

Gravitational-wave progenitors

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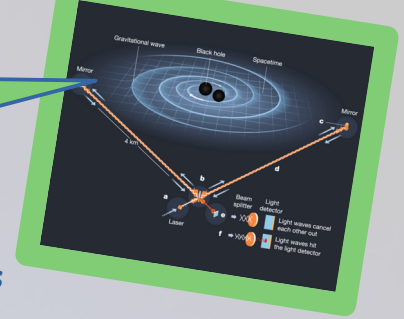
Lecture #8

NCU, Summer Semester 2022

*Previously
on GW-progenitors...*

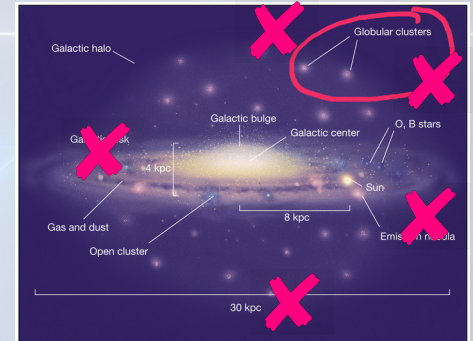
To form very heavy BHs (which go on to merge & emit GWs), low-metallicity is needed.

massive stars have strong, Z-dependent winds

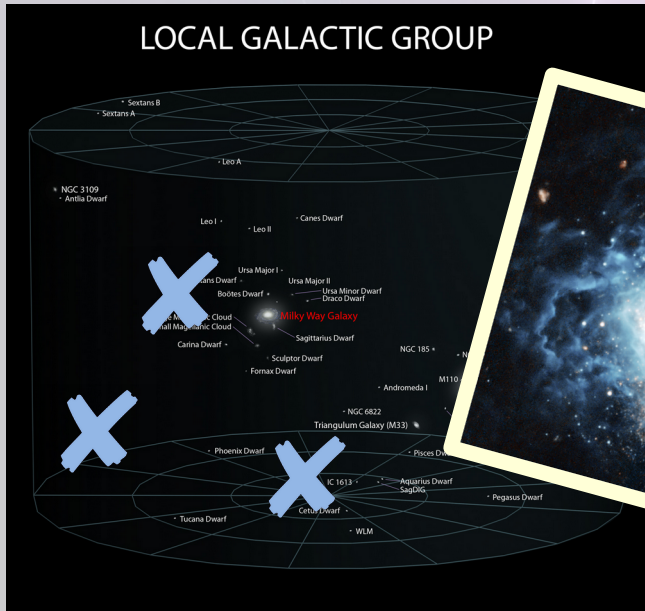


Where can we find stars* *gas/galaxies/anything: "environments" with sub-Solar Z?

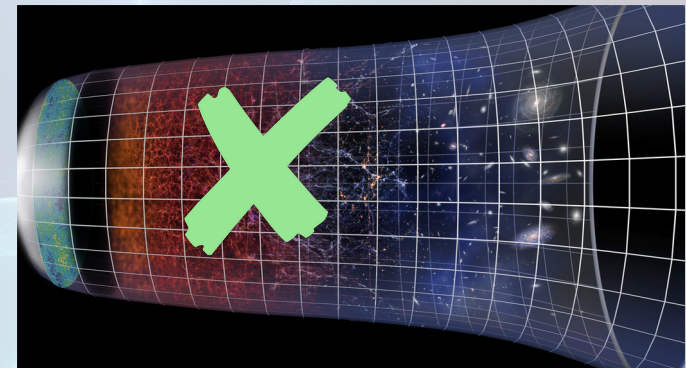
Globular clusters



Dwarf galaxies



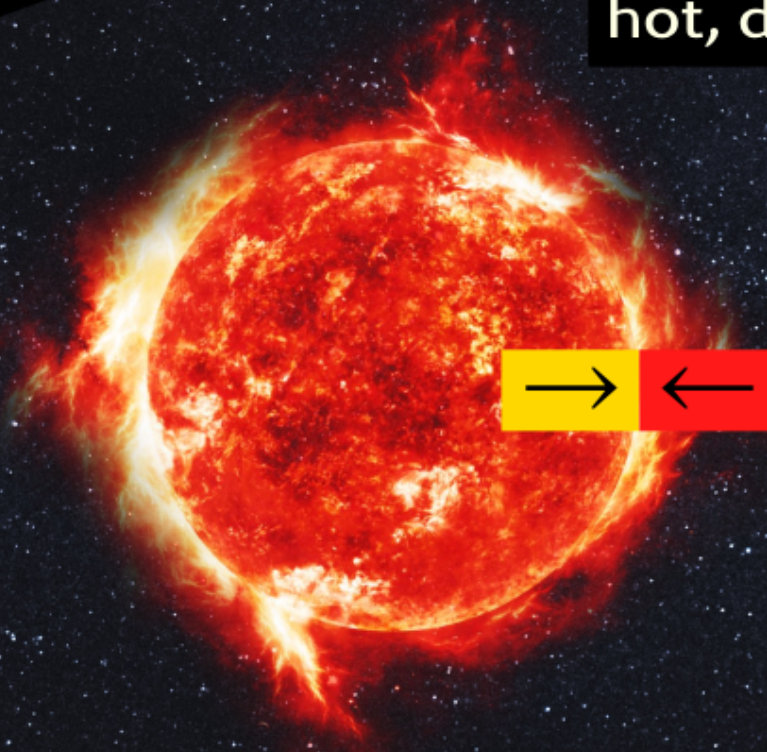
Early Universe



What is a star?

surface?
→ photons escape
"photosphere"

hot, dense plasma



equilibrium:

pressure gradient

gravity

Theoretical modelling of the stellar structure

$$\frac{\partial r}{\partial m_r} = \frac{1}{4\pi r^2 \rho} \quad \text{equation of mass conservation} \quad (1)$$

$$\frac{\partial P}{\partial m_r} = -\frac{Gm_r}{4\pi r^4} \quad \text{equation of momentum conservation} \quad (2)$$

$$\frac{\partial L_r}{\partial m_r} = \epsilon_{\text{pl}} - T \frac{\partial S}{\partial t} \quad \text{equation of energy conservation} \quad (3)$$

$$\frac{\partial T}{\partial m_r} = -\frac{Gm_r T}{4\pi r^4 P} \nabla \quad \text{equation of transport of energy} \quad (4)$$

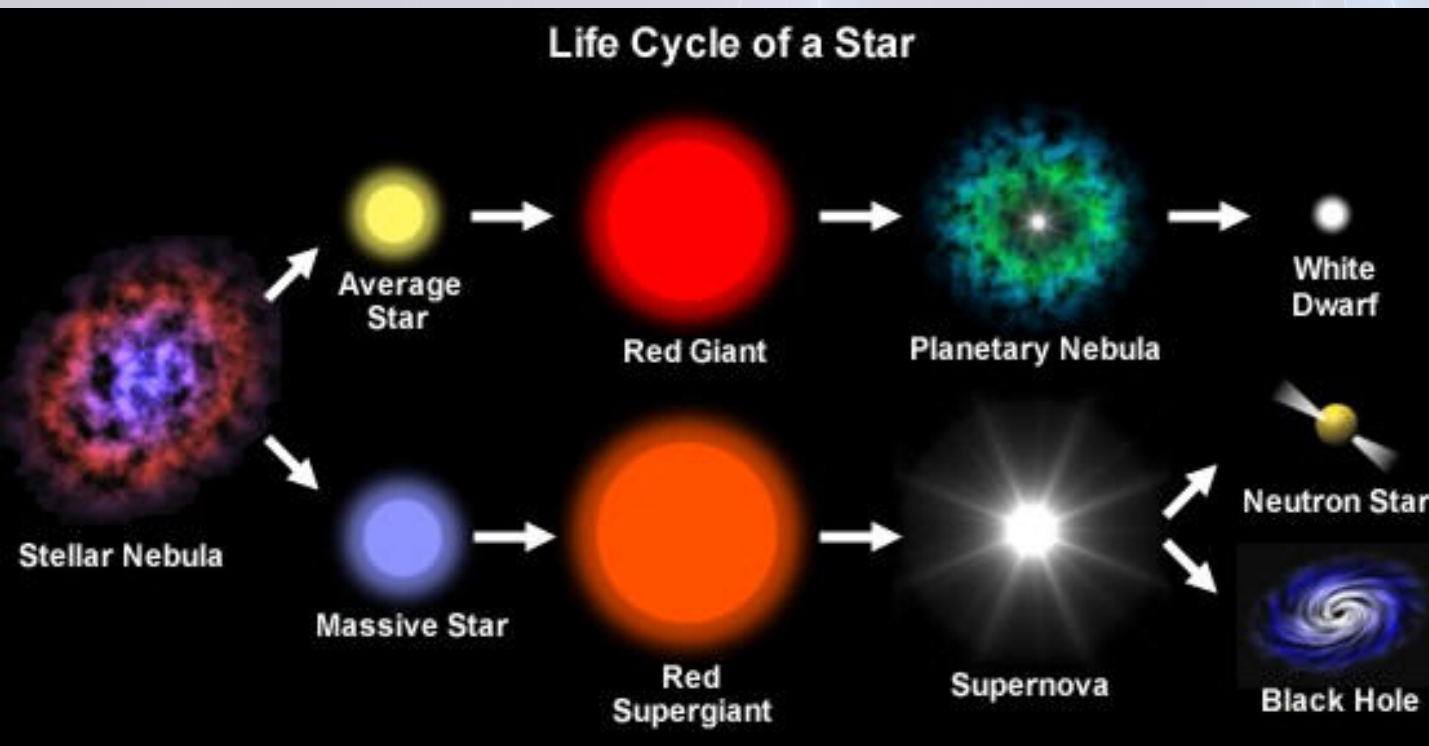
Guilera+ 11

composition change due to nuclear burning:

$$\frac{\partial X_i}{\partial t} = \frac{A_i m_u}{\rho} (-\sum_{j,k} r_{i,j,k} + \sum_{k,l} r_{k,l,i}) \quad (5)$$



stars evolve → stellar evolution



low-mass: $< 8 M_{\odot}$

massive: $> 8 M_{\odot}$

(simplistic...)

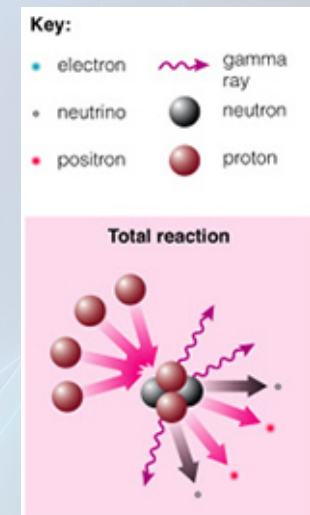
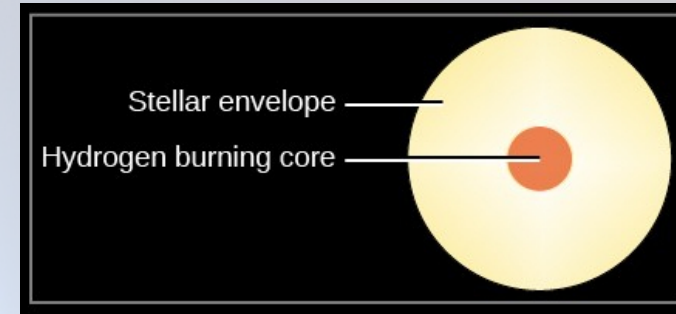
Our strategy is/has been:

start with
Massive Stars at Solar Z

- sub-Solar metallicities?
- fast-rotating stars?
- stars in a binary system?

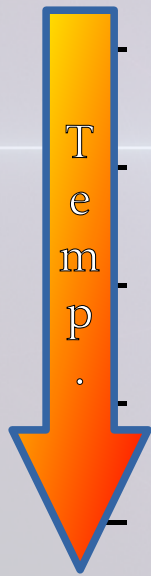
Longest phase of stellar evolution: MS

- Main Sequence
 - **core**-hydrogen-burning phase
- lasts for ~90% of the lifetime (longest of them all)
- core temperatures: ~40M K
- in massive stars: CNO cycle
 - low-mass stars like the Sun: pp-chain
- $4\ ^1\text{H} \rightarrow\ ^4\text{He} + \gamma$
- end of MS: Terminal-Age Main Sequence (TAMS)



Post-MS

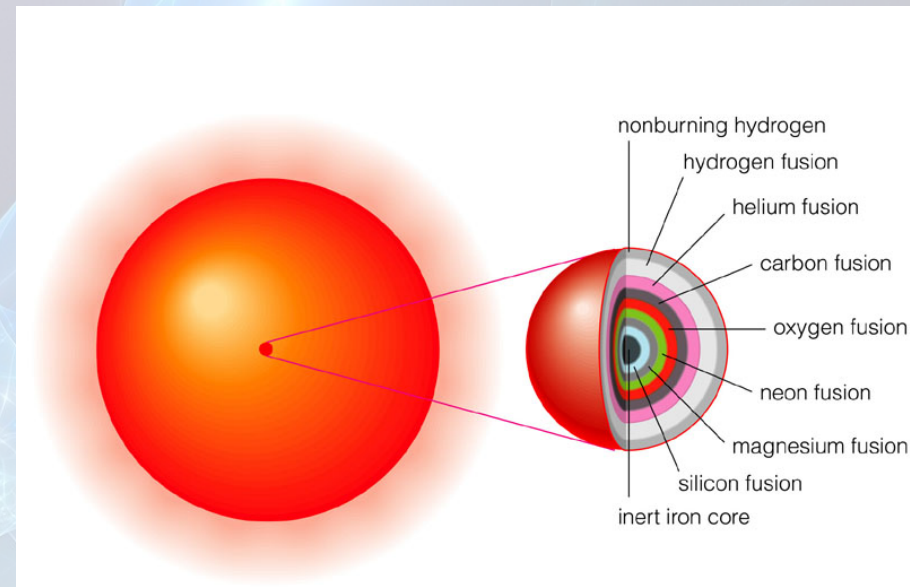
- Includes:



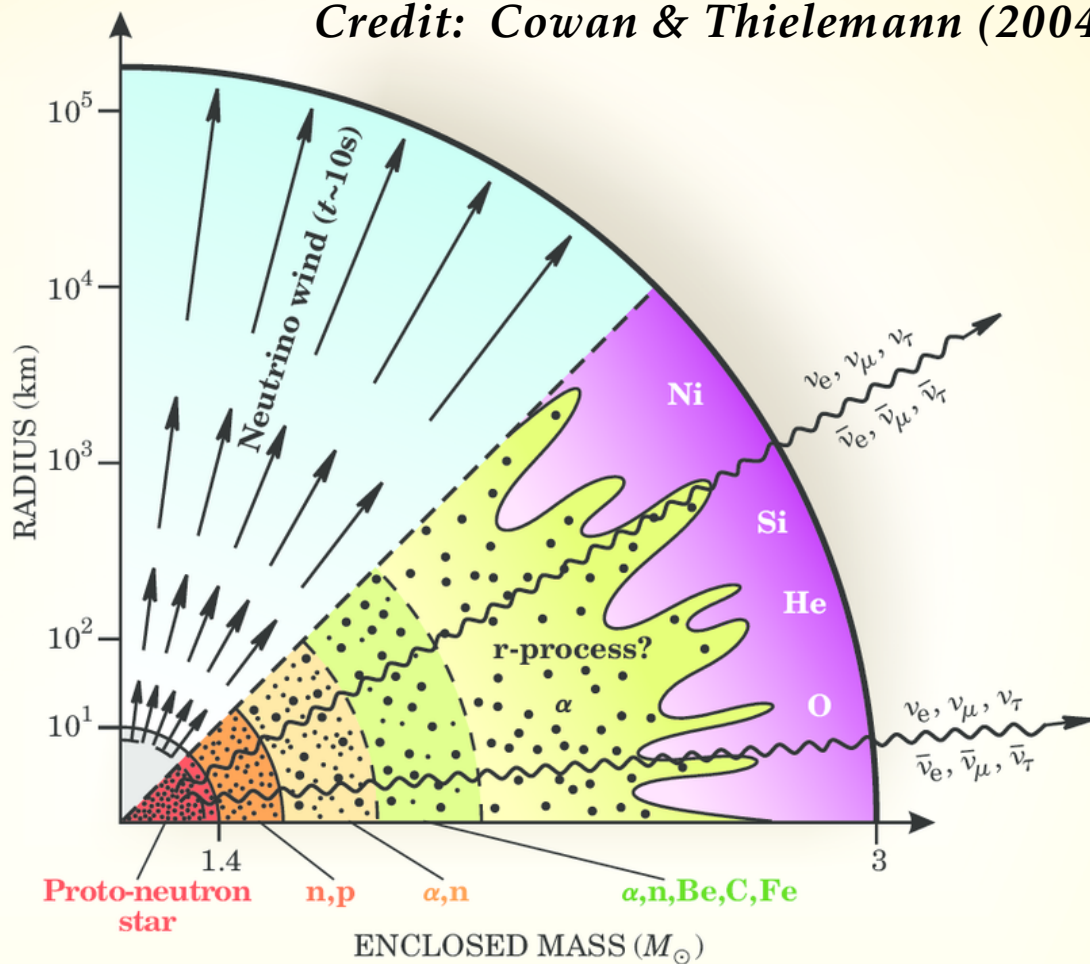
- core-He-burning (& shell-H-burning)
- core-C-burning (& shell-He & shell-H-burning)
- core-O-burning (& shell-C, shell-He, shell-H...)
- core-Ne-burning (& shell...)
- core-Si-burning (& shell...)

- **onion-structure** of massive stars

Note: the onion layers become more and more complex nearing the end of the lifetime

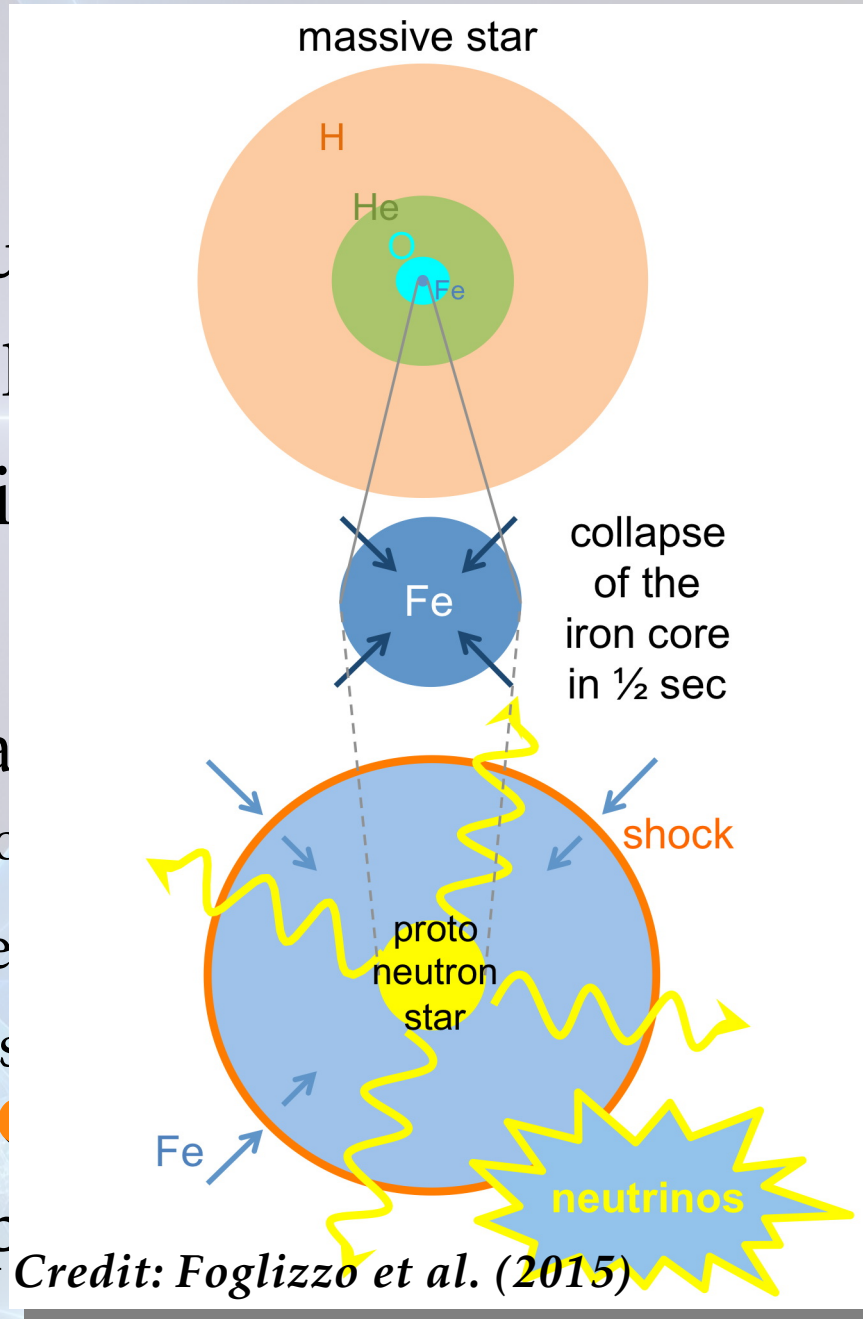


Credit: Cowan & Thielemann (2004)



apse

- forms in the center (“proto-neutron star”)
- a neutron star is: one giant nucle
 - bounce-back, shock waves, emiss
 - light = **SUPERNOVA EXPLOSION**
- technically: a core-collapse supernova

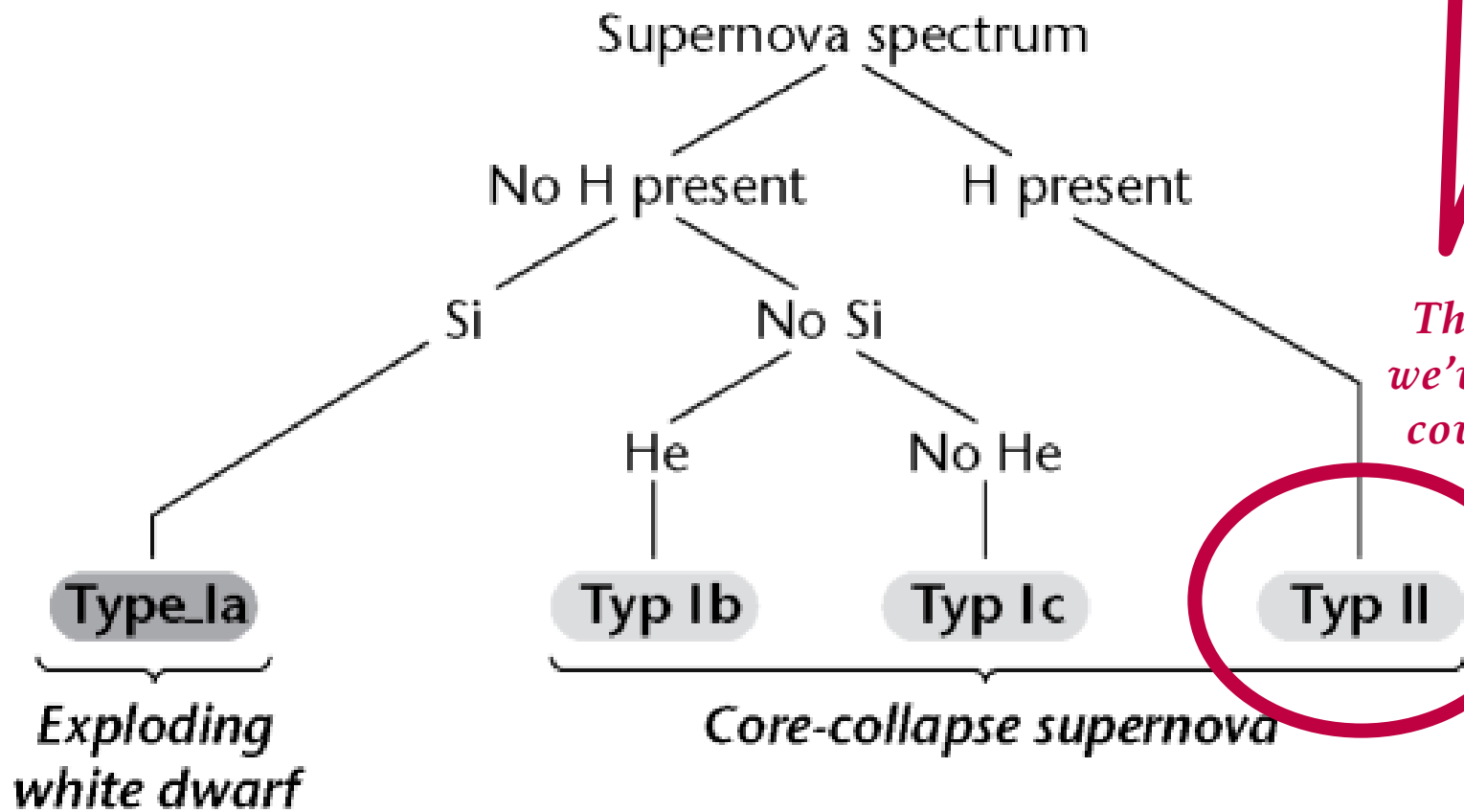


Credit: Foglizzo et al. (2015)

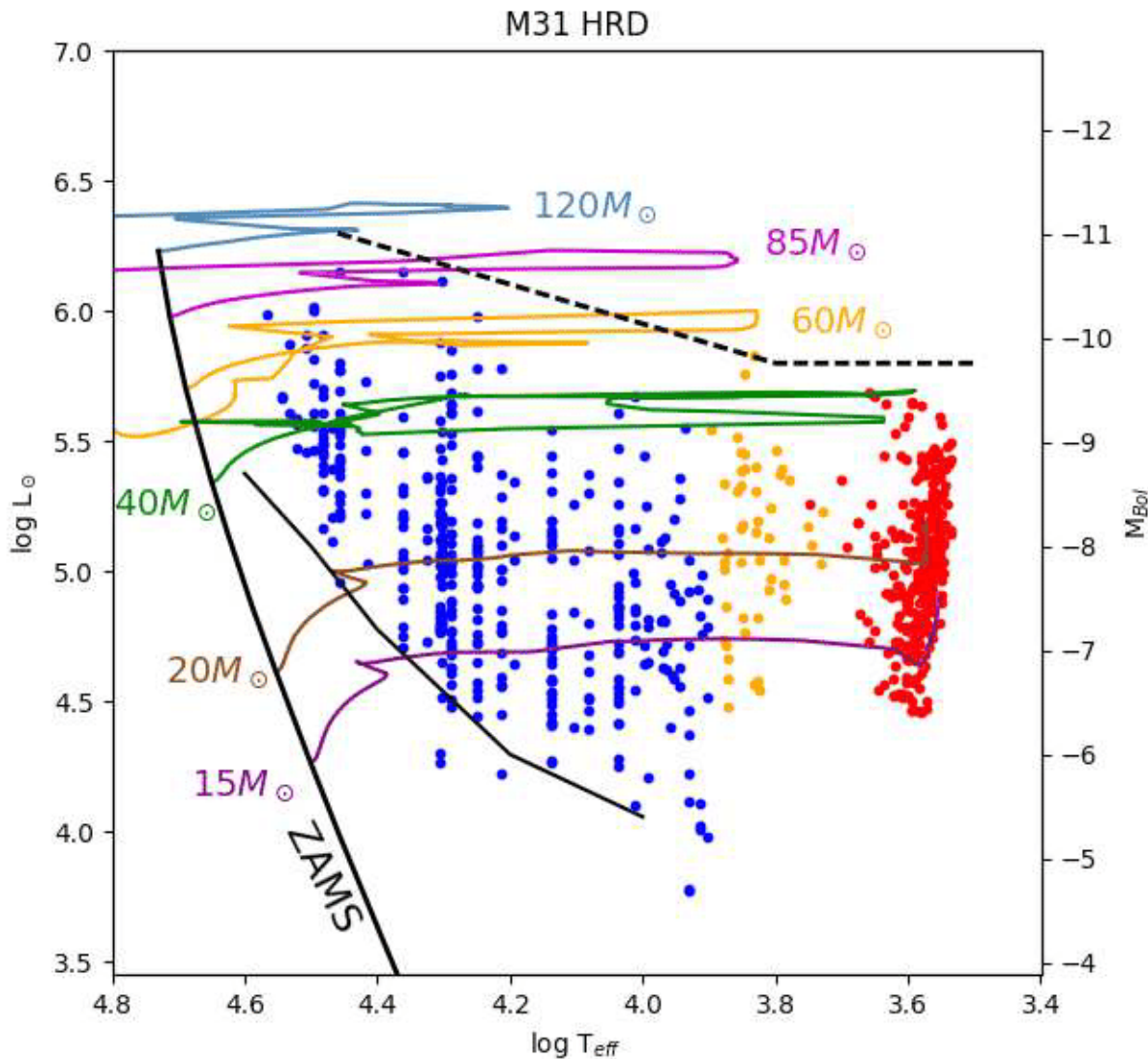
So far: core-collapse SNe

- There are so many other types...
- Classified by observers (simple picture):

Progenitor:
a massive star with
a H-rich envelope



*stripping = loss of H-rich top layers
In the context of *single* stars:
'stripping' is due to losing mass in the strong wind
In the context of *binary* stars:
mass transfer



'stripped' progenitor*
(e.g. a Wolf-Rayet star)
→ **type Ib or Ic**

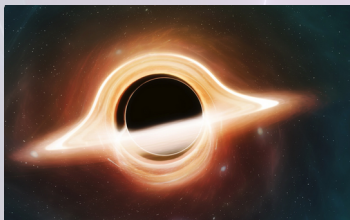
red-supergiant progenitor
→ **type II**

Sub-Solar metallicities

(and still no rotation and no binary companion)

- Main effect: mass loss becomes WEAKER
 - stars live their lives with more mass retained
 - also *end* their lives with more mass retained

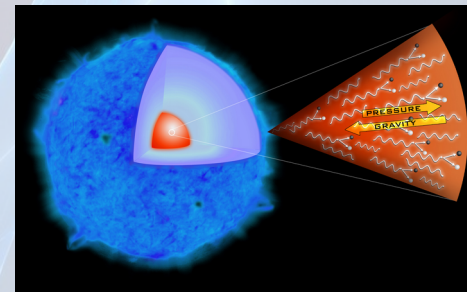
Consequence #1:



direct fall-in into
a black hole
(of mass $\sim 20-40 M_{\odot}$)

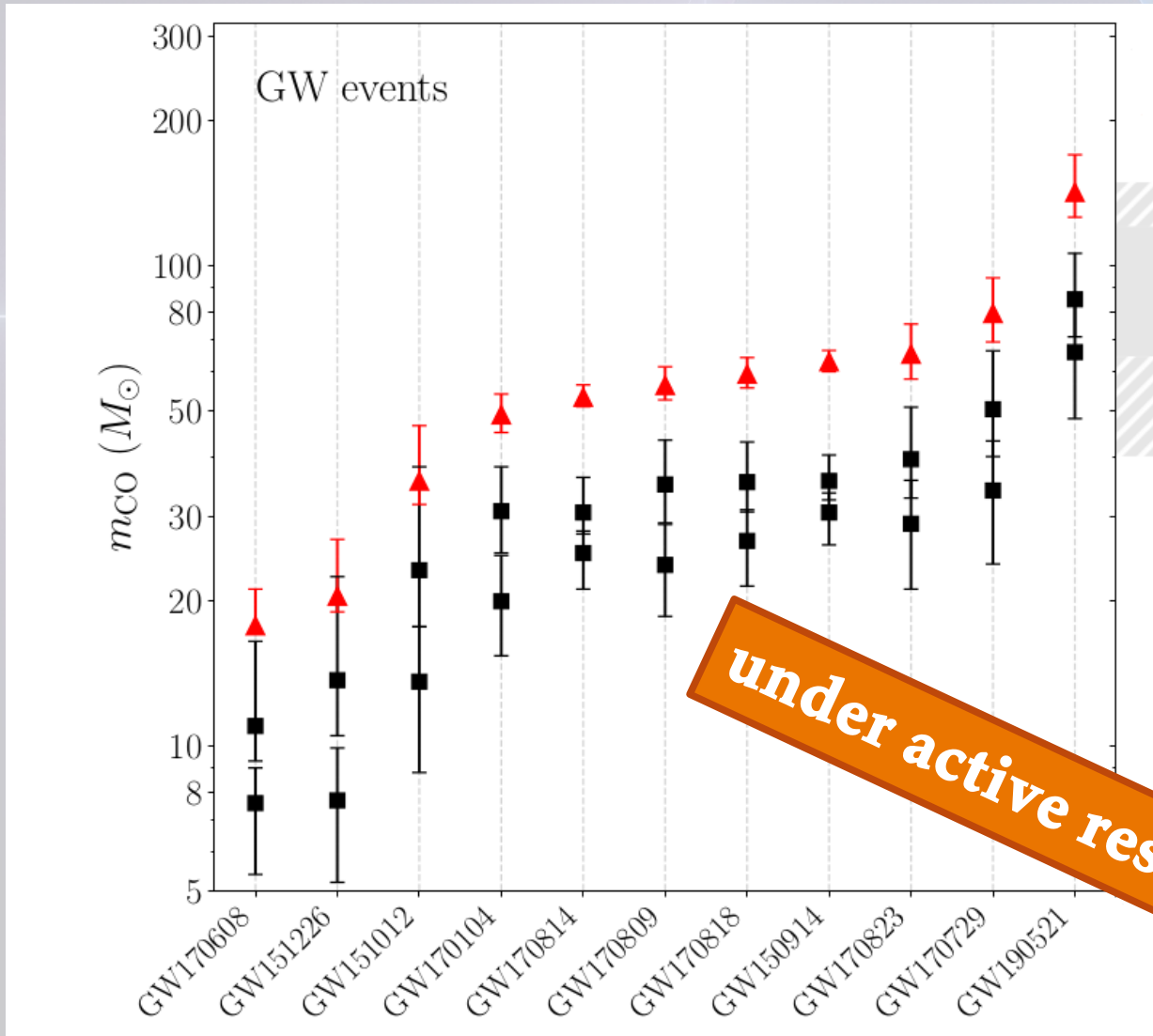
*key question: is there something to STOP
the collapse? if yes: CCSN (type II, Ib/c)
if no: direct fall-in into a BH (no explosion)*

Consequence #2:



pair-instability developing, leading to
a PISN (or maybe a pPISN)
or again to direct fall-in to a BH
(but this will be a very heavy BH with $>150 M_{\odot}$)

The BHs of GW190521 shouldn't exist...



BH no go zone

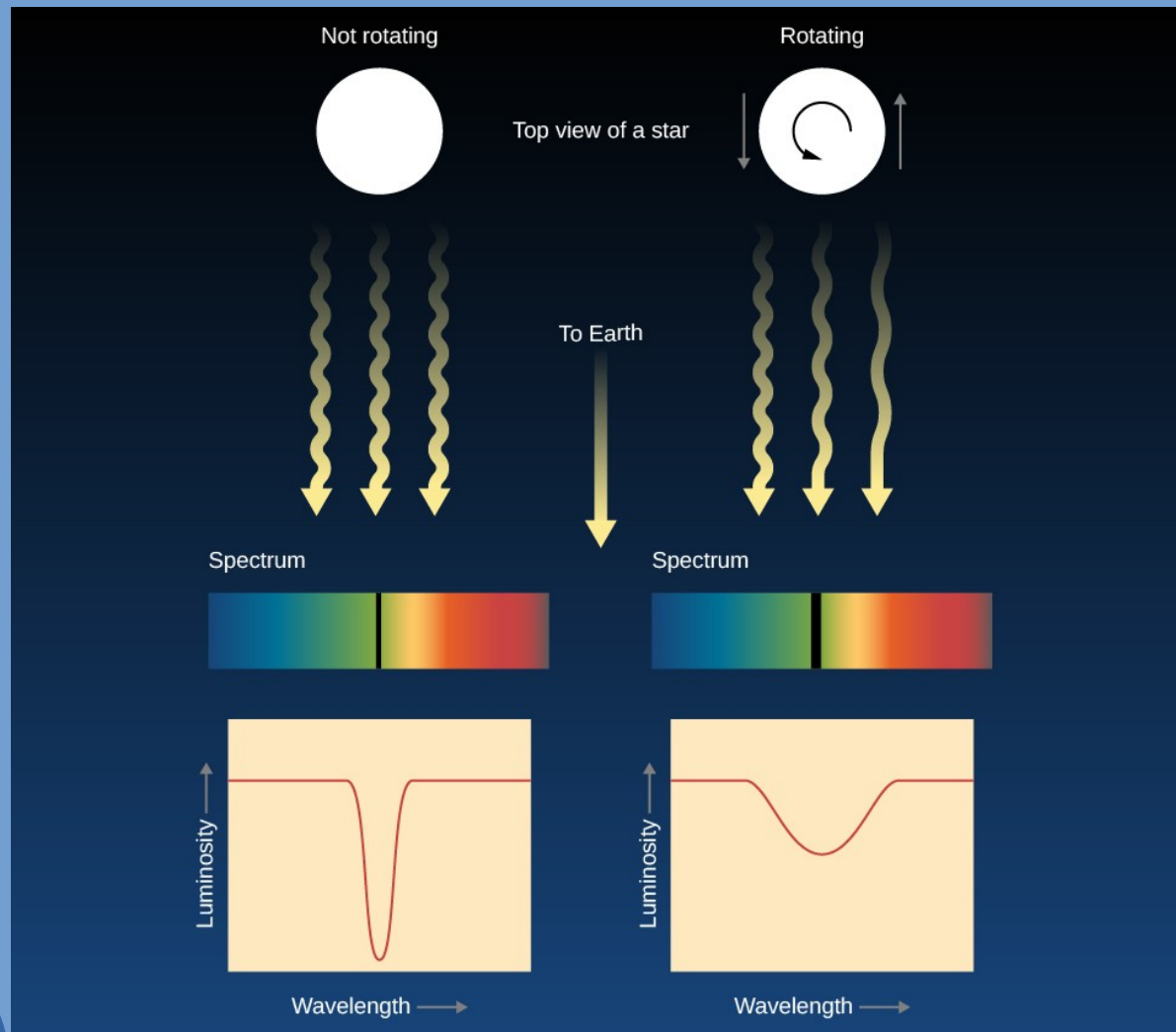
GW190521:

$m_1 = 85 (+21/-14)$
Msun

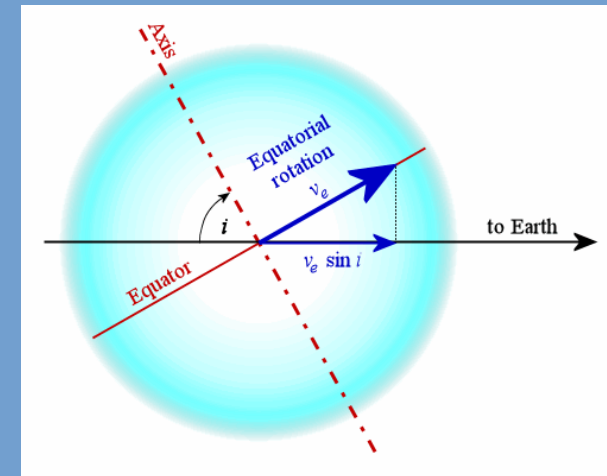
$m_2 = 66 (+17/-18)$
Msun

Massive stars rotate... sometimes quite fast

How do we know that? → line profile

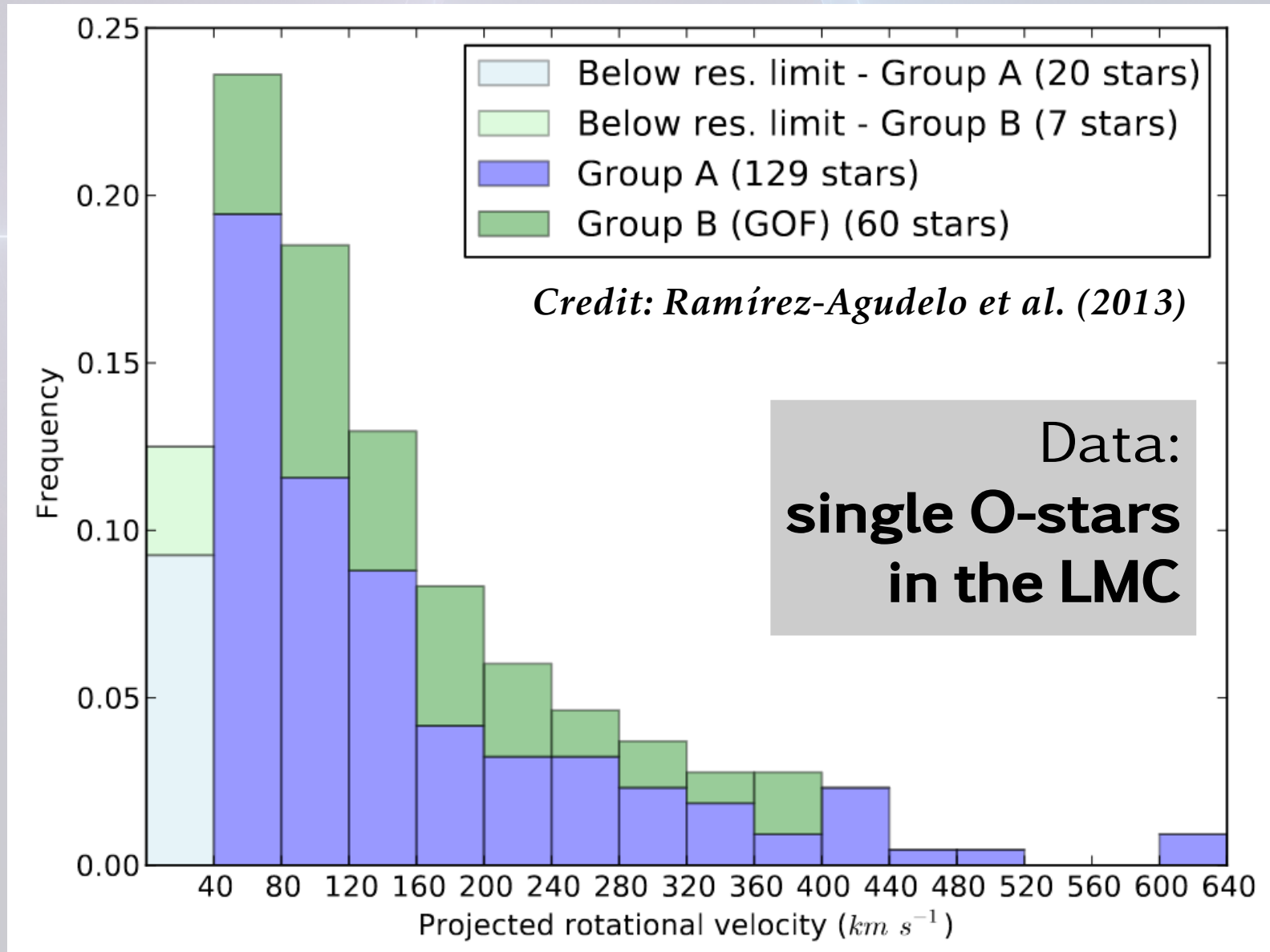


inclination?



$v \cdot \sin(i)$
("projected rotational velocity")

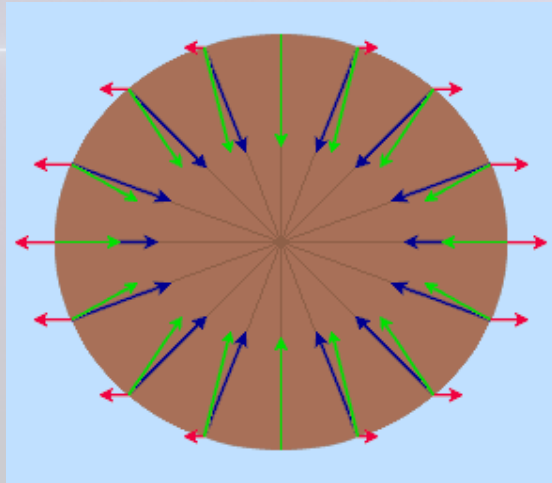
Massive stars rotate... sometimes quite fast especially at low Z!



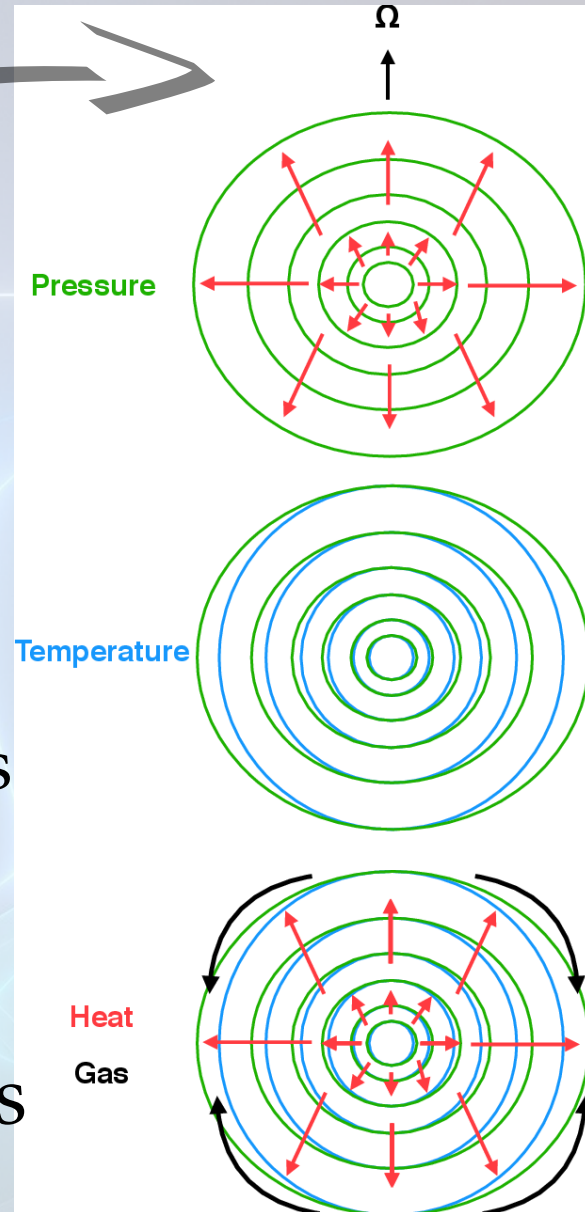
Theoretically considered:

Rotation can effect the structure

- centrifugal force
 - oblate shape
 - extra mixing inside!
- extreme case:
 - “break-up” rotation
“critical rotation”
 - $F_{\text{cen}} \geq F_{\text{grav}}$ “Keplerian break-up frequency”
 - leads to extra mass loss
 - mass dependent
e.g. “B[e] star” phenomenon



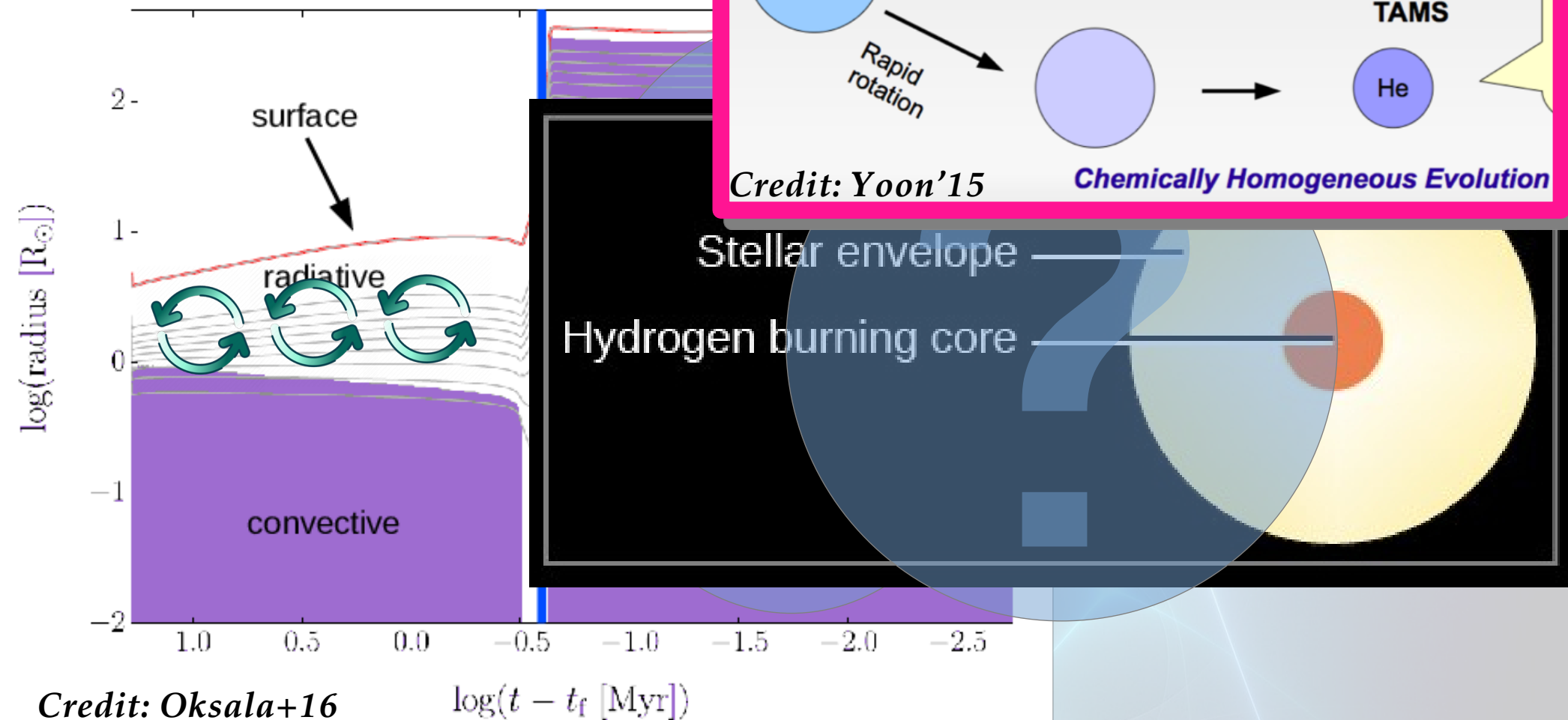
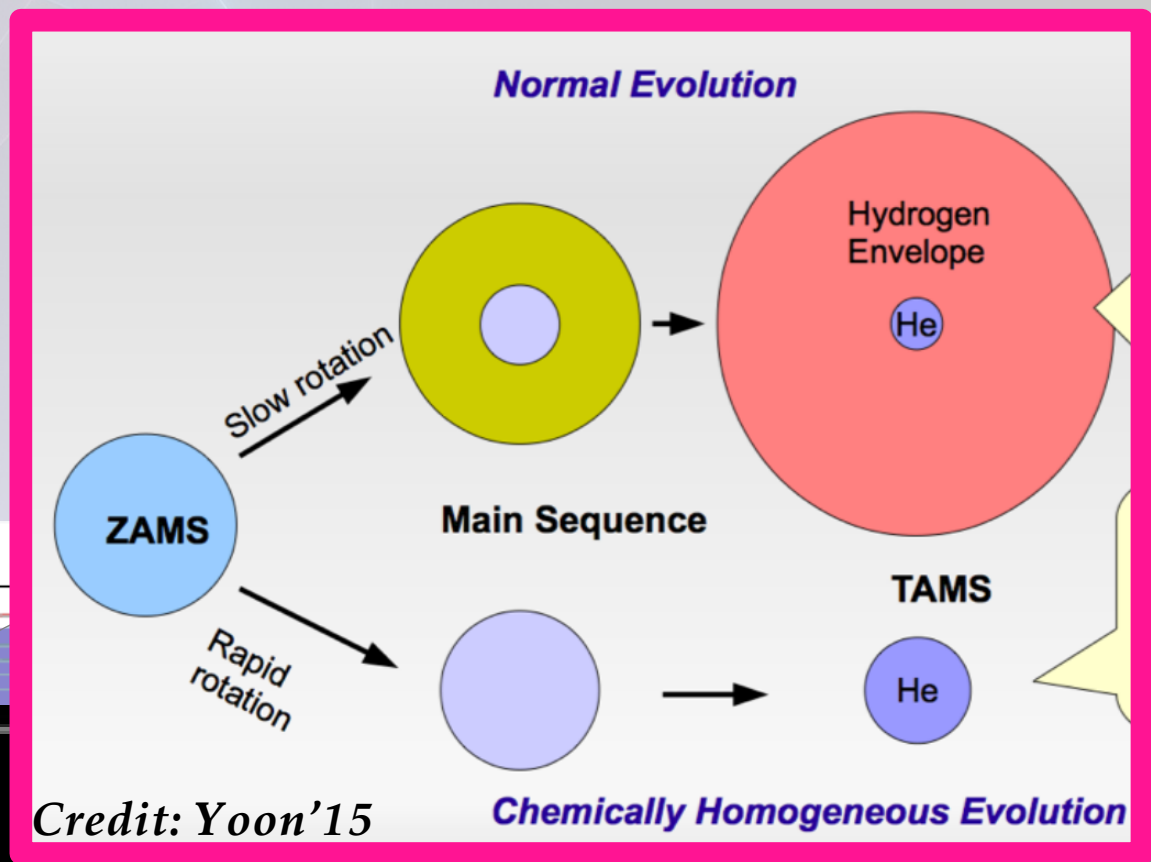
Credit: Jermyn+18



- non-extreme case: mixing & mass loss

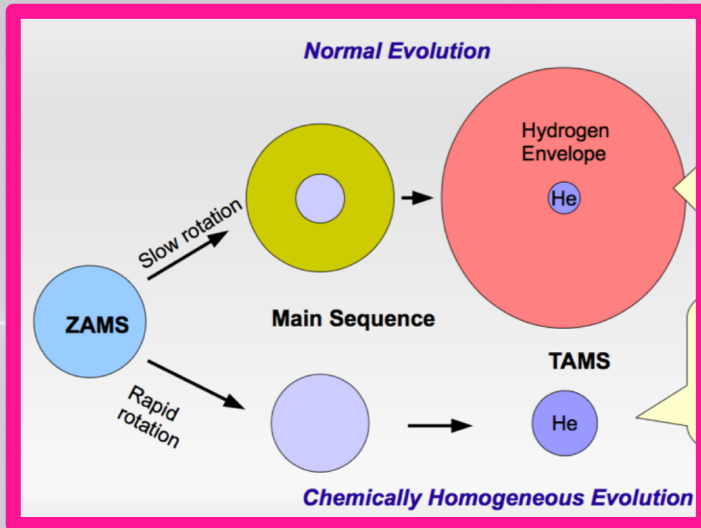
Rotational mixing

...but depends on Z too:
 metallicity mass loss;
 mass loss \rightarrow angular
 momentum loss

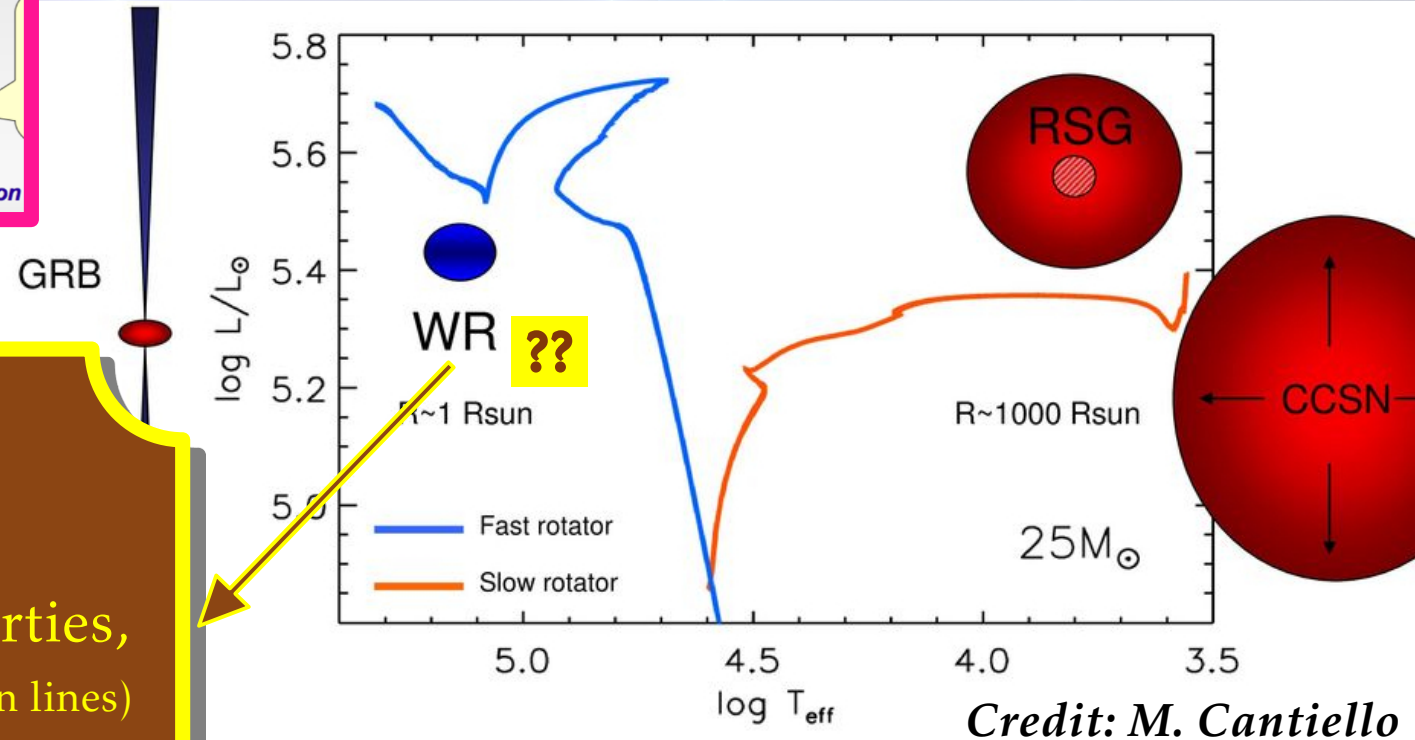


Chemically homogeneous evolution

= *Quasi-chemically homogeneous evolution*



In the Hertzsprung–Russell diagram:



Credit: M. Cantiello

a hot, He-rich star

depending on wind properties, might be a WR star (emission lines) or something else? (absorbtion lines)

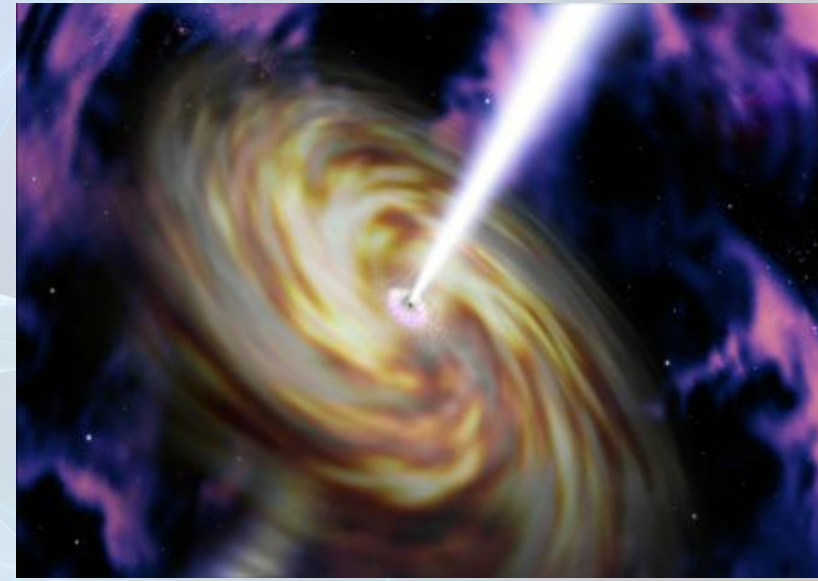
*Type of final explosion?
type Ib/Ic (core collapse)
but ROTATING!! → a 'collapsar'*

Collapsar

- “core collapse” \neq “collapsar”
- core collapse + fast rotation = collapsar
- collapsar \rightarrow accretion disc & jets
- if the jet aligns with the line of sight:
long-duration gamma-ray burst
may be observed (L-GRB)
 - accompanied by a SN Ib/Ic
- if not aligned: SN Ib/Ic

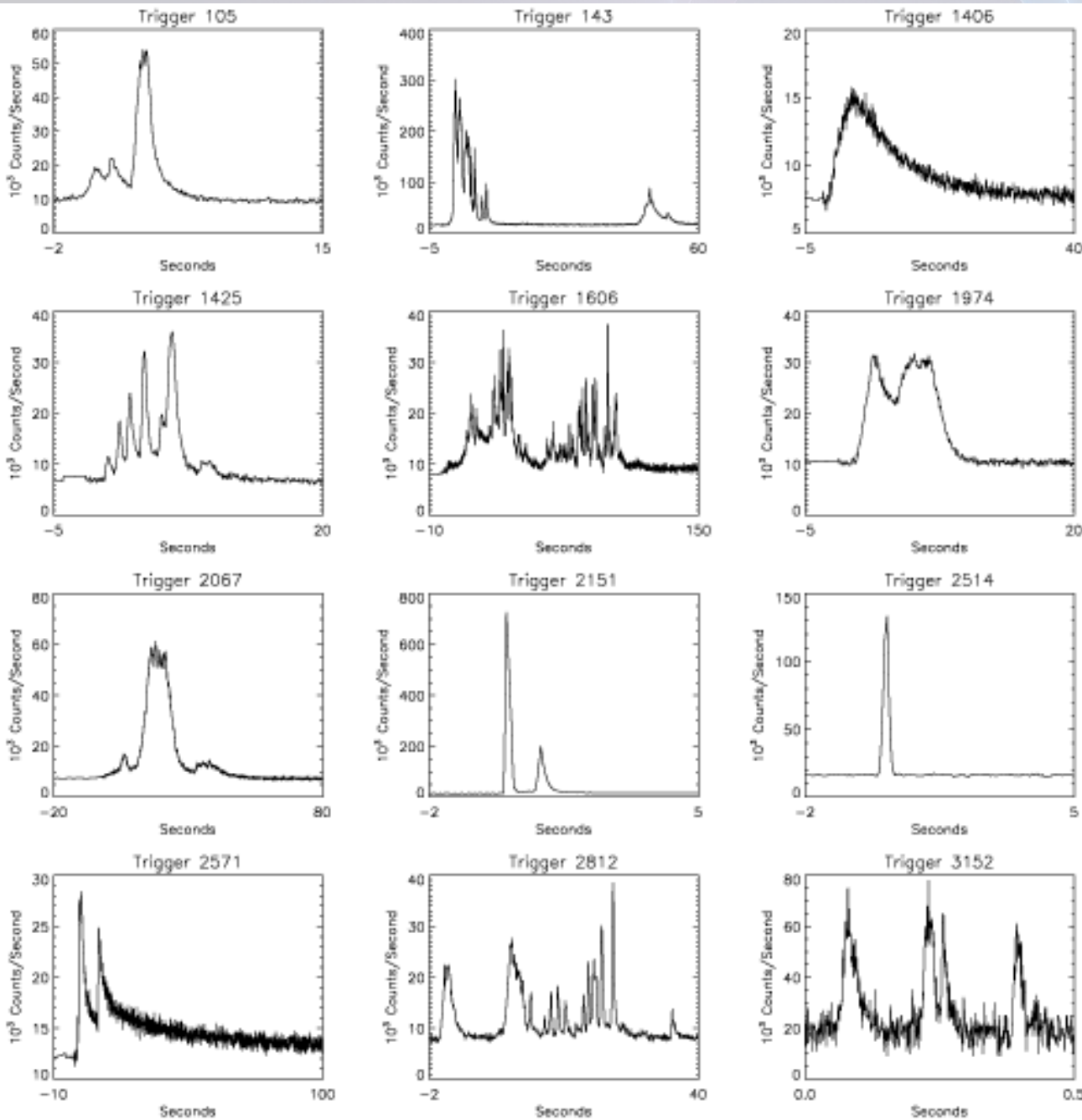
A BH or a NS forms
in the middle.
The proto-NS is probably
highly magnetized.

Synchrotron radiation
accelerated in the jet.
 γ -rays emitted.



What are GRBs?

Observationally...



– during the cold war...

– today: satellite missions

e.g.:

Fermi Gamma-ray Space Telescope
Neil Gehrels Swift Observatory etc.

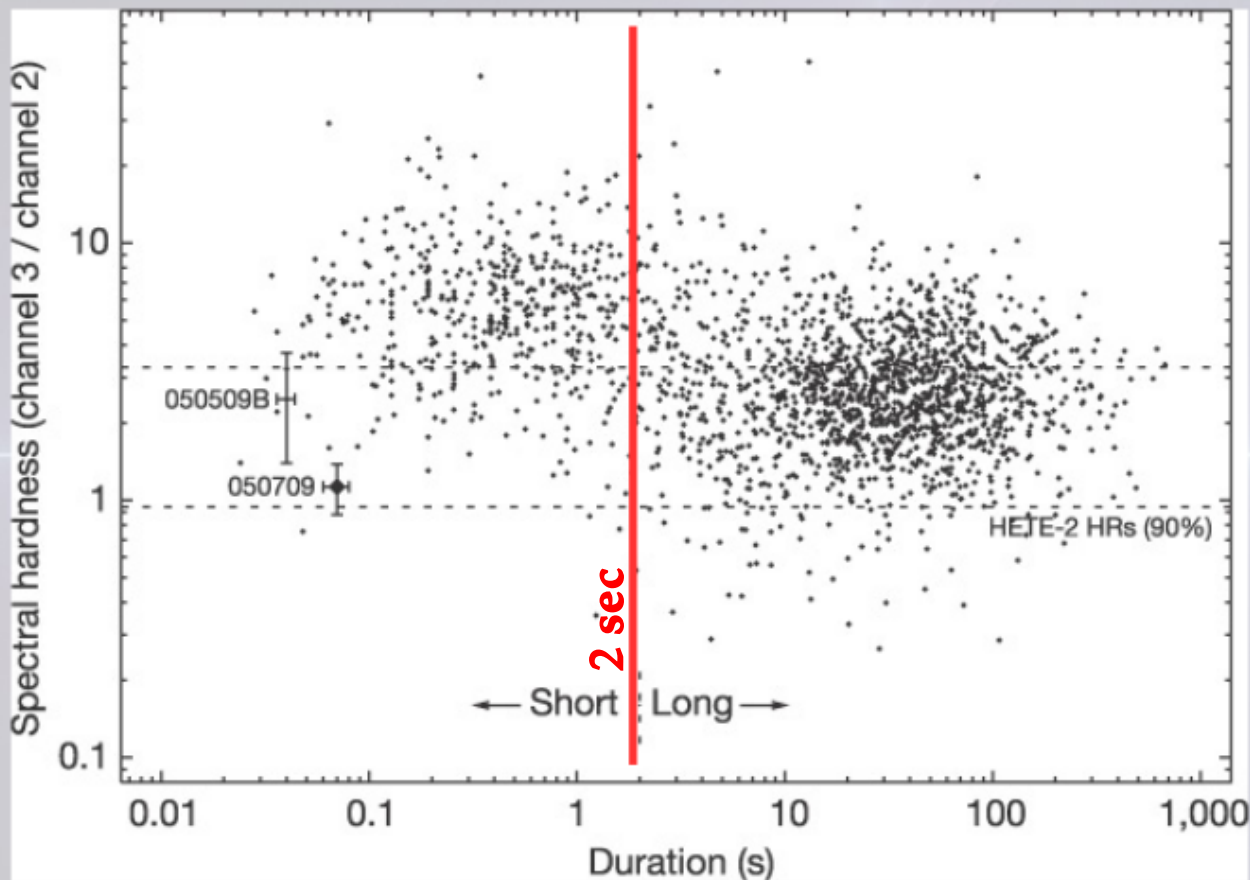
– daily observations

– majority of the energy is measured in γ -rays

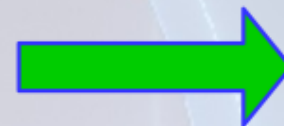
– there is a so-called “afterglow” observed at softer wavelength (X-ray, optical, IR, radio...) after the prompt γ -emission

What are GRBs?

At least two, physically distinct types of objects

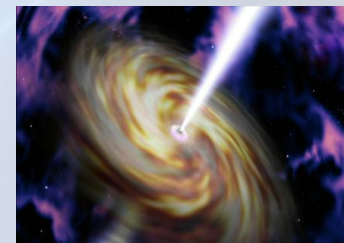


Credit: Hjorth+2005



Long/soft:
Massive Stars
at
collapse

a “collapsar”



Short/hard: two Compact Objects at merger

binarity!
GWs!

→ sub-Solar metallicities? ✓

→ fast-rotating stars? ✓

→ stars in a binary system?

Coming today! :)

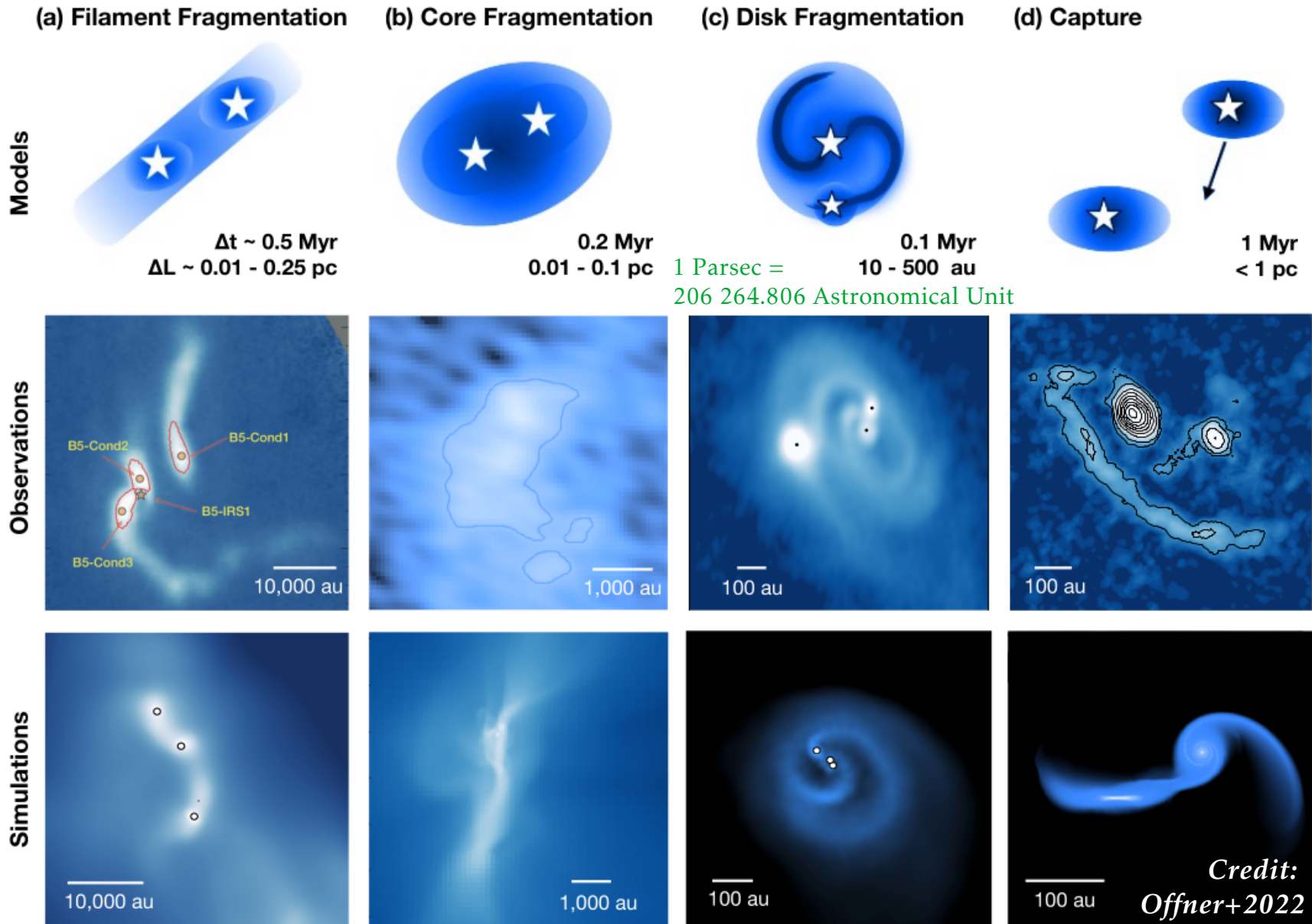


Binaries

...and other multiple systems

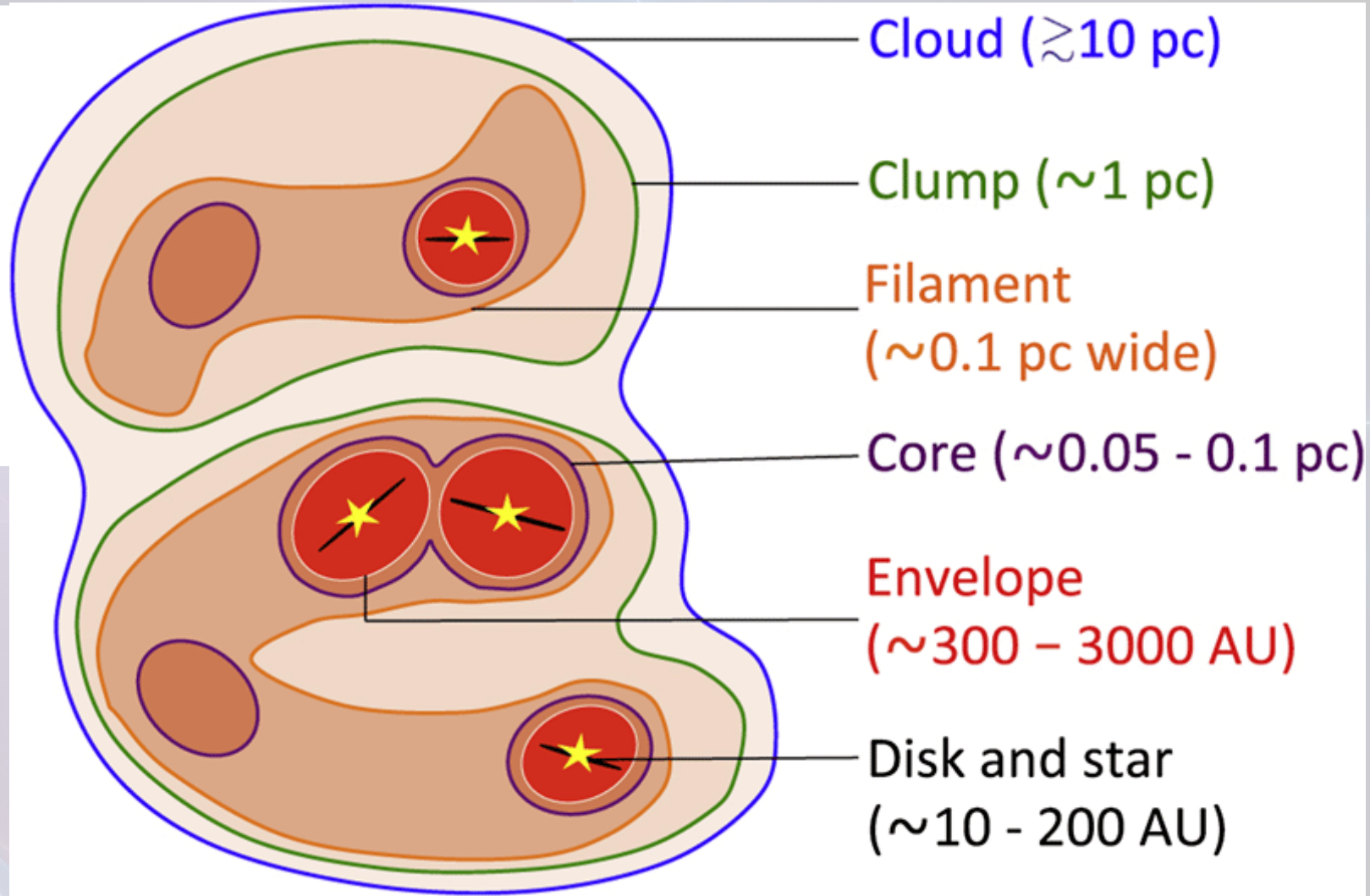
Stars sometimes form in multiples

binaries, triples, quadruples...

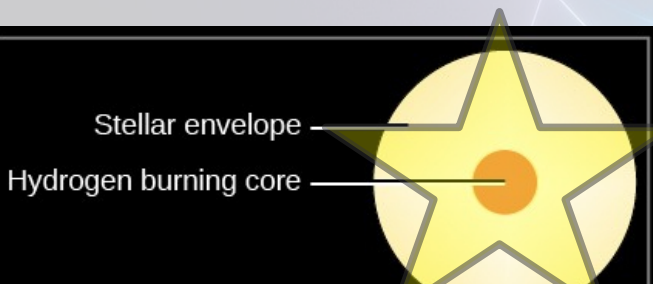


Reminder:

Structure
of a
molecular cloud
(where stars are
born)

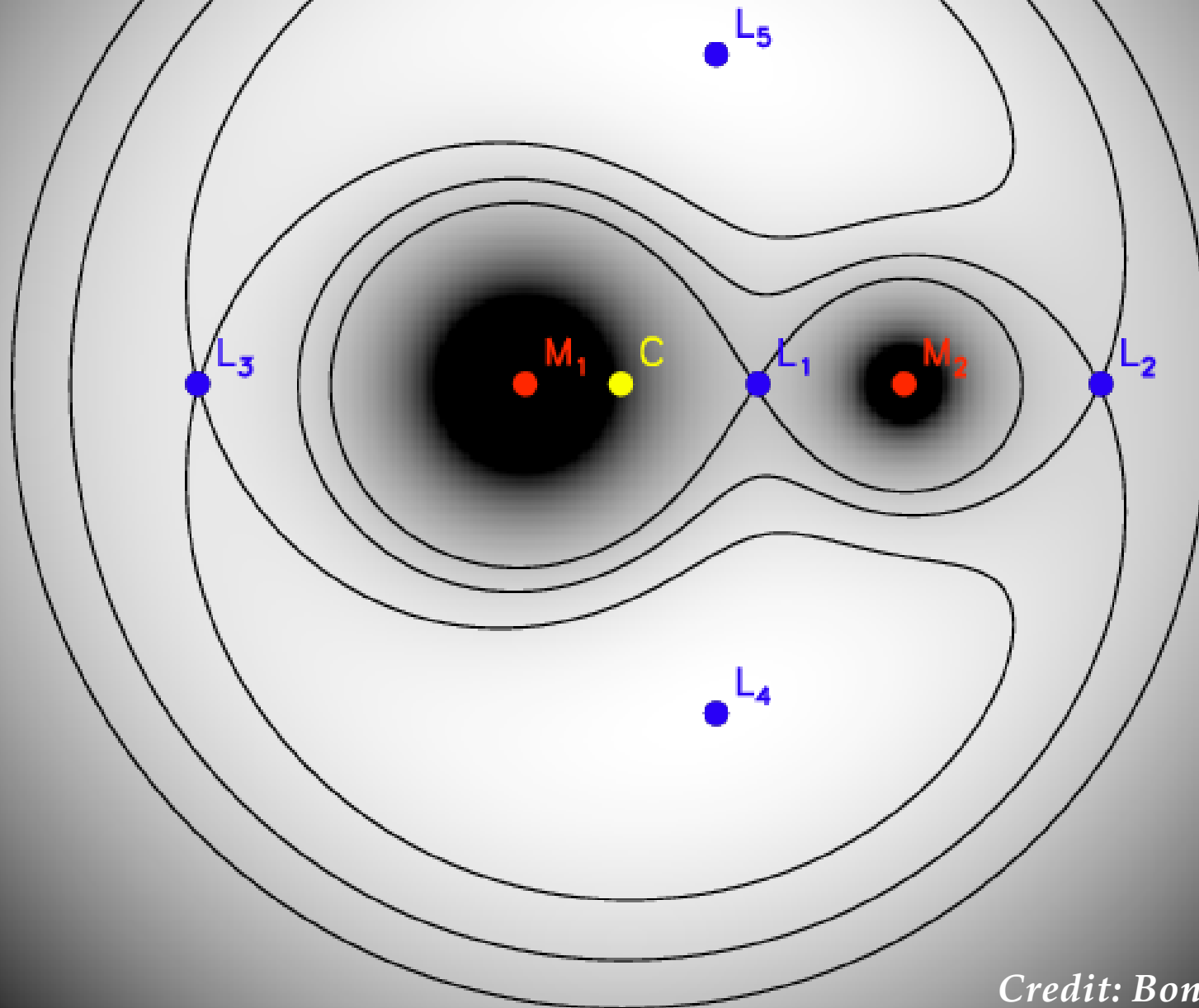


Credit:
A. L. Rosen
et al. (2020)

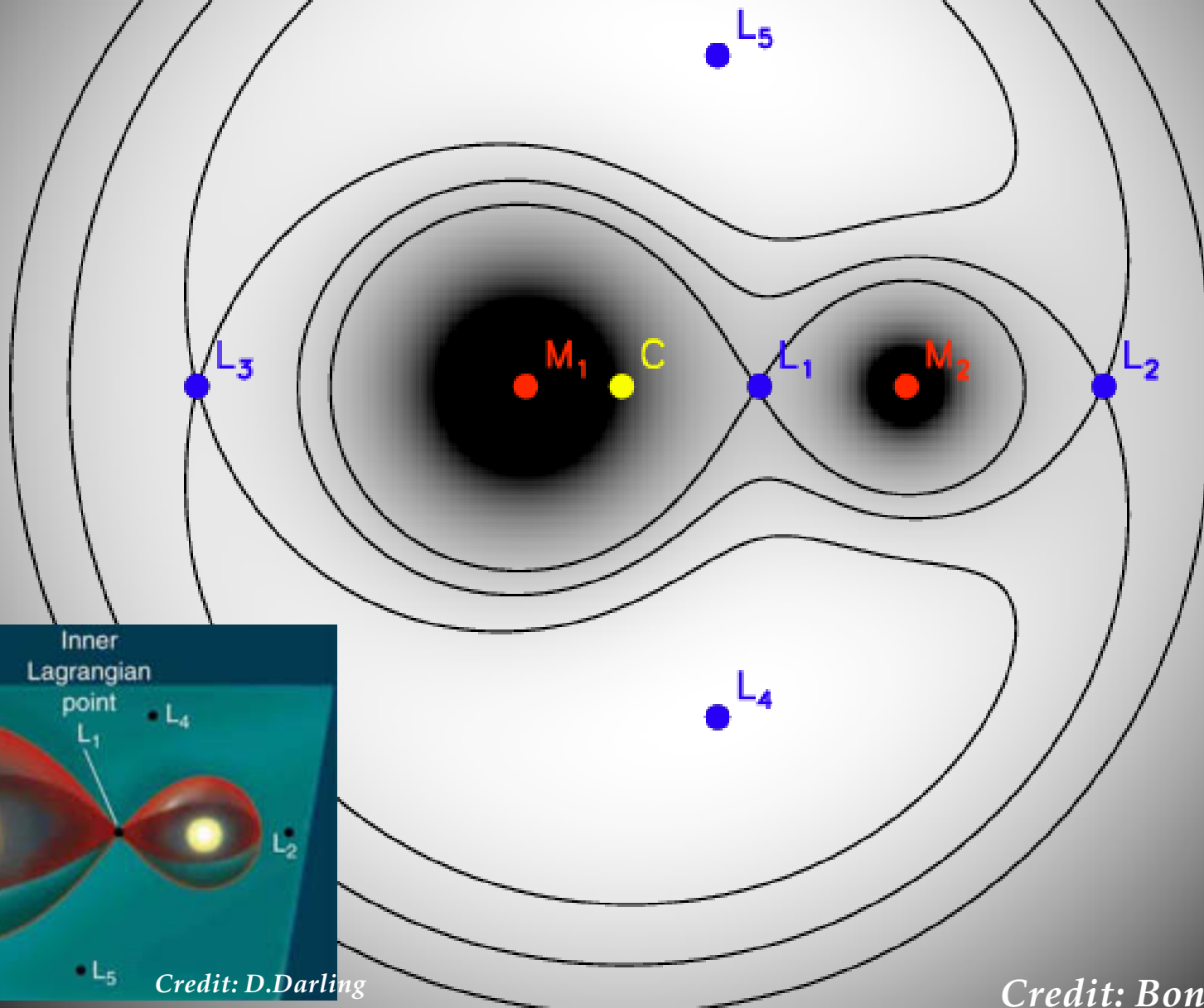


'envelope' here \neq stellar envelope
'core' here \neq stellar core

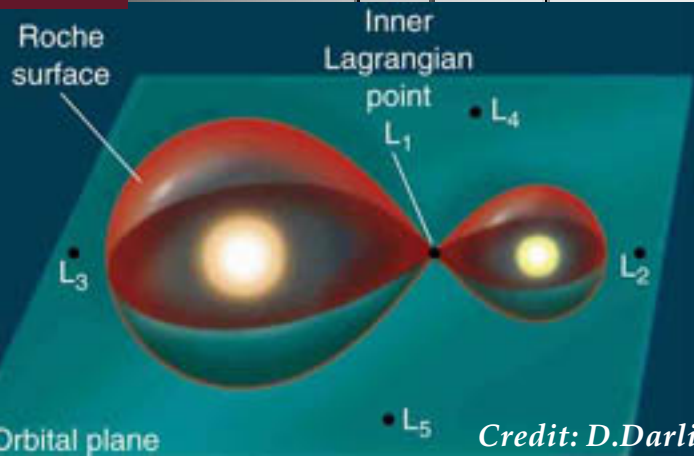
The most important concept: **Roche-lobe**



The most important concept: Roche-lobe



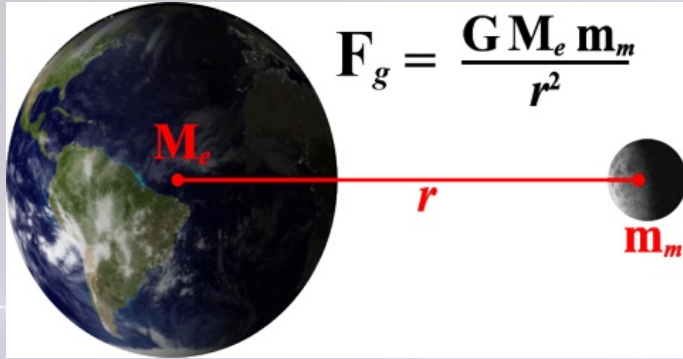
in 3D:



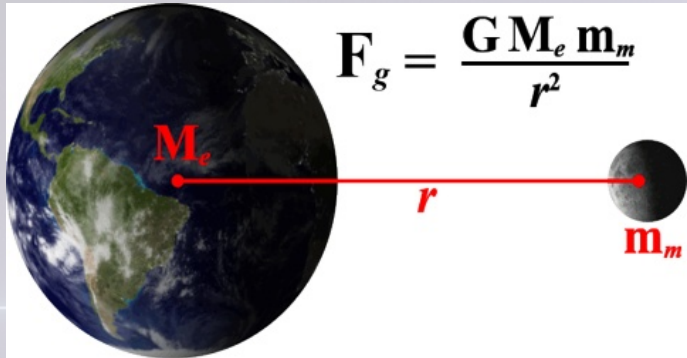
Credit: D.Darling

Credit: Bonneau+15

Gravitational equipotential surfaces



Gravitational equipotential surfaces



$$F_g = \frac{GM_e m_m}{r^2}$$

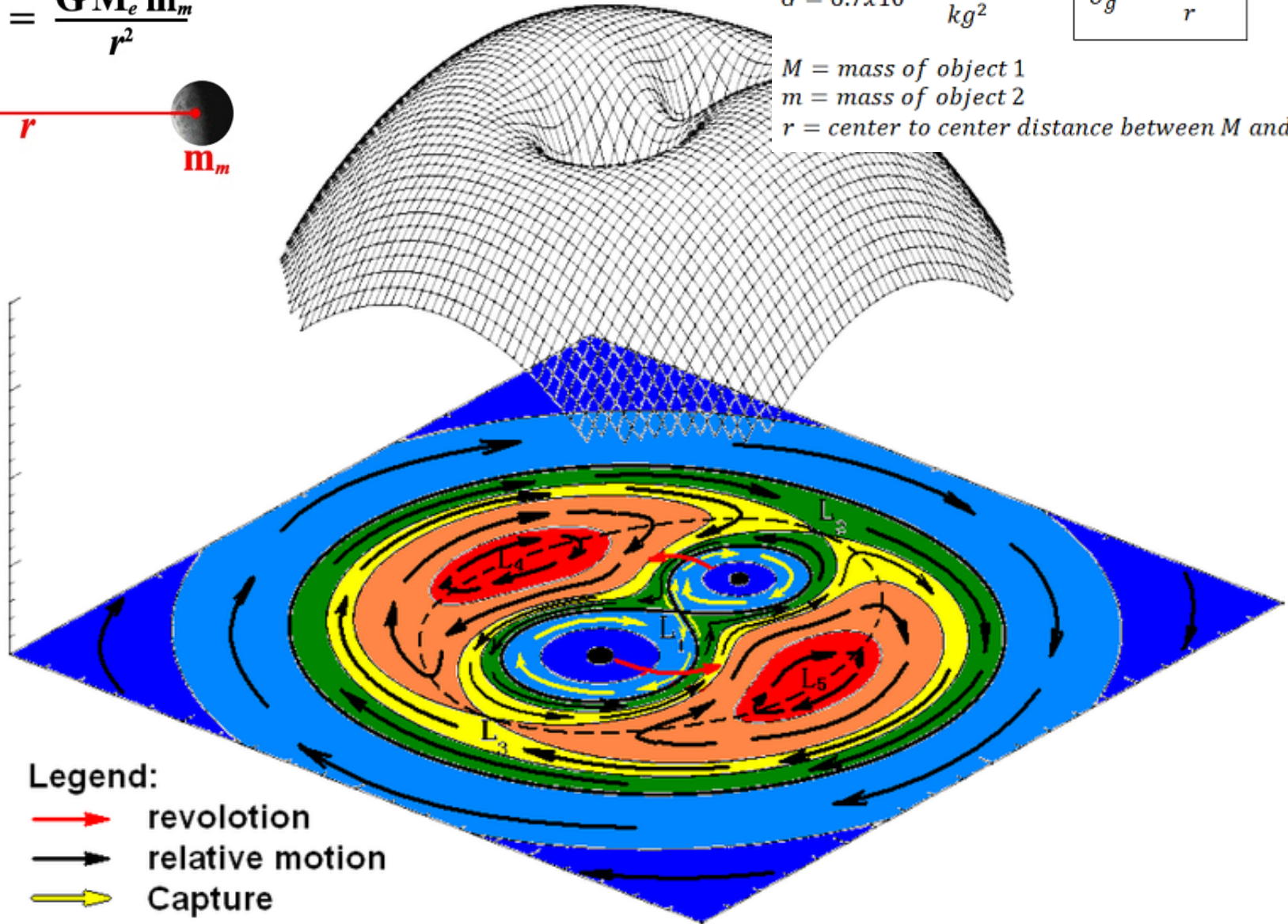
$$G = 6.7 \times 10^{-11} \frac{Nm^2}{kg^2}$$

$$U_g = \frac{-GMm}{r}$$

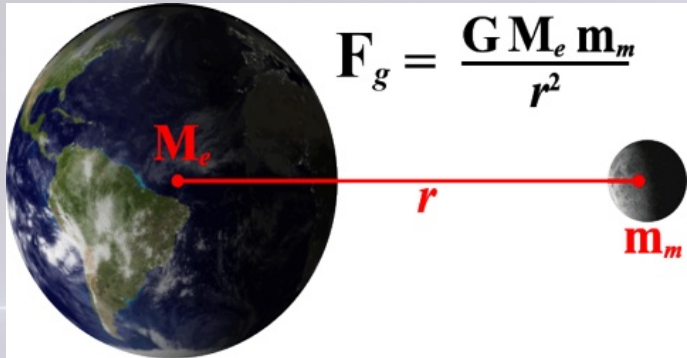
M = mass of object 1

m = mass of object 2

r = center to center distance between M and m



Gravitational equipotential surfaces



$$\mathbf{F}_g = \frac{GM_e m_m}{r^2}$$

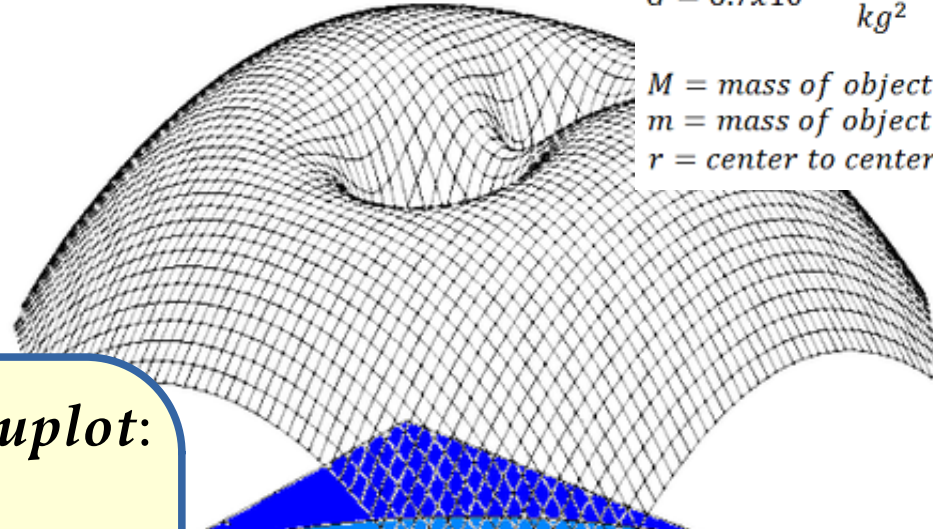
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Try it for yourself! E.g. in *gnuplot*:

$$U(x,y) = (-G*m1/\sqrt{x**2+y**2}) - G*m2/\sqrt{(x-orbsep)**2+y**2})/Rsun$$

`m1=20; m2=15; orbsep=5 #[Msun],[Rsun]`

`G=6.6743*10**(-8); Rsun=6.957*10**(10) #[cgs]`

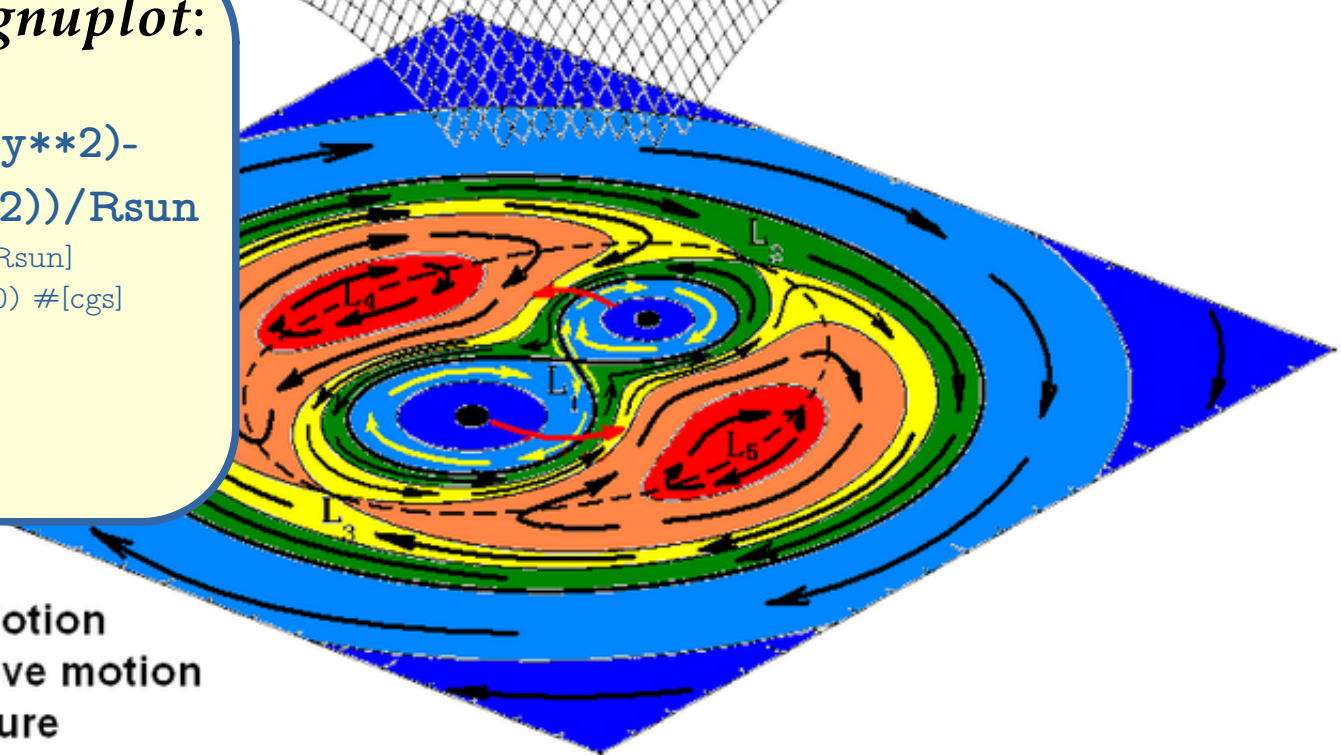
`set isosamples 60,60`

`set pm3d`

`splot U(x,y)`

Legend:

-  revolution
-  relative motion
-  Capture



Roche-lobe facts

- we can plot it but we cannot explicitly derive it

Roche-lobe facts

- we can plot it but we cannot explicitly derive it

⇒ approximation of Roche lobe

(Eggleton 1983) $q = m_1/m_2$:
from numerical fit

$$RL_1 = A \frac{0.49q^{2/3}}{0.6q^{2/3} + \ln(1 + q^{1/3})}$$

orbital separation: A

Roche-lobe facts

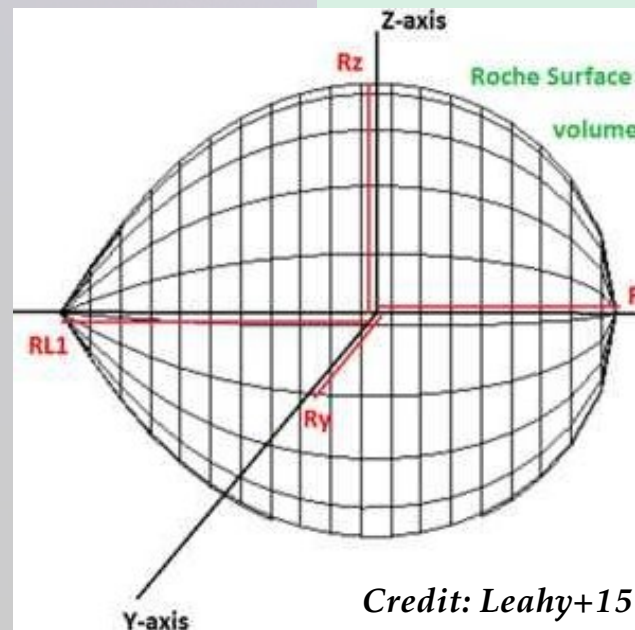
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Roche-lobe facts

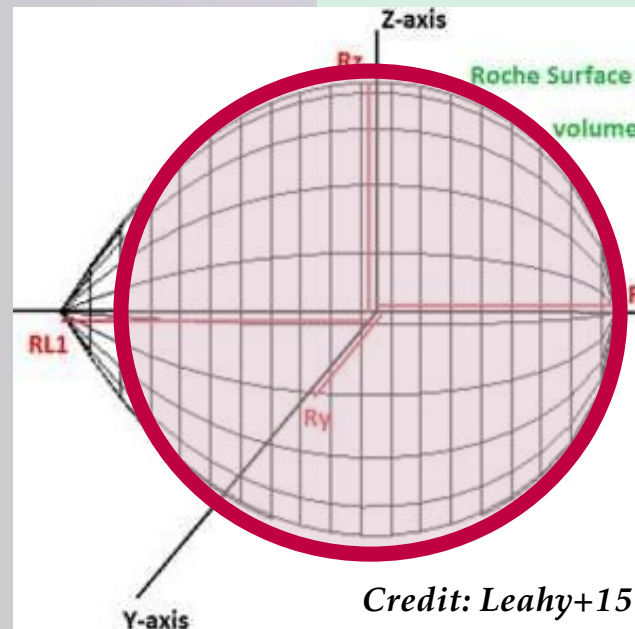
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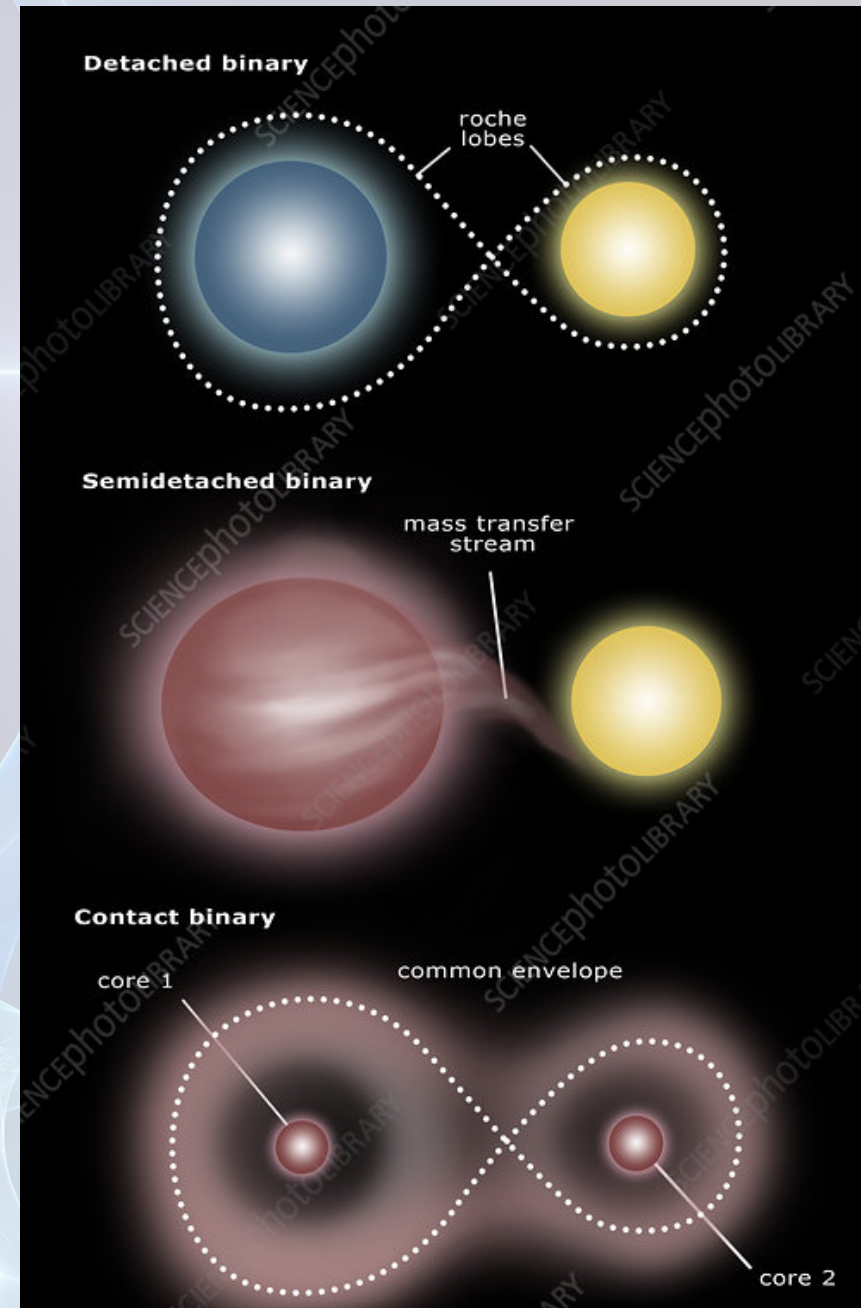


Why does the Roche-lobe matter?

- Mass transfer.

Why does the Roche-lobe matter?

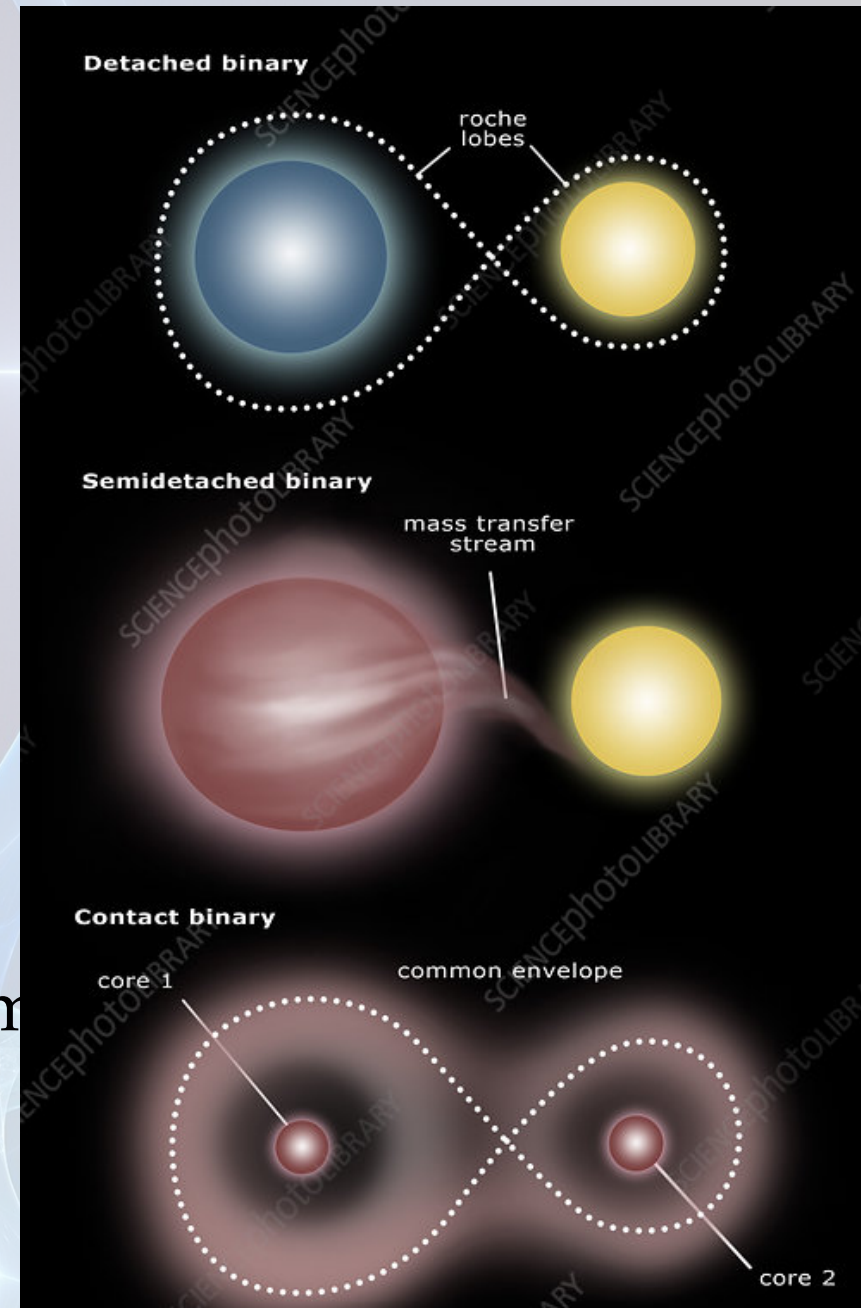
- Mass transfer.



Why does the Roche-lobe matter?

- Mass transfer.
- Some important terms:
 - primary/secondary (companions)
 - donor/accretor
 - M_1/M_2
 - detached system
 - Roche-lobe overflow
 - semi-detached, contact system
 - ‘common envelope’ (...)

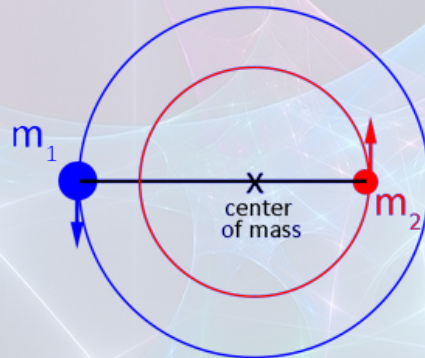
► *stellar envelope*



Some more terms

- orbital separation = orbital distance
- period = orbital period
 - \neq rotational period!! (though cf. *synchronization*)
e.g. due to tidal forces
- initial orbital separation *vs.* actual
- initial period *vs.* actual
- Connection between distance & period?

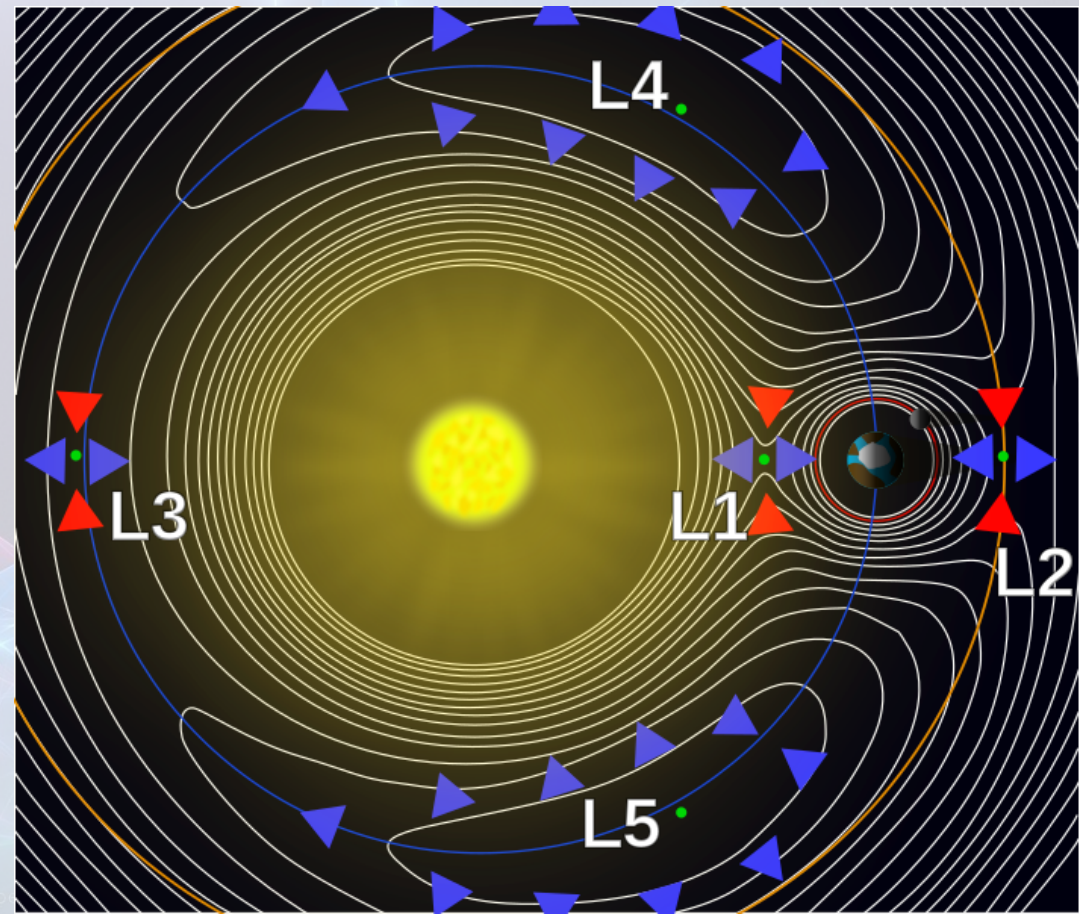
Kepler's 3rd law:



$$P^2 = \frac{4\pi^2}{G(M_1 + M_2)} r^3$$

Some more terms *part #2*

- ***Lagrangian points***: where the gravitational forces of the two bodies and the centrifugal force balance each other



Imagine two (massive) stars!

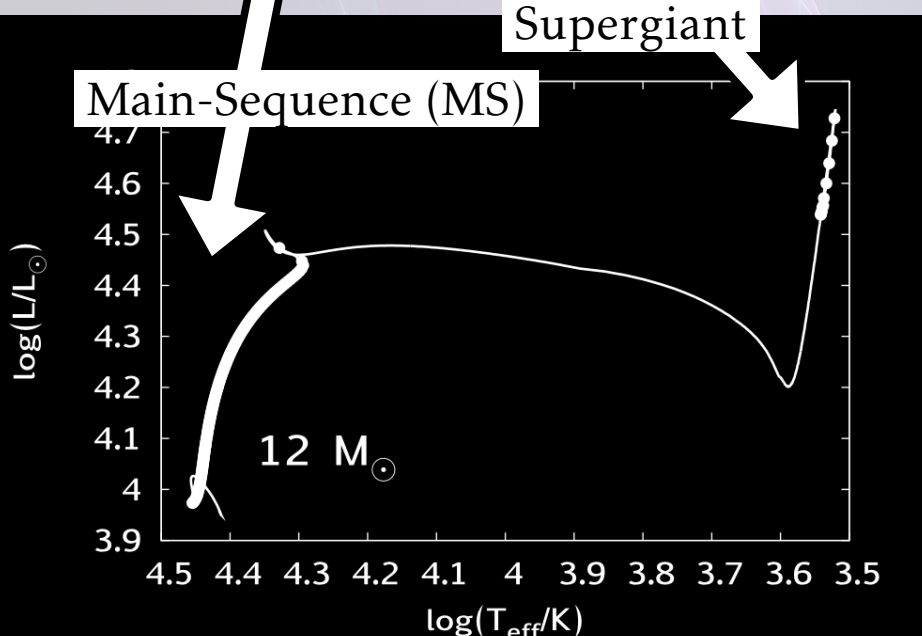
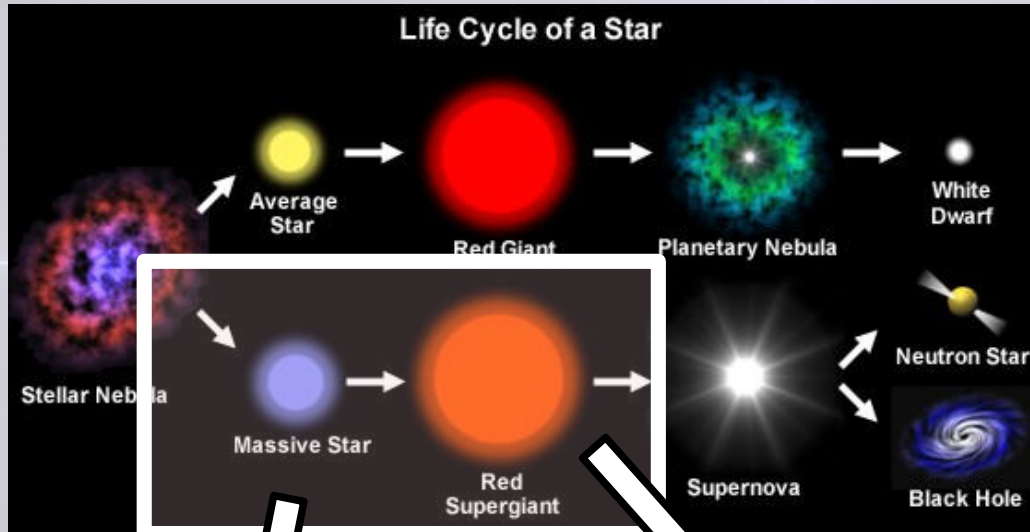
with Solar Z, no rotation
Imagine two (massive) stars!

with Solar Z, no rotation

Imagine two (massive) stars!

One (massive) star alone:

Two of them next to each other:

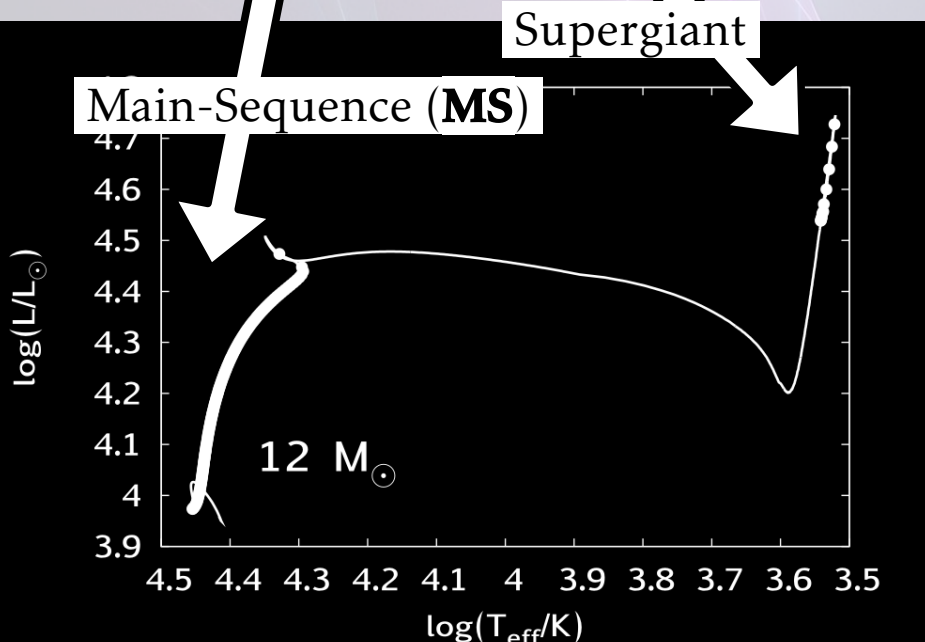
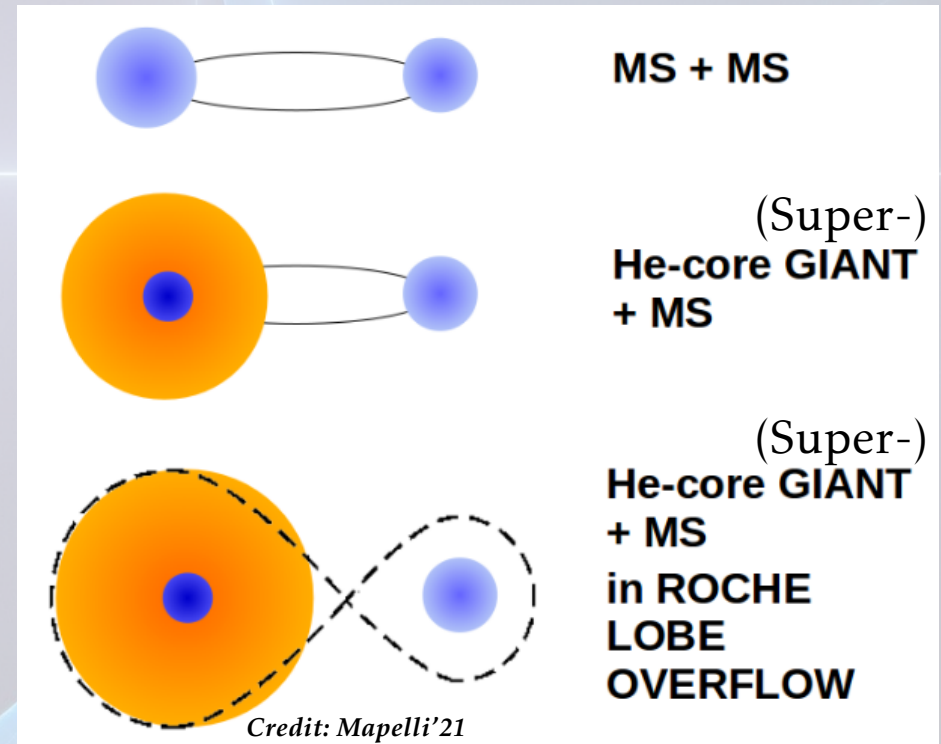
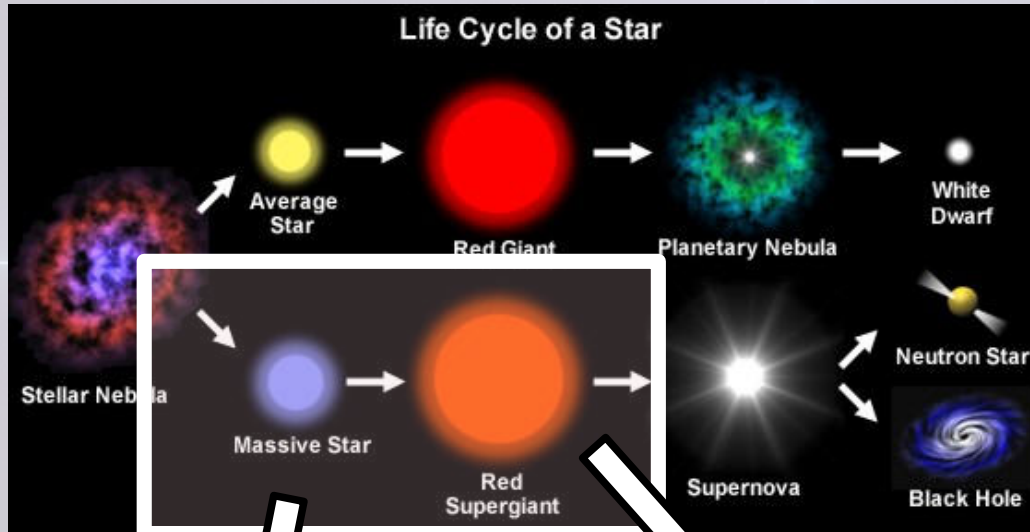


with Solar Z, no rotation

Imagine two (massive) stars!

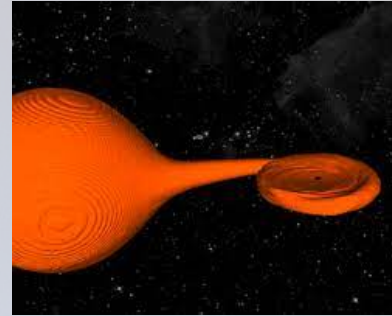
One (massive) star alone:

Two of them next to each other:



- $\tau(m) \sim m^{-2.5}$
 - Sun's lifetime: $\sim 10^{10}$ yrs
 - an 8 M_⊙ star's lifetime: $\sim 5 \times 10^7$ yrs
 - a 100 M_⊙ star's lifetime: $\sim 2 \times 10^6$ yrs

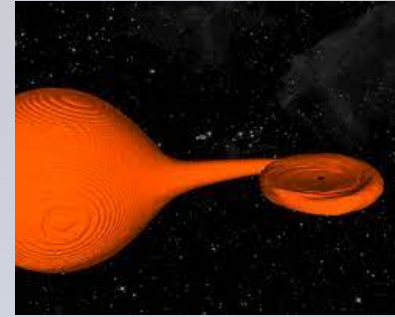
What happens when the Roche-lobe is overflowed?



- Mass transfer
 - = mass exchange
 - = (binary) interaction

Youtube video to watch:
[youtube.com/watch?v=xAjq7VGnf4s](https://www.youtube.com/watch?v=xAjq7VGnf4s)

What happens when the Roche-lobe is overflowed?



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 - = (binary) interaction

Youtube video to watch:
youtube.com/watch?v=xAjq7VGnf4s

Next time.