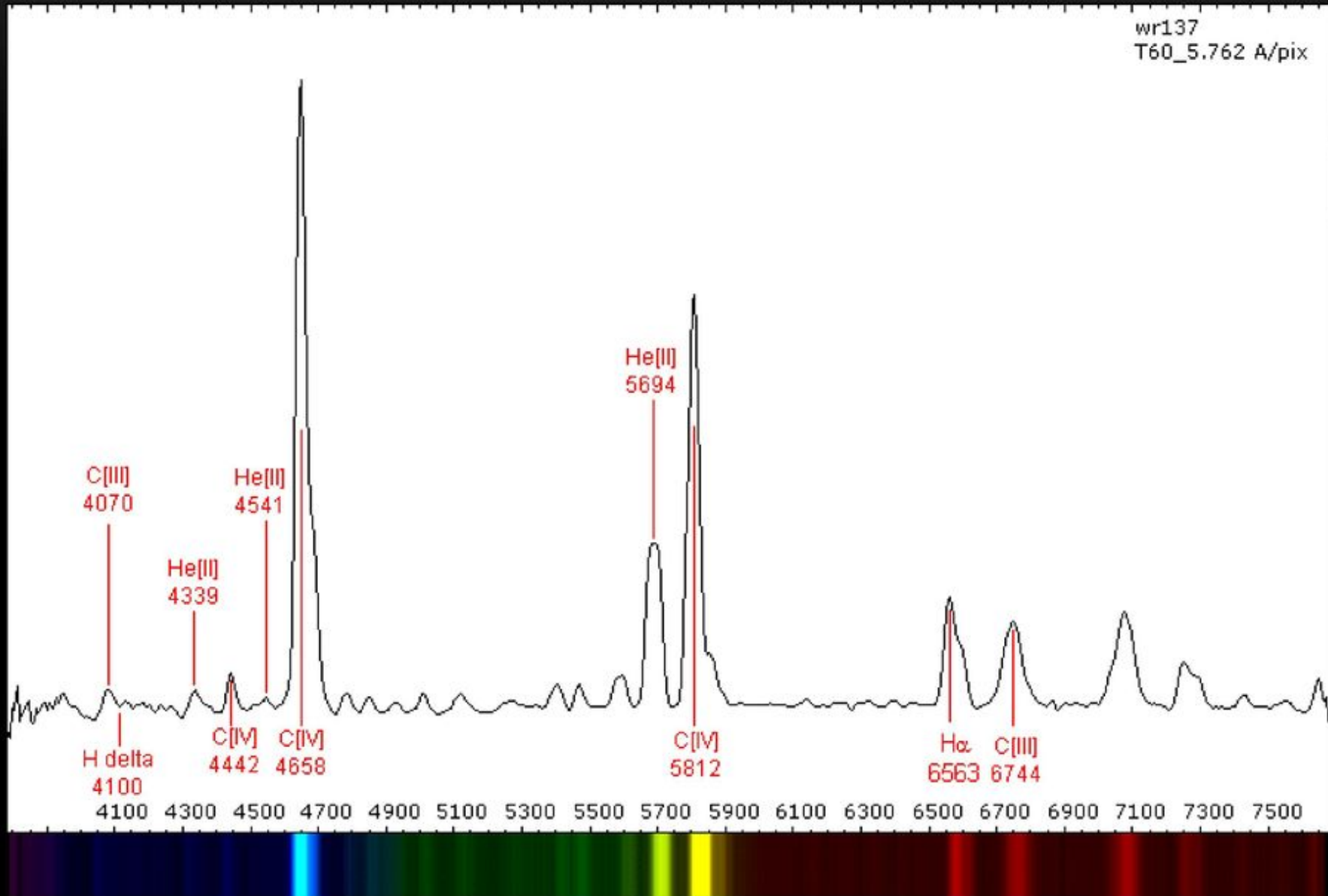


- Nebular spectra
  - emission lines (a light source needed for the excitation)



# FIRST OBSERVATION

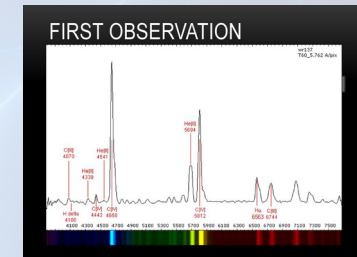
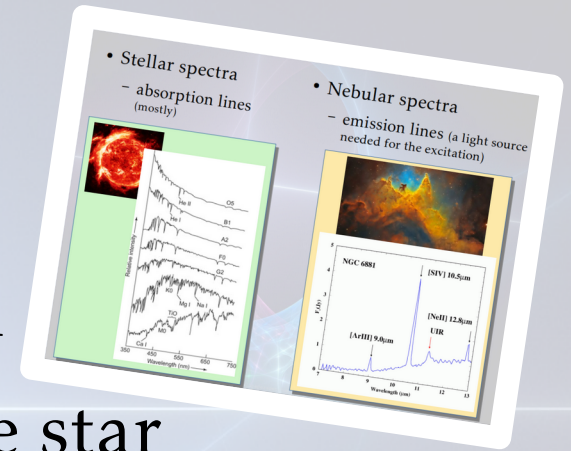
1867: Wolf & Rayet





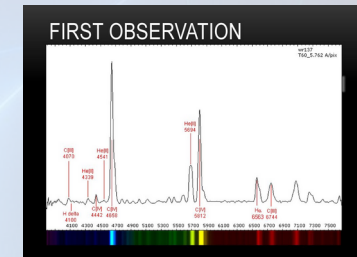
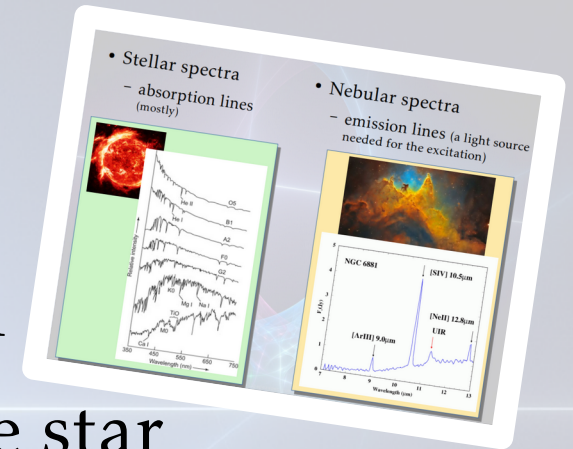
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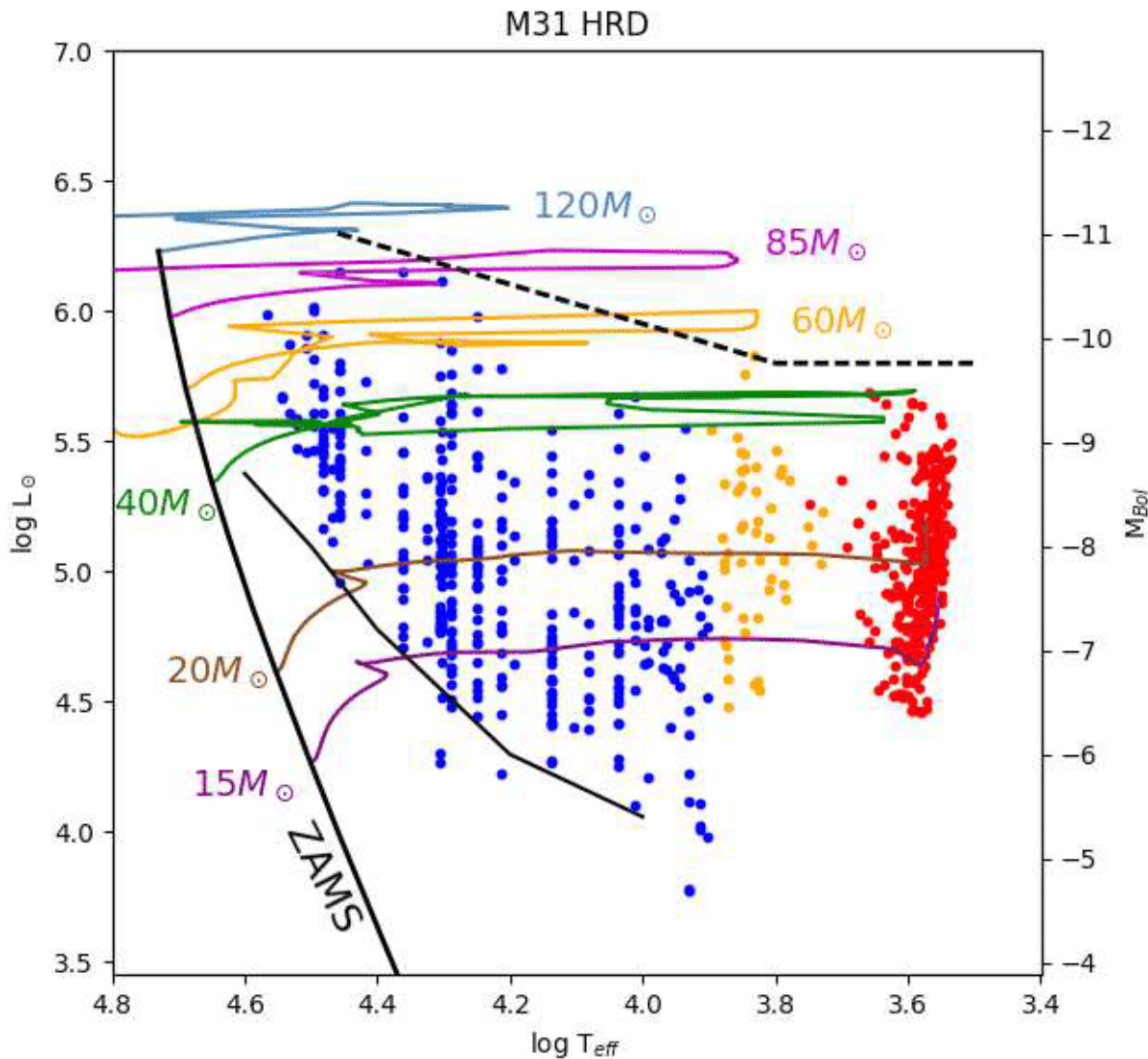
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- Theoretically:
  - a H-free star with a nebula around it can be produced by:
    - strong wind (single & binary stars) when the mass is very high ( $> 40 M_{\odot}$ , but highly Z-dependent!)
    - binary interaction (needs a close-enough companion & a so-called non-conservative mass transfer, etc.)





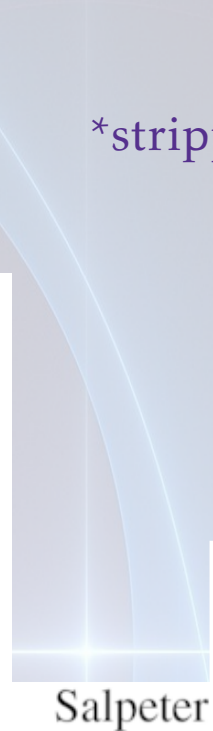
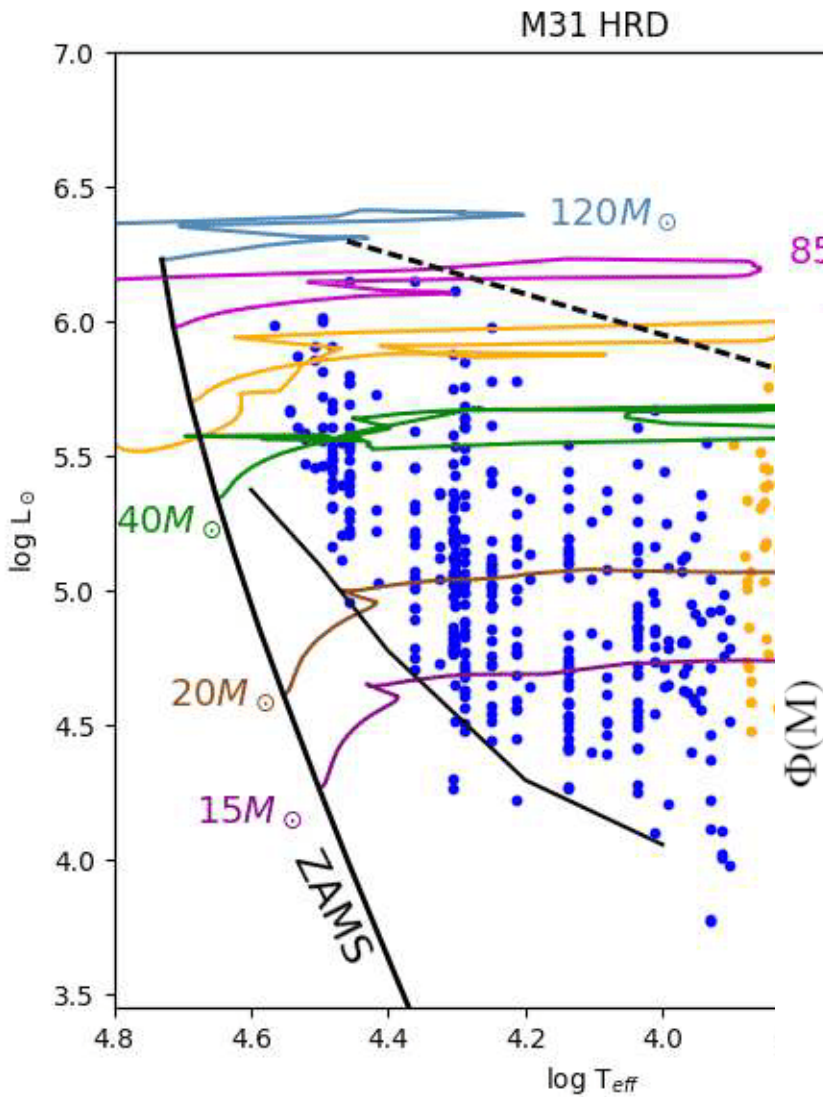
\*stripping = loss of H-rich top layers  
In the context of *single* stars:  
'stripping' is due to losing mass in the strong wind  
In the context of *binary* stars:  
mass transfer



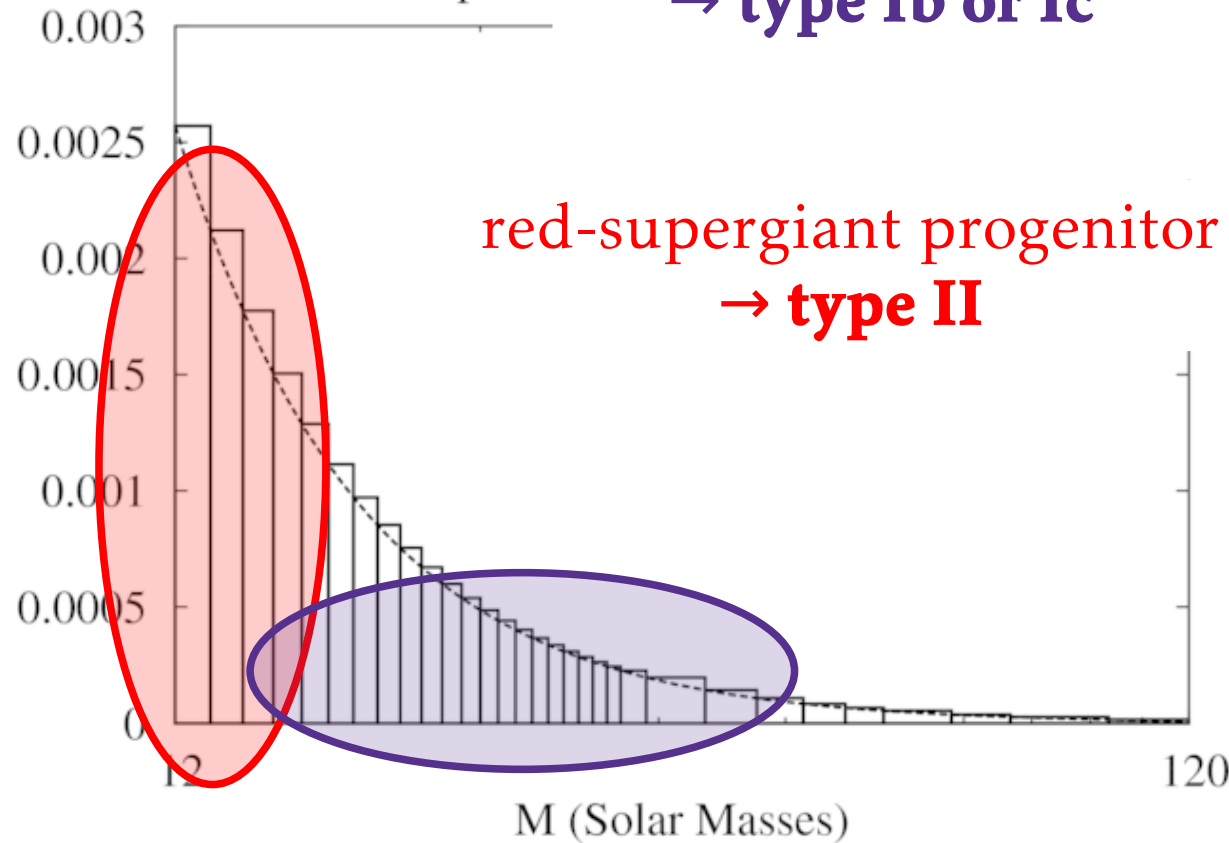
'stripped' progenitor\*  
(e.g. a Wolf-Rayet star)  
→ **type Ib or Ic**

red-supergiant progenitor  
→ **type II**

\*stripping = loss of H-rich top layers  
 In the context of *single* stars:  
 'stripping' is due to losing mass in the strong wind  
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 mass transfer

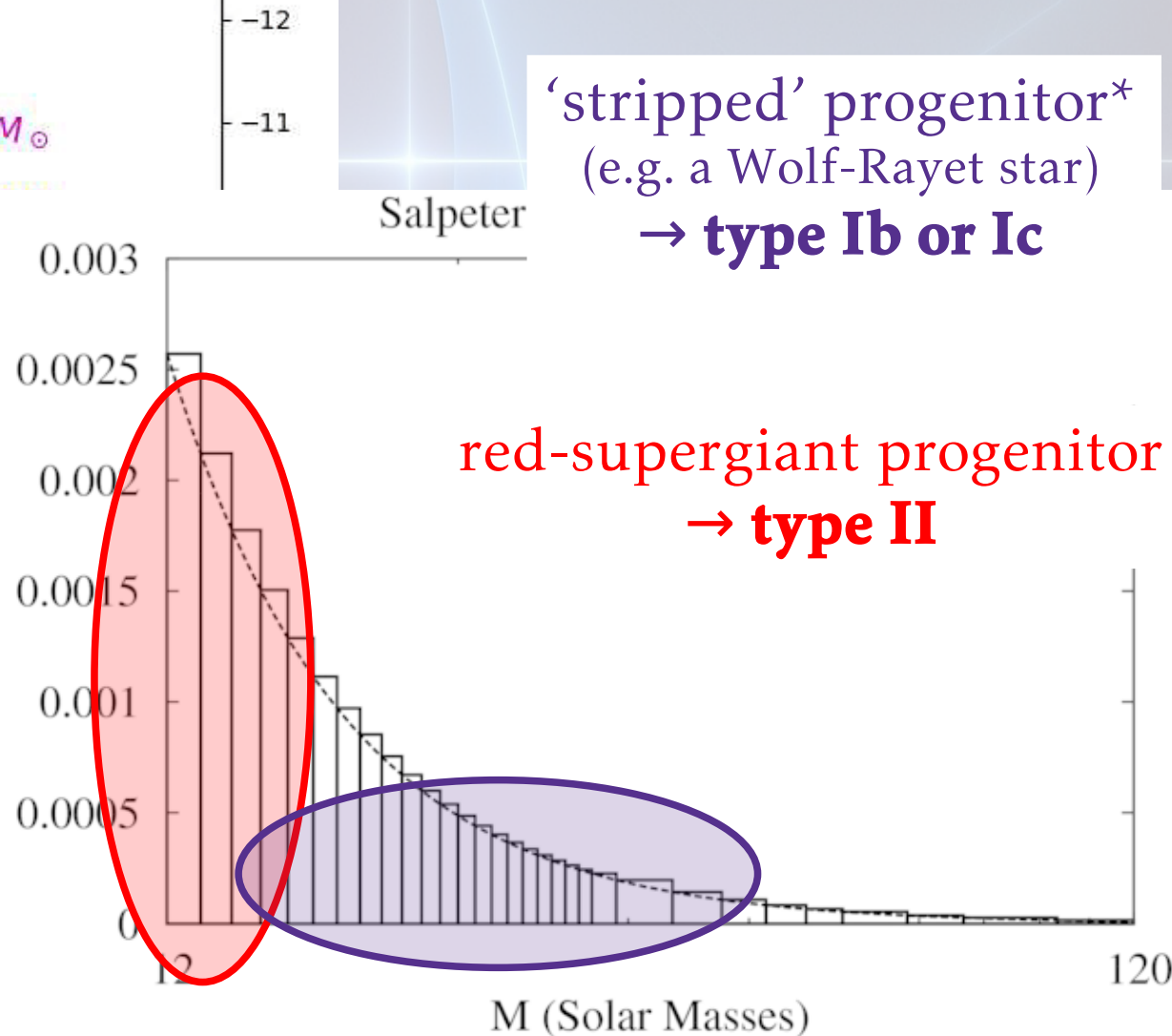
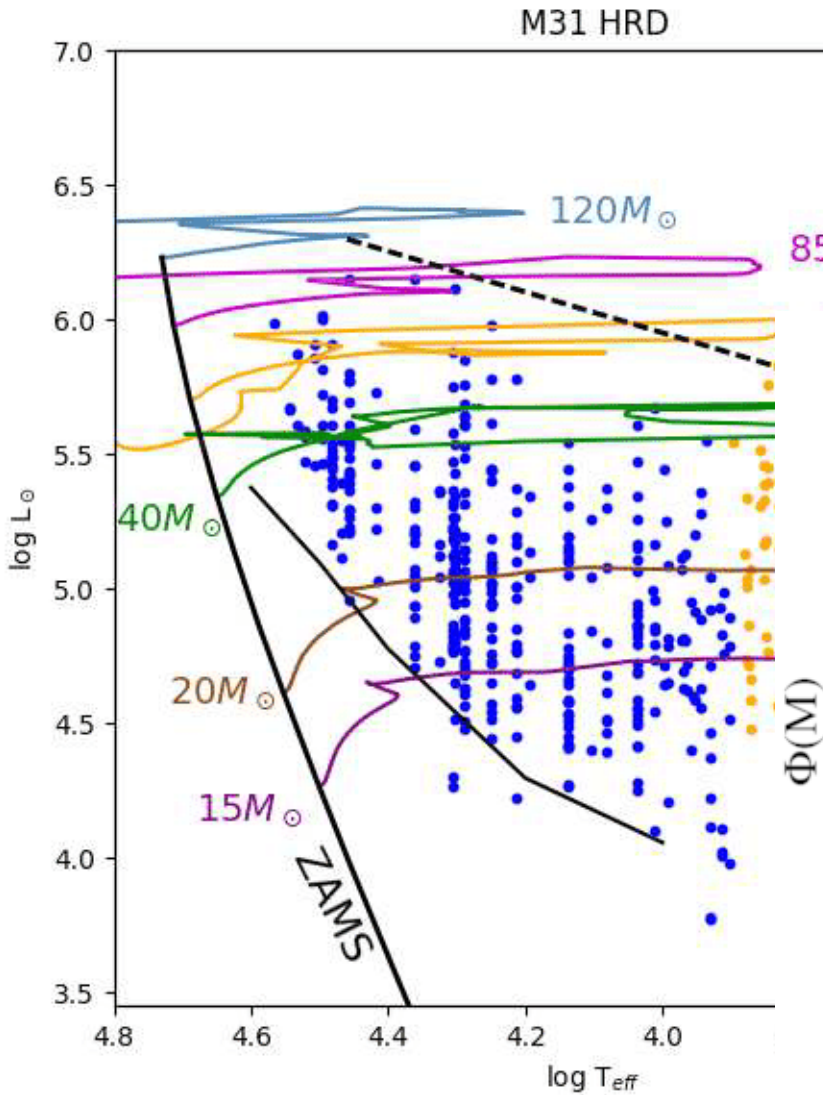


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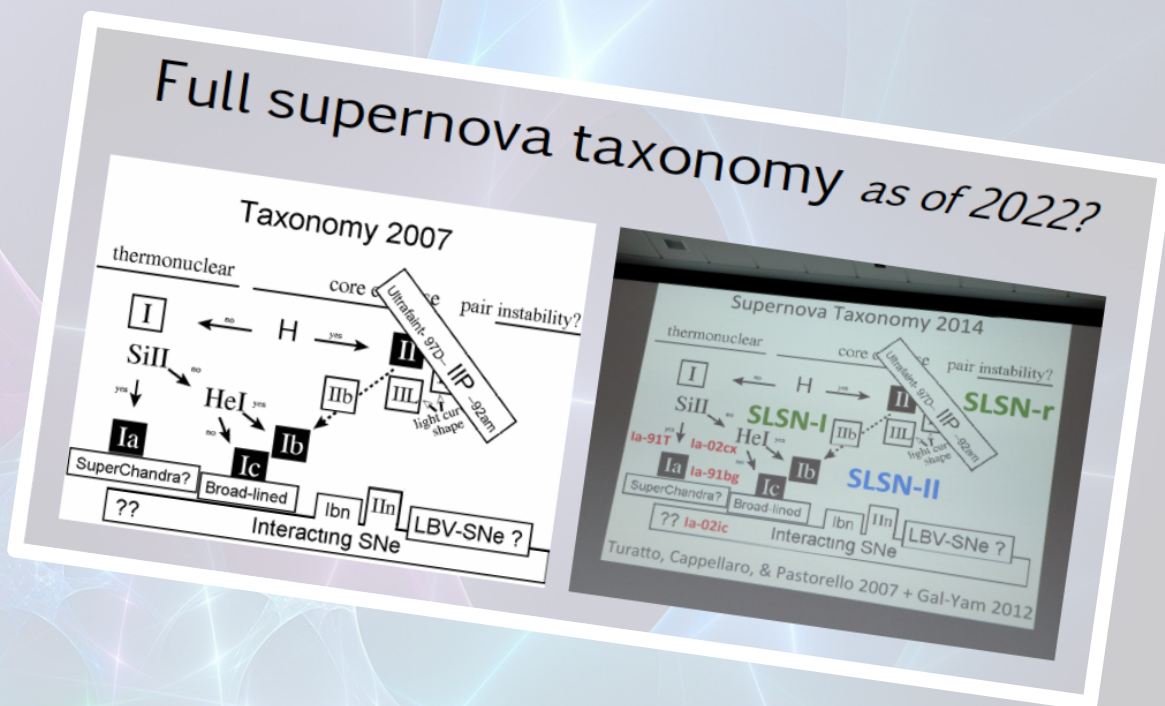
*This is only true:* single stars  
 at solar metallicity  
 no (or slow) rotation

\*stripping = loss of H-rich top layers  
 In the context of *single* stars:  
 'stripping' is due to losing mass in the strong wind  
 In the context of *binary* stars:  
 mass transfer



# What happens at

- sub-Solar metallicities?
- fast-rotating stars?
- stars in a binary system?



# Sub-Solar metallicities

(and still no rotation and no binary companion)

- Main effect: mass loss becomes **WEAKER**



# Sub-Solar metallicities

(and still no rotation and no binary companion)

- Main effect: mass loss becomes WEAKER
  - stars live their lives with more mass retained
  - also *end* their lives with more mass retained

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## Consequence #1:

- if an iron core is able to form, then it will be a **more massive** one

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  - higher chance to form a BH after the collapse

# Star metallicities

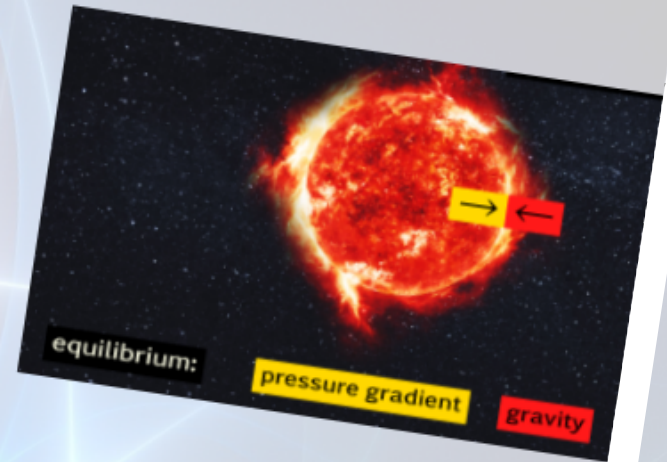
## Core collapse

(and no binary companion)

- Gravity takes over
  - end of the long-term equilibrium
  - fall-in: on the free-fall timescale
- ...is there something to stop it?
  - Well... it depends.

Most of the time ("classical" case): a neutron star forms in the center ("proto-neutron-star")

- a neutron star is: one giant nucleus. dense. stable.
- bounce-back, shock waves, emission of neutrinos and light = **SUPERNOVA EXPLOSION**



Cons

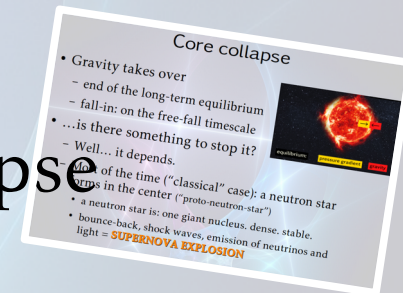
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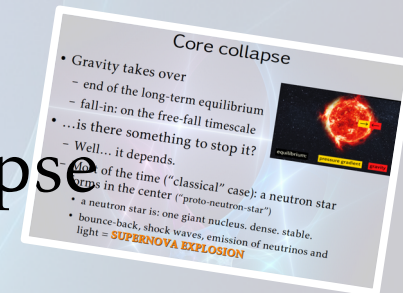
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  - higher chance to form a BH after the collapse
  - key question: is there something to **STOP** the collapse?



# Sub-Solar metallicities

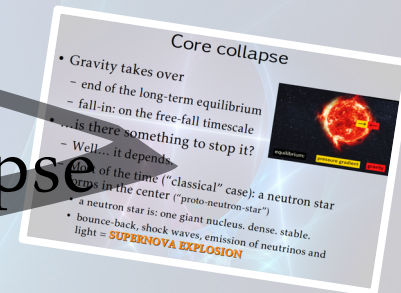
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- key question: is there something to **STOP** the collapse?
- if yes: CCSN
  - type II, Ib/c



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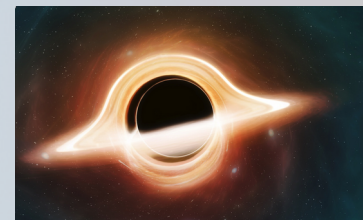
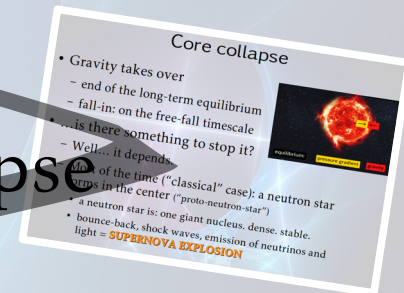
## Consequence #1:

- if an iron core is able to form, then it will be a **more massive** one

– higher chance to form a BH after the collapse

– key question: is there something to **STOP** the collapse?

– if yes: CCSN      if no: direct fall-in into a BH  
type II, Ib/c      no explosion



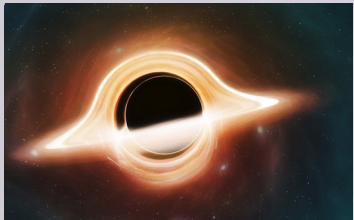


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**Consequence #1:**



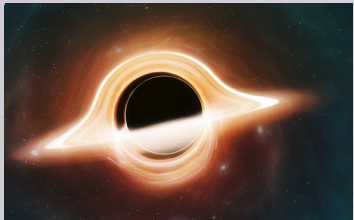
**Consequence #2:**

# Sub-Solar metallicities

(and still no rotation and no binary companion)

- Main effect: mass loss becomes WEAKER
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## Consequence #1:



## Consequence #2:

sometimes even the iron-core won't be able to form

# Why?

# Pair Instability

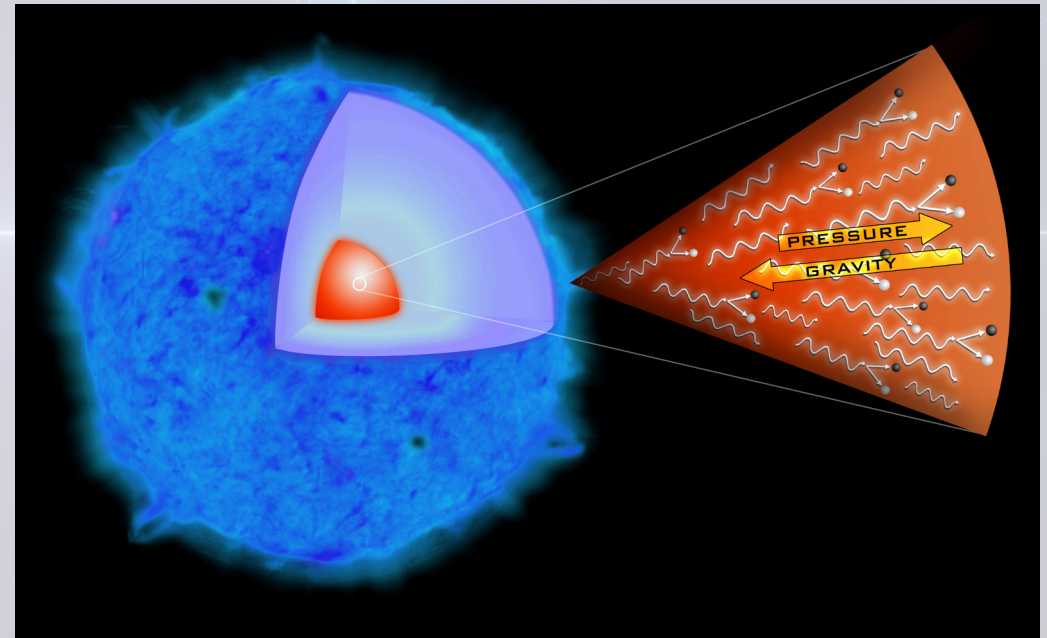
happens in *quite* massive stellar cores

Photon pressure  
drops due to  
 $\gamma\gamma \rightarrow e^- \text{ \& \ } e^+$

Collapse

Explosive O-burning  
→ supernova

No remnant!



# Why?

# Pair Instability

happens in *quite* massive stellar cores

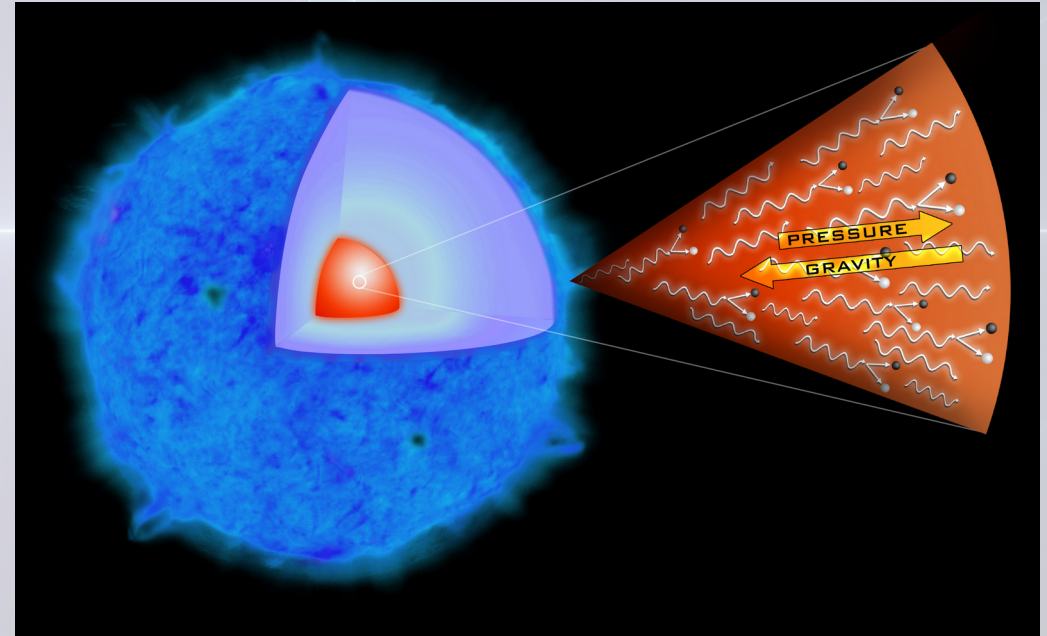
Photon pressure  
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can happen  
already in stars  
with  $\approx 60 M_{\odot}$

Collapse

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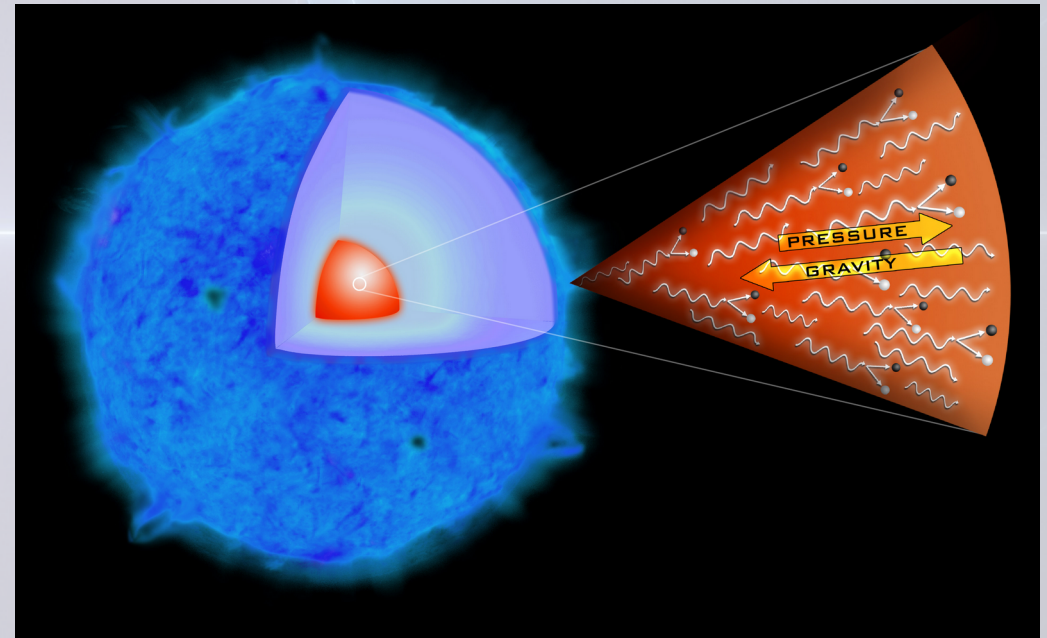
Collapse

*key question, as always:  
is there something to stop it?  
...if not:*

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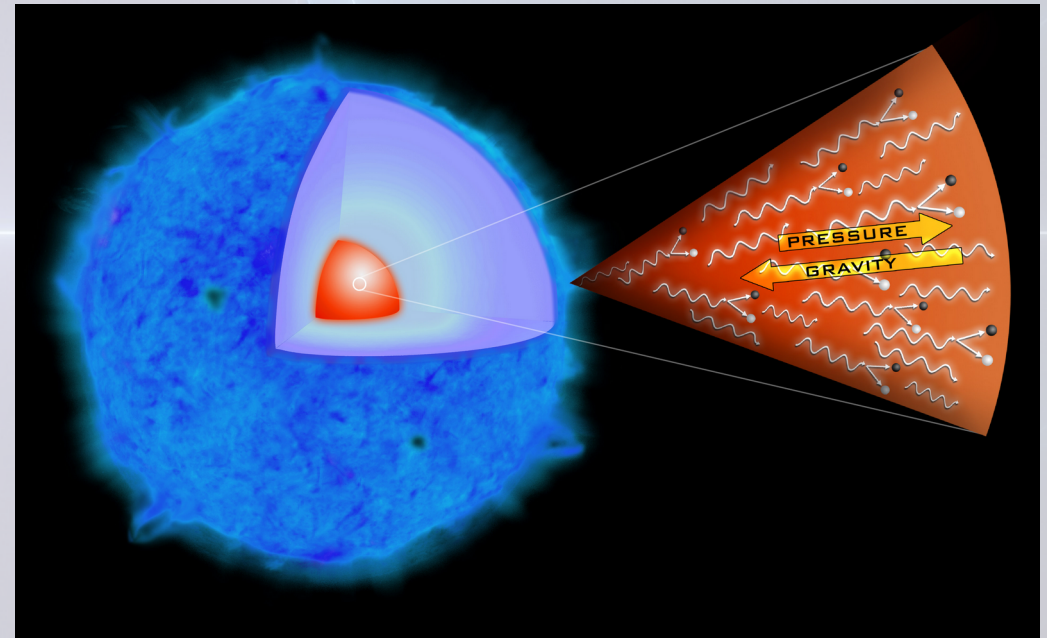
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happens with stars  
 $\sim 140\text{-}260 M_{\odot}$

No remnant!



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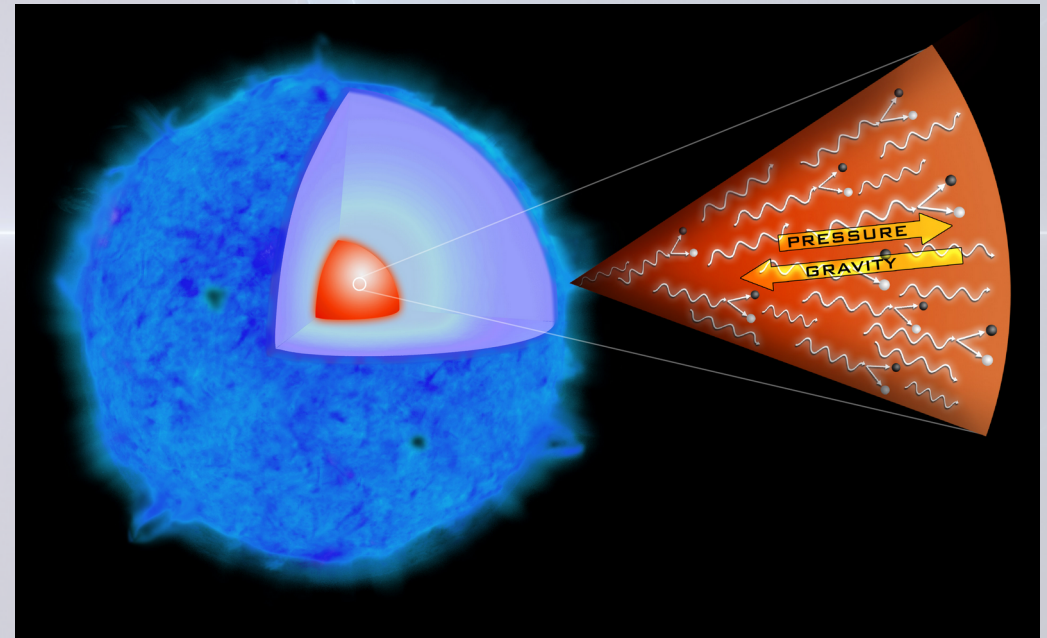
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## Explosive O-burning

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pair-instability supernova (PISN)

## No remnant!



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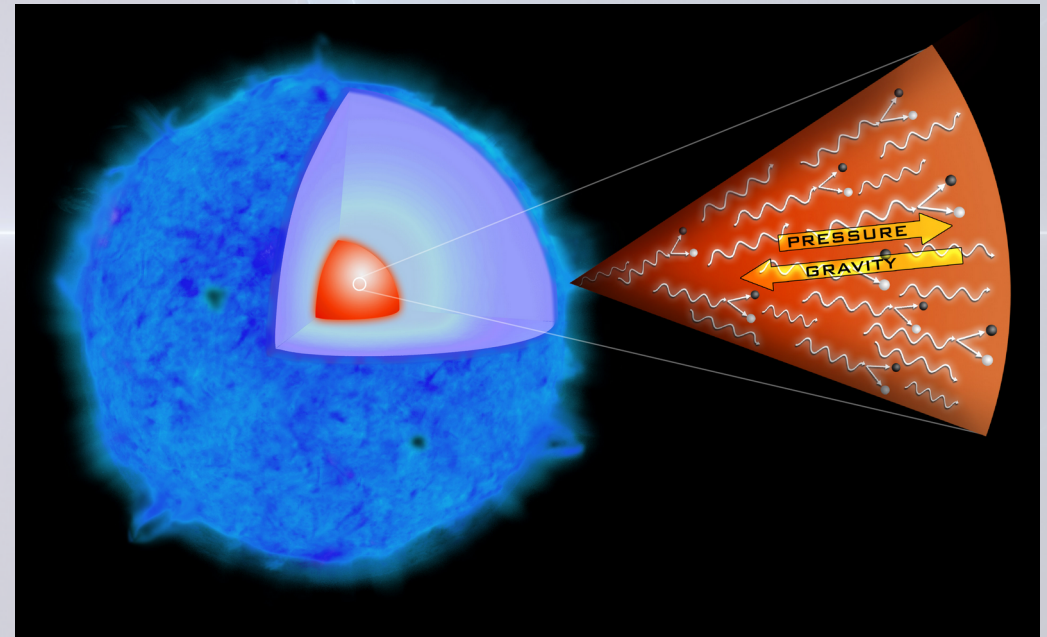
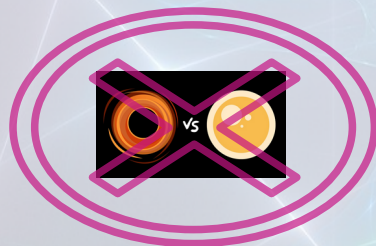
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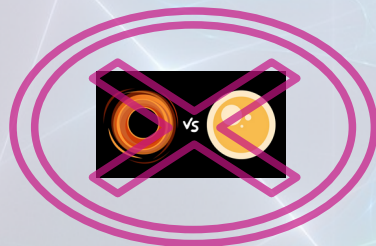
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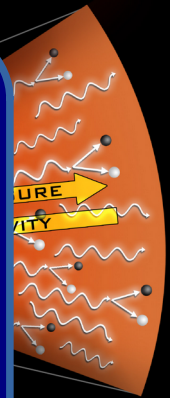
pair-instability supernova (PISN)

No remnant!



Note:

- iron-core stage is not even reached yet
- **whole star explodes**
- nucleosynthetic yield (ejected material's composition) is different from classical CCSNe
- have we ever observed such a SN?  
*...who knows*



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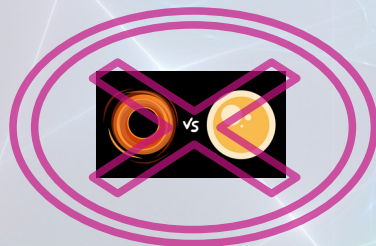
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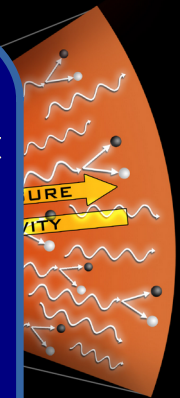
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stars between  $60\text{-}140 M_{\odot}$ :  
*collapse is  
stopped by the star  
re-gaining its hydrostatic  
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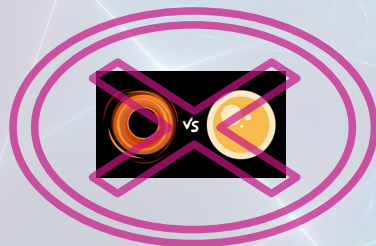
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## Explosive O-burning

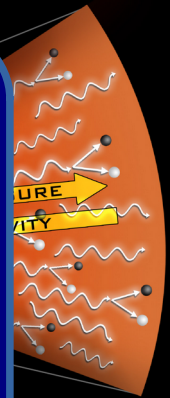
→ supernova happens with stars  
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pair-instability supernova (PISN)

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stars between  $60\text{-}140 M_{\odot}$ :  
*collapse is  
stopped by the star  
re-gaining its hydrostatic  
stability*

might\* lead to a  
'pulsational pair-instability supernova' (pPISN)

because layers lost in the pulsations  
*might* collide and emit light

above  $260 M_{\odot}$ :  
again direct collapse into BH  
(gravity wins)

# Pair Instability

happens in *quite* massive stellar cores

Photon pressure  
drops due to  
 $\gamma\gamma \rightarrow e^- \text{ \& \ } e^+$

can happen  
already in stars  
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Collapse

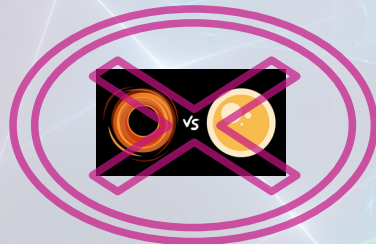
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Explosive O-burning  
→ supernova

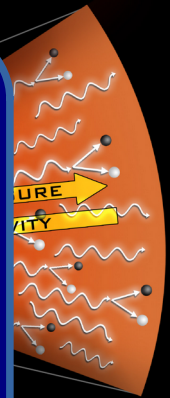
happens with stars  
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pair-instability supernova (PISN)

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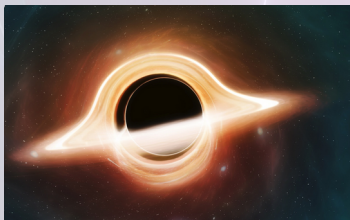
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# Sub-Solar metallicities

(and still no rotation and no binary companion)

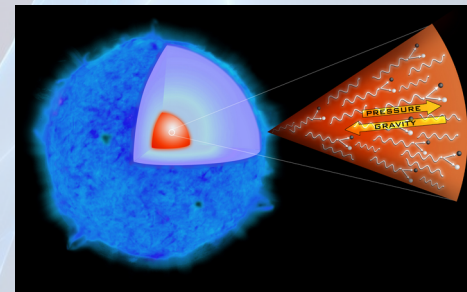
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## Consequence #1:



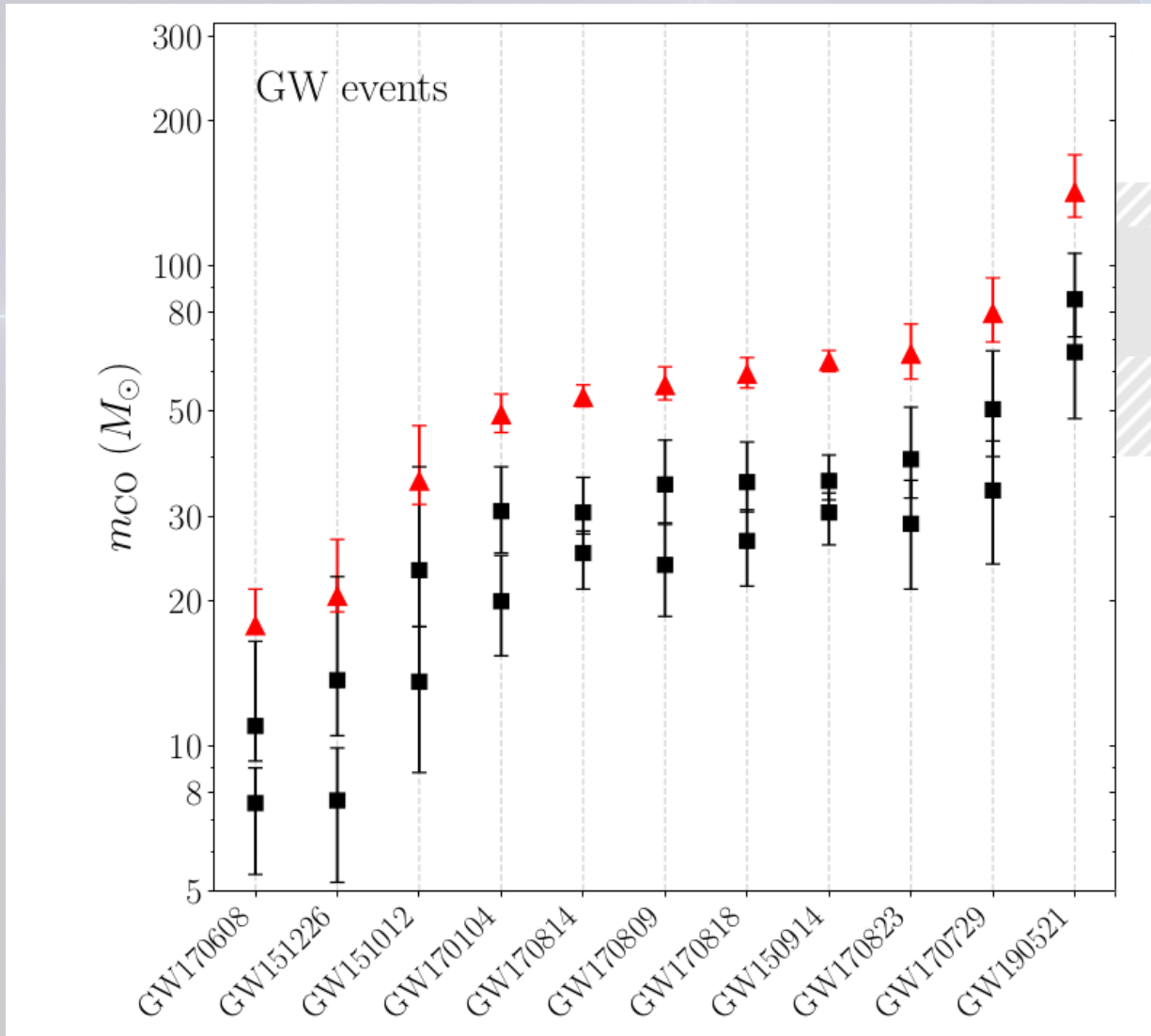
direct fall-in into  
a black hole  
(of mass  $\sim 20\text{-}40 M_{\odot}$ )

## Consequence #2:



pair-instability developing, leading to  
a PISN (or maybe a pPISN)  
or again to direct fall-in to a BH  
(*but this will be a very heavy BH with  $>150 M_{\odot}$* )

# The BHs of GW190521 shouldn't exist...



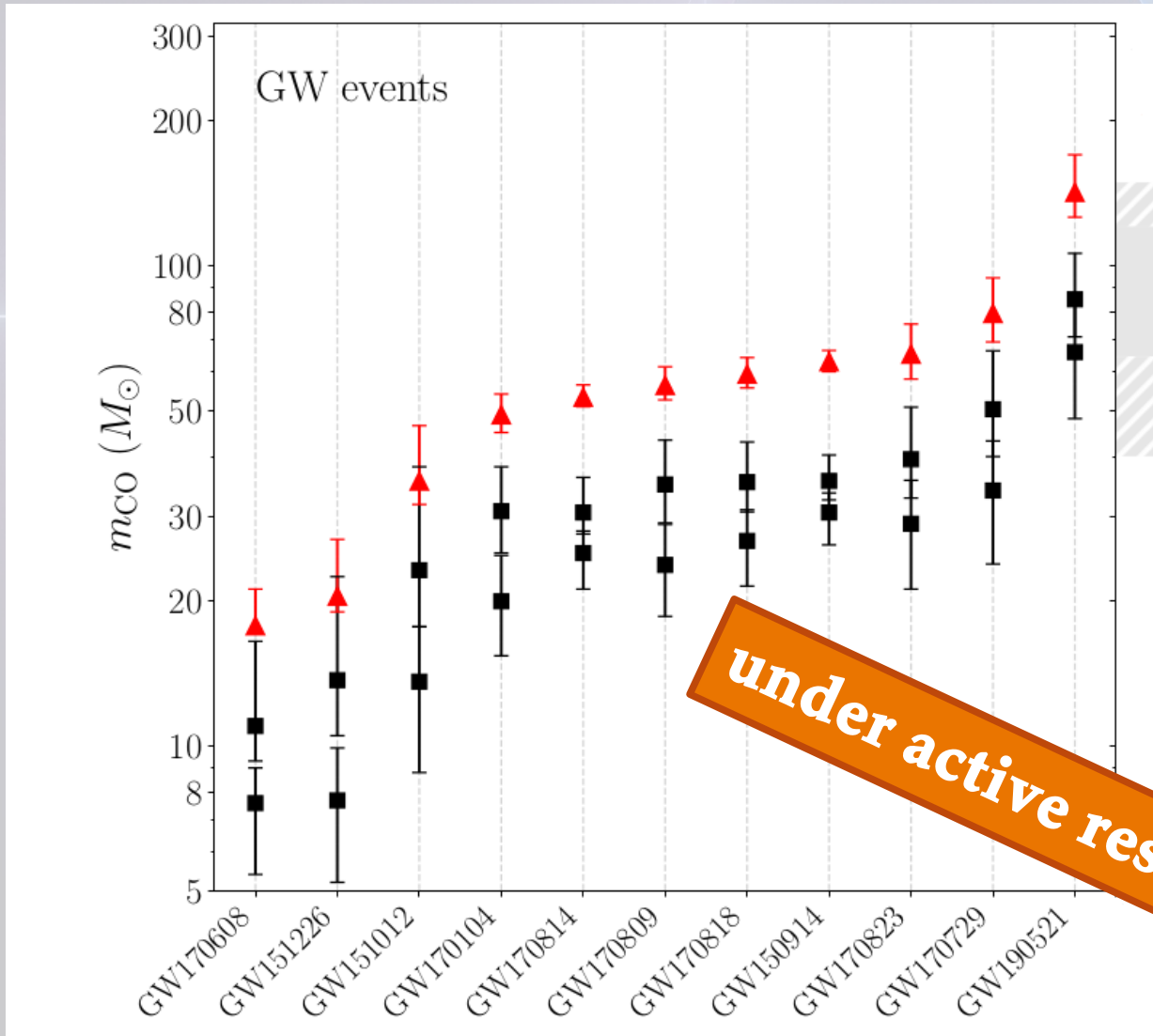
BH no go zone

**GW190521:**

$m_1 = 85 (+21/-14)$   
Msun

$m_2 = 66 (+17/-18)$   
Msun

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BH no go zone

**GW190521:**

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